

# Muon $g - 2$ and Lepton Flavour Violation in the MRSSM

Dominik Stöckinger, TU Dresden

Collaborators: Wojciech Kotlarski, Hyejung Stöckinger-Kim

Matter to the Deepest Conference, Katowice, September 2019

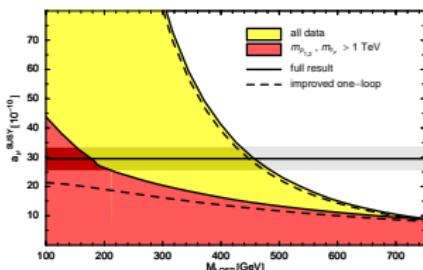
# Motivation: low-energy lepton observable $g - 2$

$$(g-2)_\mu^{\text{Exp.}} - a_\mu^{\text{SM}} = (28.1 \pm 6.3^{\text{Exp.}} \pm 3.6^{\text{Th(KNT18)}}) \times 10^{-10}$$

New experiment at Fermilab(E969):  $\sim 0.16$  ppm

Question in preparation of new experiment:

- Which models predict what?
- Outcome: interesting scenarios, other experimental tests?



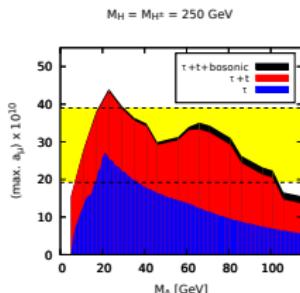
[DS '06]

→ Dark Matter, LHC constraints,  $M_h$

Heaviest SUSY  
( $\tan \beta \rightarrow \infty$ )  
[Bach, Park, DS, Stöckinger-Kim '15]

→ Higgs couplings, flavour, vacuum

stability



[Cherchiglia, DS, Stöckinger-Kim '17]

→ tau-physics, LHC-Higgs/Yukawa

# Motivation: more low-energy lepton observables

$(g - 2)_\mu$ :  $a_\mu^{\text{Exp.}} - a_\mu^{\text{SM}} = (28.1 \pm 6.3^{\text{Exp.}} \pm 3.6^{\text{Th(KNT18)}}) \times 10^{-10}$   
New experiment at Fermilab(E969):  $\sim 0.16$  ppm

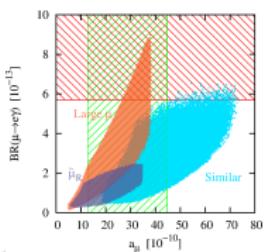
$\mu \rightarrow e\gamma$ :  $B_{\mu^+ \rightarrow e^+\gamma} = \frac{\Gamma(\mu \rightarrow e\gamma)}{\Gamma(\mu \rightarrow e\nu_\mu \bar{\nu}_e)} < 4.2 \times 10^{-13}$  (MEG 2016)  
Future MEG-II: expect to improve sensitivity  $\sim 5 \times 10^{-14}$

$\mu \rightarrow e$ :  $B_{\mu\text{Au} \rightarrow e\text{Au}} < 7 \times 10^{-13}$  (SINDRUM 2006)  
Future COMET and Mu2E: expected  $7.2 \times 10^{-15}$

Question:

- (Non-)correlations? Sensitivity to which models?

[Kersten, Park, DS, Velasco-Sevilla '14]



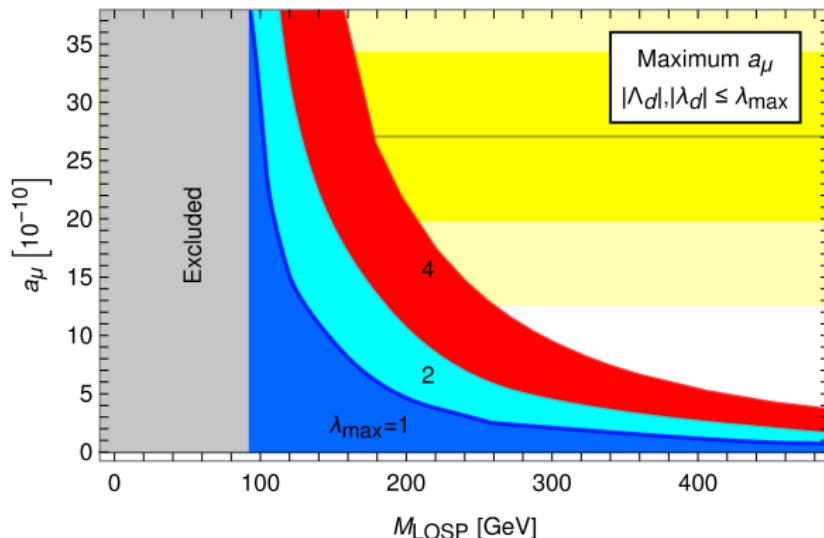
# Motivation: Supersymmetry with R-symmetry

- Supersymmetry is one of the most attractive ideas for BSM
- It becomes even more attractive with R-symmetry [Kribs, Poppitz, Weiner]
- MRSSM is realization of SUSY **distinct** from MSSM
- Surprisingly rich and successful phenomenology [Diessner, Kalinowski, Kotlarski, DS'14-'19]

## Question:

- What are the possible MRSSM contributions to  $a_\mu$ ?
- (Non-)correlations with LFV?

# First answer/preview



Result:

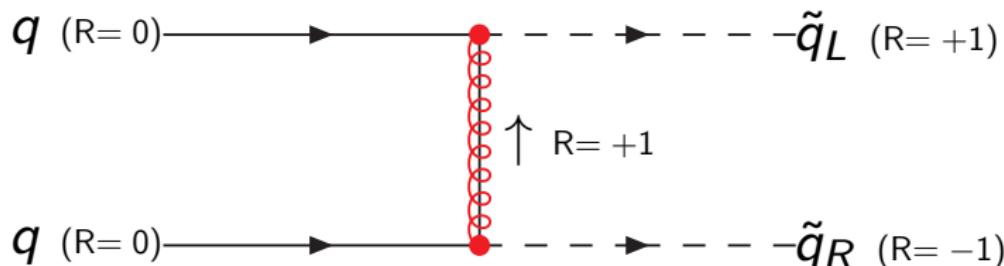
$a_\mu$  much smaller  
in MRSSM than  
in MSSM

Next questions/remainder of the talk:

- Why? Detailed influence of MRSSM parameters?
- Lepton flavour violation LFV — study!

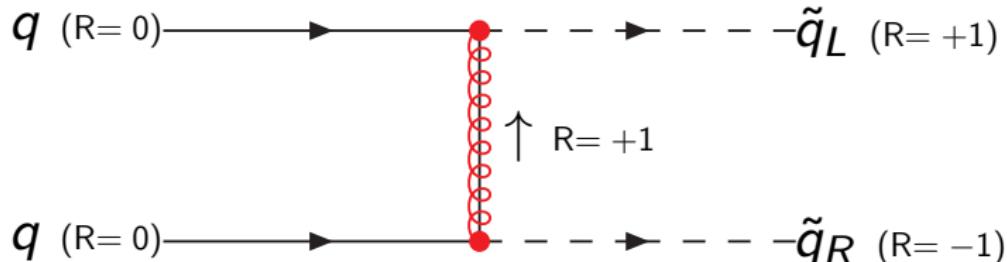
# Definition MRSSM

[Kribs, Poppitz, Weiner]



# Definition MRSSM

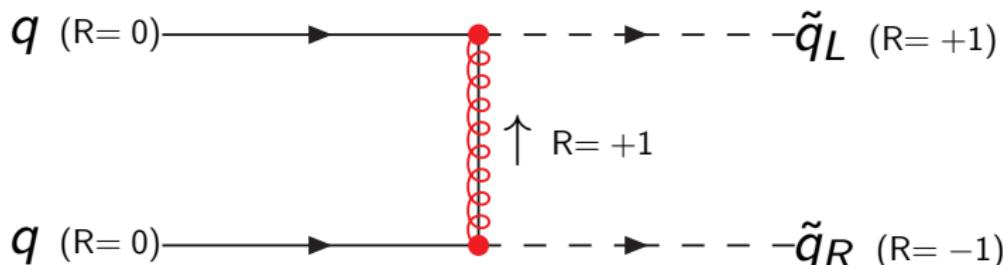
[Kribs, Poppitz, Weiner]



- MRSSM: beautiful alternative realization of SUSY
- R-symmetry: conserved U(1) R-charge (in superspace:  $\theta \rightarrow e^{i\alpha} \theta$ )
- no sfermion L/R mixing
- Dirac gauginos/Higgsinos, hence Dirac partner fields  $\hat{R}_{u,d}$ ,  $\hat{S}$ ,  $\hat{T}$ ,  $\hat{O}$

# Definition MRSSM

[Kribs, Poppitz, Weiner]



- Minimal: fewer parameters than MSSM (though more EW par.)

$$W_{\text{MRSSM}} = \dots + \mu \hat{H}_u \hat{H}_d + \mu_u \hat{R}_u \hat{H}_u + \Lambda_u \hat{H}_u \hat{T} \hat{R}_u + y_u \hat{Q} \hat{H}_u \hat{U}$$

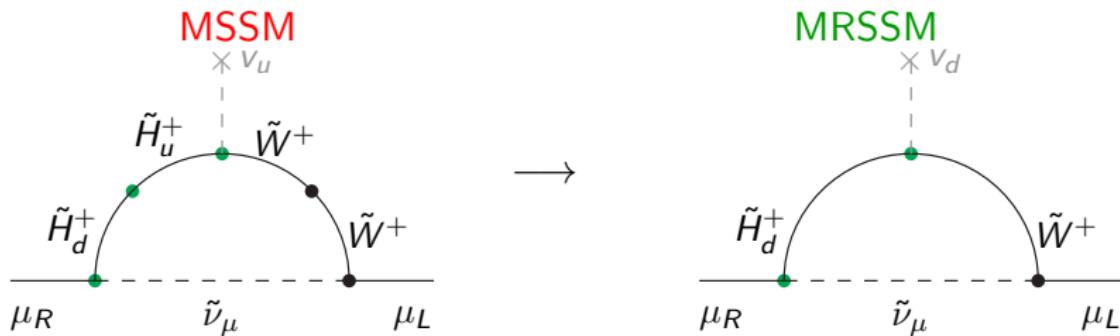
## Phenomenological successes:

- natural protection from FCNC [Kribs, Poppitz, Weiner]
- smaller LHC cross section, lower masses possible [Diessner, Kalinowski, Kotlarski, DS '19]
- new  $\Lambda, \lambda$ -par. increase  $M_h$  but don't mess up EWPO precision [DKKS 14]
- dark matter possible, and light extra Higgs/sparticles [DKKS 15]

## $g - 2$ : compare standard/R-symmetric SUSY

new Yukawa-like terms for Dirac partners  $\hat{R}_{u,d}$ ,  $\hat{T}$ ,  $\hat{S}$

$$W_{\text{MRSSM}} = \dots + \mu \hat{H}_u \hat{H}_d + \mu_u \hat{R}_u \hat{H}_u + \Lambda_u \hat{H}_u \hat{T} \hat{R}_u + y_u \hat{Q} \hat{H}_u \hat{U}$$



$$\text{MSSM} \propto \frac{v_u}{v_d} \tan \beta \sim 10 \dots 50$$

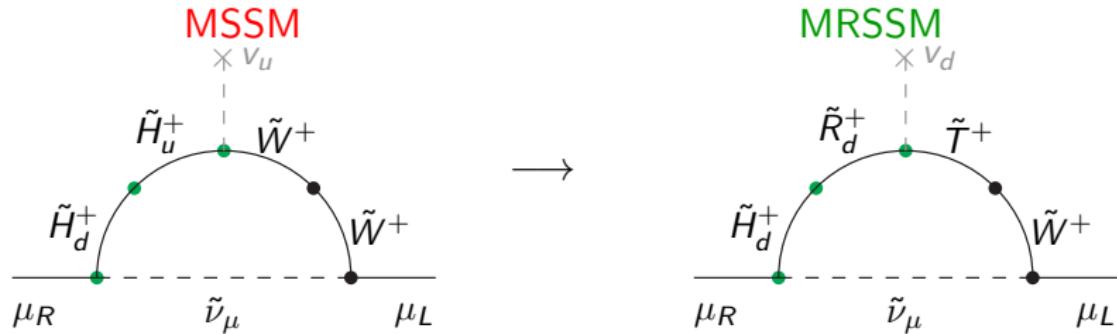
$$\text{MRSSM} \propto \frac{\Lambda_d}{g_2} \sim 1 \dots 5$$

- In all models: need chirality flip  $\rightsquigarrow$  VEV  $\rightsquigarrow$  enhancements
- Perturbativity and EWPO constrain  $\Lambda_i, \lambda_i$

## $g - 2$ : compare standard/R-symmetric SUSY

new Yukawa-like terms for Dirac partners  $\hat{R}_{u,d}$ ,  $\hat{T}$ ,  $\hat{S}$

$$W_{\text{MRSSM}} = \dots + \mu \hat{H}_u \hat{H}_d + \mu_u \hat{R}_u \hat{H}_u + \Lambda_u \hat{H}_u \hat{T} \hat{R}_u + y_u \hat{Q} \hat{H}_u \hat{U}$$

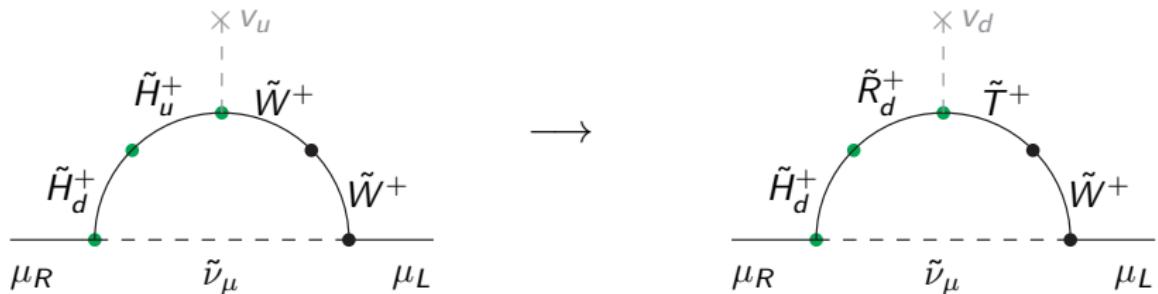


$$\text{MSSM} \propto \frac{v_u}{v_d} \tan \beta \sim 10 \dots 50$$

$$\text{MRSSM} \propto \frac{\Lambda_d}{g_2} \sim 1 \dots 5$$

- In all models: need chirality flip  $\rightsquigarrow$  VEV  $\rightsquigarrow$  enhancements
- Perturbativity and EWPO constrain  $\Lambda_i, \lambda_i$

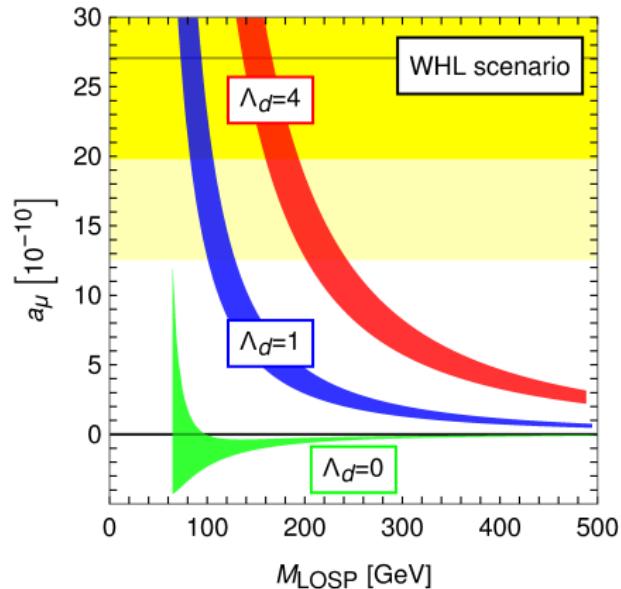
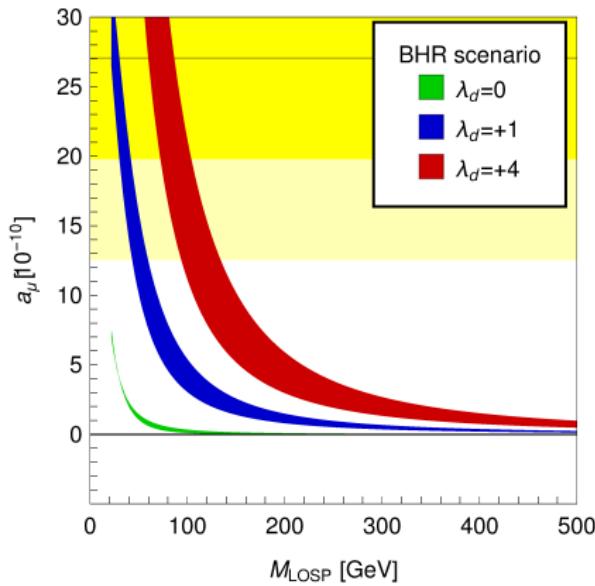
## $g - 2$ : compare standard/R-symmetric SUSY



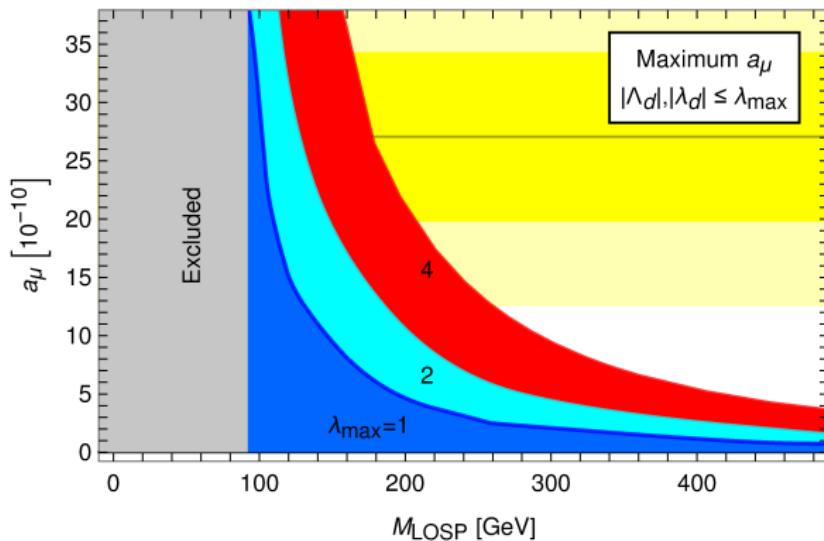
$$a_\mu^{\text{MSSM, WHL}} \approx \frac{g_2^2 \tan \beta}{16\pi^2} \frac{5}{12} \frac{m_\mu^2}{M_{\text{SUSY}}^2}, \quad a_\mu^{\text{MI (WHL/cn)}} \approx \frac{g_2 \Lambda_d}{16\pi^2} \frac{5}{12} \frac{m_\mu^2}{M_{\text{SUSY}}^2} \quad (1)$$

similar for BHL, BHR, ... (2)

# Results for $a_\mu$ in the MRSSM: WHL and BHR



# Results for $a_\mu$ in the MRSSM: general

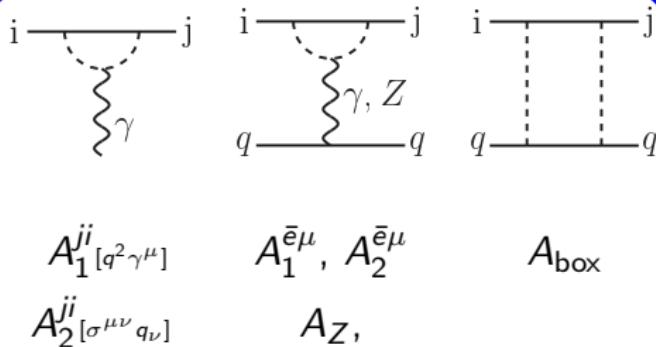


**Result:**  
 $a_\mu$  much smaller  
in MRSSM than  
in MSSM

## Reason and details:

- no  $\tan \beta$  enhancement, only enhancement by  $\Lambda_d, \lambda_d$
- Large  $a_\mu$  at most if several SUSY particles below 200 GeV and  $\Lambda_i \ll g_2$

# $a_\mu$ vs LFV observables

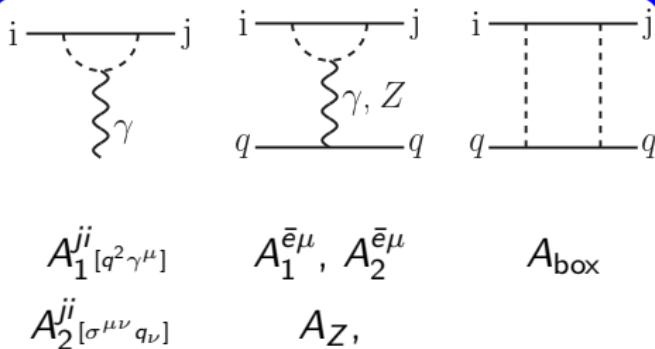


$$(g-2)_\mu \propto A_2^{\bar{\mu}\mu}$$

$$\mu \rightarrow e\gamma \propto A_2^{\bar{e}\mu}$$

$$\mu \rightarrow e \propto A_1^{\bar{e}\mu}, A_2^{\bar{e}\mu}, A_Z, A_{\text{box}}$$

# $a_\mu$ vs LFV observables



$$(g-2)_\mu \propto A_2^{\bar{\mu}\mu}$$
$$\mu \rightarrow e\gamma \propto A_2^{\bar{e}\mu}$$
$$\mu \rightarrow e \propto A_1^{\bar{e}\mu}, A_2^{\bar{e}\mu}, A_Z, A_{\text{box}}$$

Expect:

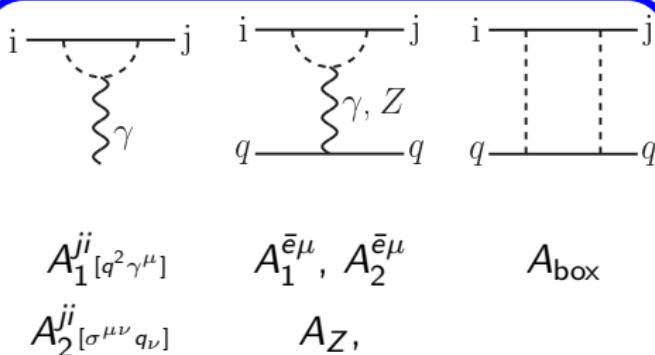
- ①  $a_\mu$  and  $\mu \rightarrow e\gamma$  always correlated
- ② correlation with  $\mu \rightarrow e$  conversion if dipole  $A_2$  dominates (large  $a_\mu$ )
- ③ this is usually not the case  $\rightsquigarrow$  interesting non-correlation

# $a_\mu$ vs LFV observables

LFV in MRSSM: flavour-transitions in slepton sector  $\mathcal{L} = \dots - (m_{\tilde{l}}^2)_{12} \tilde{l}_1^\dagger \tilde{l}_2$

LFV  $\propto$  dimensionless parameters  $\delta_{12}^L \equiv \frac{(m_{\tilde{l}}^2)_{12}}{m_{\tilde{l},11} m_{\tilde{l},22}}$ ,  $\delta_{12}^R \equiv \frac{(m_{\tilde{e}}^2)_{12}}{m_{\tilde{e},11} m_{\tilde{e},22}}$

- otherwise  $(g-2)_\mu$  and  $\mu \rightarrow e\gamma$  depend on same parameters
- $\mu \rightarrow e$  in addition: Z-couplings to Higgsinos and sleptons; squarks

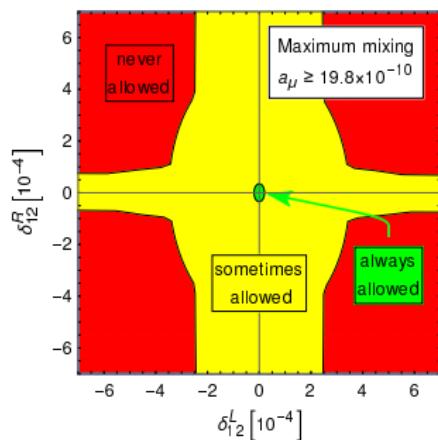
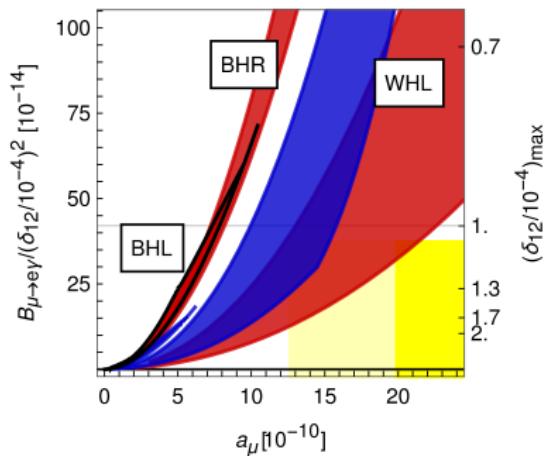


$(g-2)_\mu \propto A_2^{\bar{\mu}\mu}$   
 $\mu \rightarrow e\gamma \propto A_2^{\bar{e}\mu}$   
 $\mu \rightarrow e \propto A_1^{\bar{e}\mu}, A_2^{\bar{e}\mu}, A_Z, A_{\text{box}}$

# Results for $\mu \rightarrow e\gamma$ in the MRSSM

[Kotlarski,DS,Stöckinger-Kim]

$$a_\mu \propto A_2^{\bar{\mu}\mu L} + A_2^{\bar{\mu}\mu R} \quad B_{\mu \rightarrow e\gamma} \propto |A_{2\text{red}}^{\bar{e}\mu L}|^2 \times |\delta_{12}^L|^2 + |A_{2\text{red}}^{\bar{e}\mu R}|^2 \times |\delta_{12}^R|^2$$



**Expected:**  $a_\mu$  and  $\mu \rightarrow e\gamma$  correlated  
**Result:** True  $\rightsquigarrow$  distinctive patterns

**Apply:** max.  $\delta$ 's assuming  
 exptl. limits  $\rightsquigarrow$  tight!

## Results for $\mu \rightarrow e$ : details (sample scenario BHR)

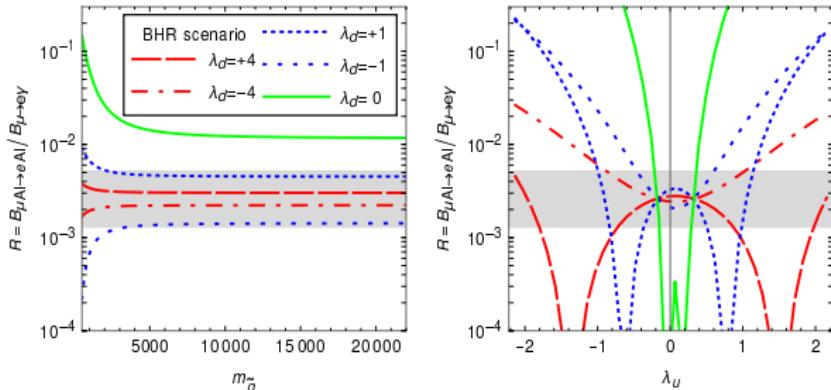
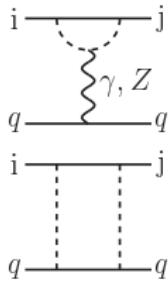
$$R(N) \equiv \frac{B_{\mu N \rightarrow e N}}{B_{\mu \rightarrow e \gamma}} \propto \frac{|A_2, A_1, A_Z, A_{\text{box}}|^2}{|A_2|^2}$$

(dependence on the  $\delta$ 's essentially drops out)

$$R^{\text{only } A_2}(AI) = 0.0026$$

Especially for  $A_2$  dominance: perfect correlation  
[Kitano, Koike, Okada, 2002]

# Results for $\mu \rightarrow e$ : details (sample scenario BHR)



**Expected:** correlation if dipole  $A_2$  dominates

- $\mu \rightarrow e\gamma$  MEG limit determines the max. possible  $\mu \rightarrow e$  rate

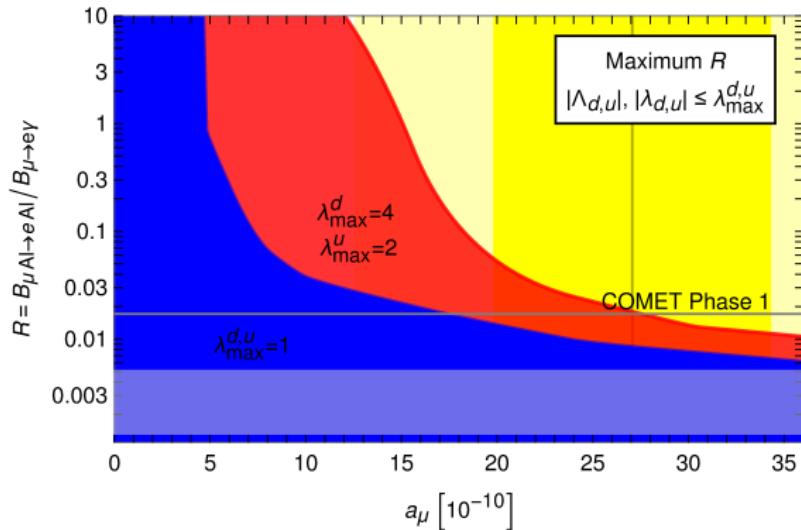
**Result:** often impact of form factors  $A_1$ ,  $A_Z$ ,  $A_{\text{box}}$   $\rightsquigarrow$  non-correlation

- Large  $\lambda_u \rightarrow A_Z$  dominance ( $Z$ -Higgsino coupling  $\sim v_u \lambda_u$ )

# Results for correlation $\frac{\mu \rightarrow e}{\mu \rightarrow e\gamma}$ in the MRSSM

Expected: correlation if dipole  $A_2$  dominates

Result:  $\Leftrightarrow$  large  $a_\mu$



[Kotlarski,DS,Stöckinger-Kim '19]

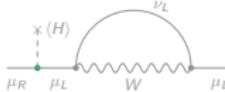
If  $a_\mu$  large  $\Rightarrow$   
narrow param. space

$m_{\text{LOSP}} < \sim 200 \text{ GeV}, \Lambda_i \gg g_i$

$\Rightarrow$  correlation  
MEG  
 $\Rightarrow \mu \rightarrow e$  small  
If  $\mu \rightarrow e$  observed  $\Rightarrow$   
 $a_\mu$  must be small

Typical behaviour:  $\sim$  chirality flip ( $\rightsquigarrow$  Higgs!) and masses

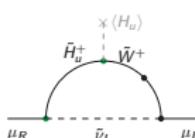
- EWSM:  $\alpha \frac{m_\mu^2}{M_W^2}$



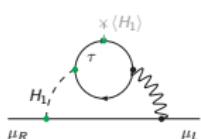
- $Z', A'$ :  $\alpha' \frac{m_\mu^2}{M_{Z'}^2}$



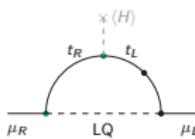
- SUSY:  $\alpha \frac{m_\mu^2 \tan \beta}{M_{\text{SUSY}}^2}$



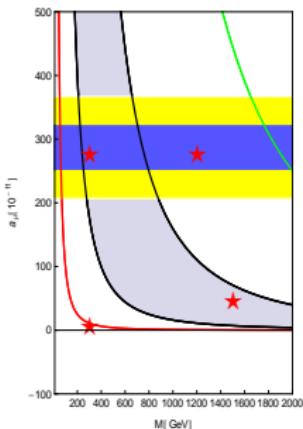
- 2HDM:  $\alpha^2 \tan^2 \beta \frac{m_\mu^2}{M_H^2}$



- LQ:  $g_L g_R \frac{m_\mu m_t}{M_{\text{LQ}}^2}$

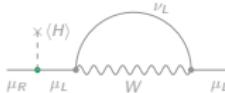


- rad.  $m_\mu \sim \frac{m_\mu^2}{M_{NP}^2}$



Typical behaviour:  $\sim$  chirality flip ( $\rightsquigarrow$  Higgs!) and masses

- EWSM:  $\alpha \frac{m_\mu^2}{M_W^2}$

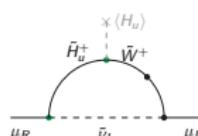


- $Z', A'$ :  $\alpha' \frac{m_\mu^2}{M_{Z'}^2}$   
No chiral enhancement

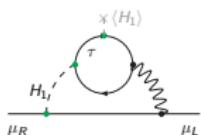
### No chiral enhancement



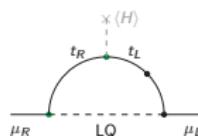
- SUSY:  $\alpha \frac{m_\mu^2 \tan \beta}{M_{\text{SUSY}}^2}$



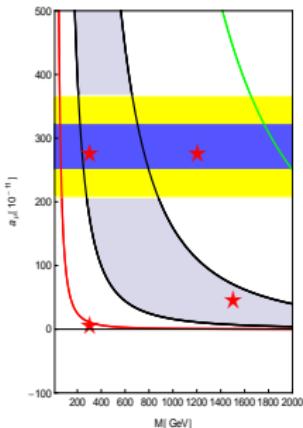
- 2HDM:  $\alpha^2 \tan^2 \beta \frac{m_\mu^2}{M_H^2}$



- LQ:  $g_L g_R \frac{m_\mu m_t}{M_{\text{LQ}}^2}$

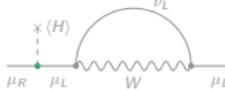


- rad.  $m_\mu \sim \frac{m_\mu^2}{M_{NP}^2}$



Typical behaviour:  $\sim$  chirality flip ( $\rightsquigarrow$  Higgs!) and masses

- EWSM:  $\alpha \frac{m_\mu^2}{M_W^2}$

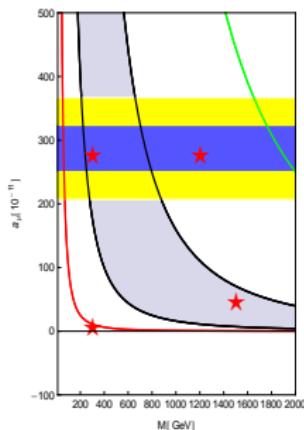


- $Z', A'$ :  $\alpha' \frac{m_\mu^2}{M_{Z'}^2}$

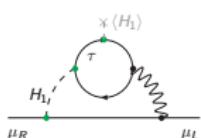


- SUSY:  $\alpha \frac{m_\mu^2 \tan \beta}{M_{\text{SUSY}}^2}$

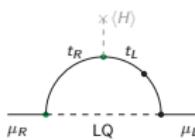
**Well-motivated. “Fits like a glove”**



- 2HDM:  $\alpha^2 \tan^2 \beta \frac{m_\mu^2}{M_H^2}$



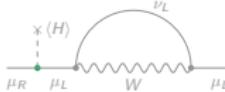
- LQ:  $g_L g_R \frac{m_\mu m_t}{M_{\text{LQ}}^2}$



- rad.  $m_\mu \sim \frac{m_\mu^2}{M_{NP}^2}$

Typical behaviour:  $\sim$  chirality flip ( $\rightsquigarrow$  Higgs!) and masses

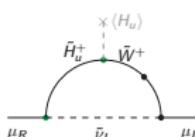
- EWSM:  $\alpha \frac{m_\mu^2}{M_W^2}$



- $Z', A'$ :  $\alpha' \frac{m_\mu^2}{M_{Z'}^2}$

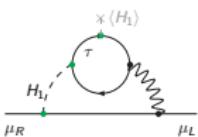


- SUSY:  $\alpha \frac{m_\mu^2 \tan \beta}{M_{\text{SUSY}}^2}$

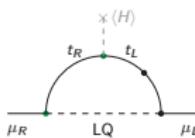


- 2HDM:  $\alpha^2 \tan^2 \beta \frac{m_\mu^2}{M_H^2}$

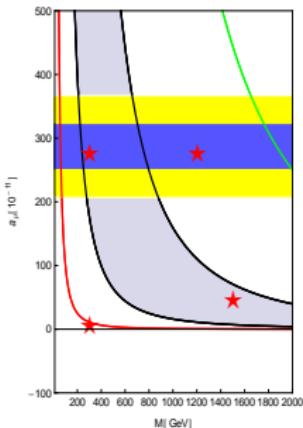
Well motivated; typically very small



- LQ:  $g_L g_R \frac{m_\mu m_t}{M_{\text{LQ}}^2}$

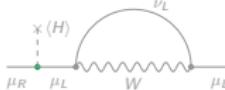


- rad.  $m_\mu \sim \frac{m_\mu^2}{M_{NP}^2}$



Typical behaviour:  $\sim$  chirality flip ( $\rightsquigarrow$  Higgs!) and masses

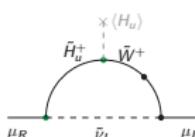
- EWSM:  $\alpha \frac{m_\mu^2}{M_W^2}$



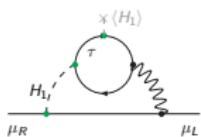
- $Z', A'$ :  $\alpha' \frac{m_\mu^2}{M_{Z'}^2}$



- SUSY:  $\alpha \frac{m_\mu^2 \tan \beta}{M_{\text{SUSY}}^2}$



- 2HDM:  $\alpha^2 \tan^2 \beta \frac{m_\mu^2}{M_H^2}$

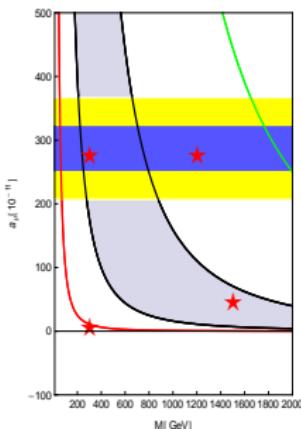


- LQ:  $g_L g_R \frac{m_\mu m_t}{M_{LQ}^2}$

Also possible, although difficult: B-physics.

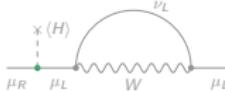
Beware:  $\Delta m_\mu / m_\mu \sim g_L g_R m_t / m_\mu$  restricts couplings

- rad.  $m_\mu \sim \frac{m_\mu^2}{M_{NP}^2}$



Typical behaviour:  $\sim$  chirality flip ( $\rightsquigarrow$  Higgs!) and masses

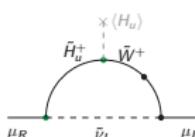
- EWSM:  $\alpha \frac{m_\mu^2}{M_W^2}$



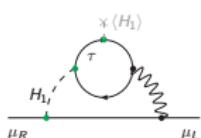
- $Z', A'$ :  $\alpha' \frac{m_\mu^2}{M_{Z'}^2}$



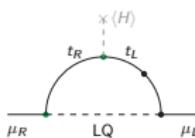
- SUSY:  $\alpha \frac{m_\mu^2 \tan \beta}{M_{\text{SUSY}}^2}$



- 2HDM:  $\alpha^2 \tan^2 \beta \frac{m_\mu^2}{M_H^2}$

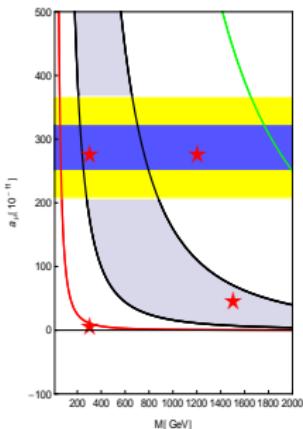


- LQ:  $g_L g_R \frac{m_\mu m_t}{M_{\text{LQ}}^2}$

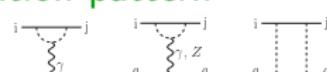


- rad.  $m_\mu$

Theoretical maximum. Need  $M_{\text{NB}} < \approx 2 \text{ TeV}$



# Conclusions

- R-symmetric SUSY challenges usual views on SUSY!
  - ▶ very different from standard SUSY, no MSSM limit
  - ▶ phenomenologically rich, viable for smaller  $M_{\text{SUSY}}$
  - ▶ Interplay  $a_\mu / \mu \rightarrow e\gamma / \mu \rightarrow e$
- MSSM:  $a_\mu$  large and LFV correlation pattern
- MRSSM:  $a_\mu$  small, not  $\propto \tan \beta$ 
- Suppose  $a_\mu$  large and MEG-limit ( $\mu \rightarrow e\gamma$ ) met
  - ▶ need very small/compressed  $M_{\text{SUSY}}$ ,  $\Lambda_i \gg g_i$
  - ▶ LFV-parameters  $\delta_{12}$  very small  $\leadsto$  non-generic!
  - ▶ Upper limit on  $\mu \rightarrow e \leadsto$  No COMET signal possible!
- If  $a_\mu$  small
  - ▶ Larger/non-compressed masses possible
  - ▶ COMET signal possible! Enhancements  $\propto \Lambda_u \dots$
- $a_\mu$  is hint for BSM — MSSM and MRSSM are viable and motivated
  - ▶ New  $a_\mu$  and LFV measurements could distinguish!

