



PRECISION PREDICTIONS FOR HIGGS-BOSON DIFFERENTIAL CROSS SECTIONS AT THE LHC MATTER TO THE DEEPEST 2019



Universität
Zürich^{UZH}



MC@NNLO

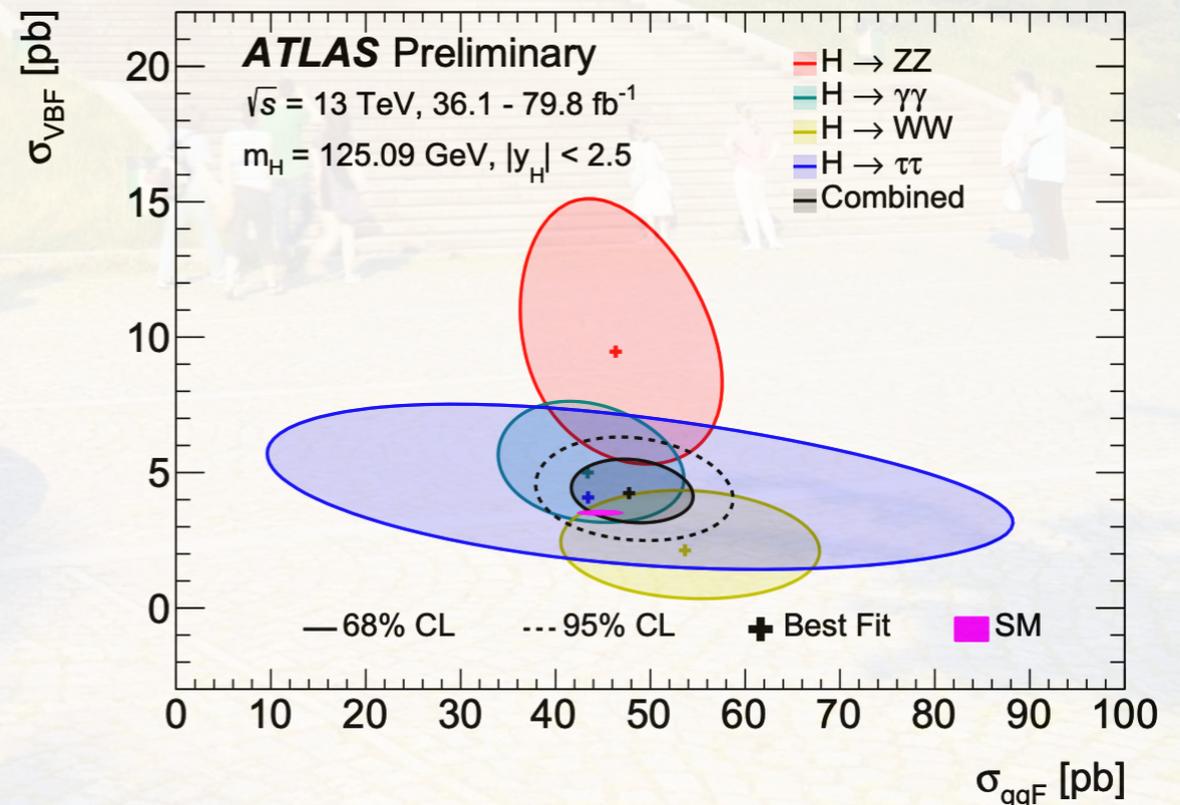
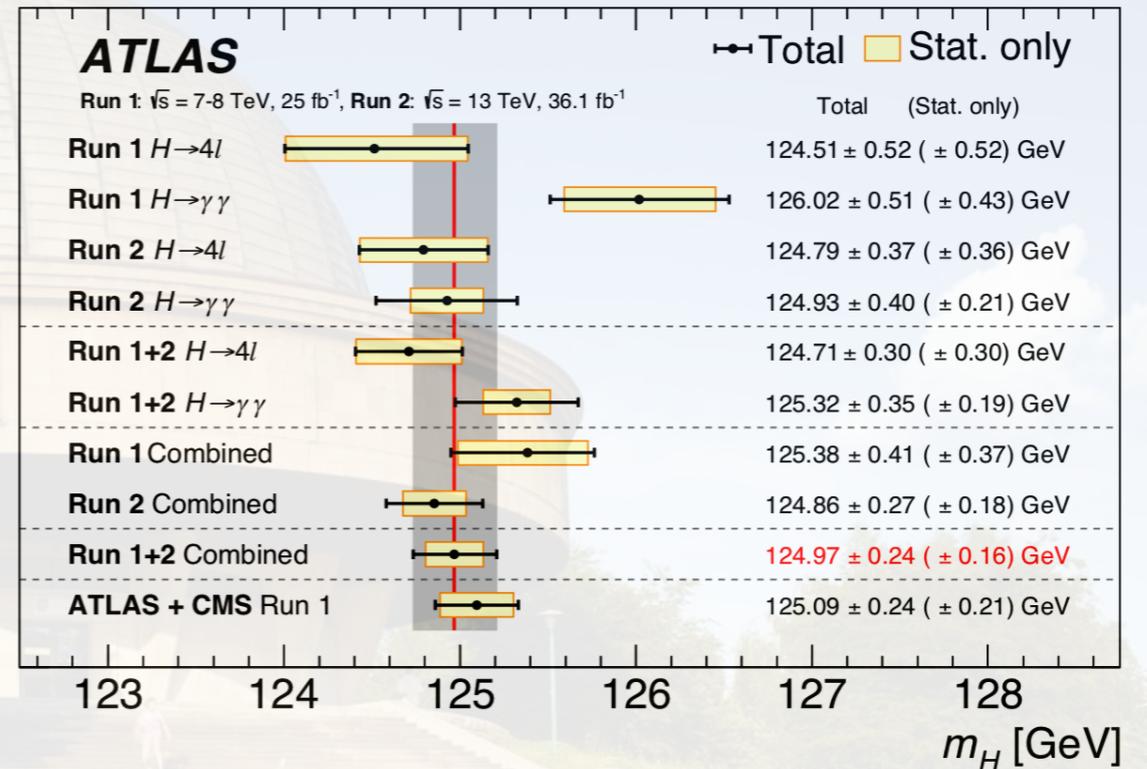
*Xuan Chen
Physik-Institut, Universität Zürich
Katowice, Poland, September 3, 2019*

OUTLINE

- Precision measurements and predictions of the Higgs boson
 - Current status from both theory and experiment (cherry pick)
 - Projection of HL-LHC, is it precise enough?
- Higgs production and decay processes in NNLOJET
- Higgs transverse momentum distribution in full spectrum
 - Small, medium and boosted regions
- Higgs rapidity distribution at N3LO (ggF channel)
- Summary

SUCCESS OF LHC HIGGS EXPERIMENTS

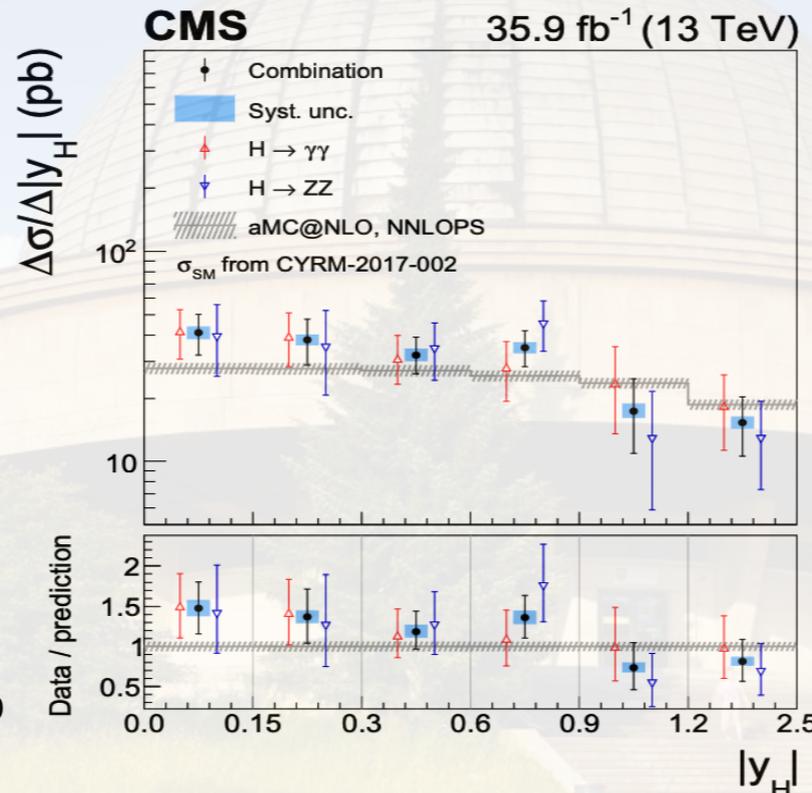
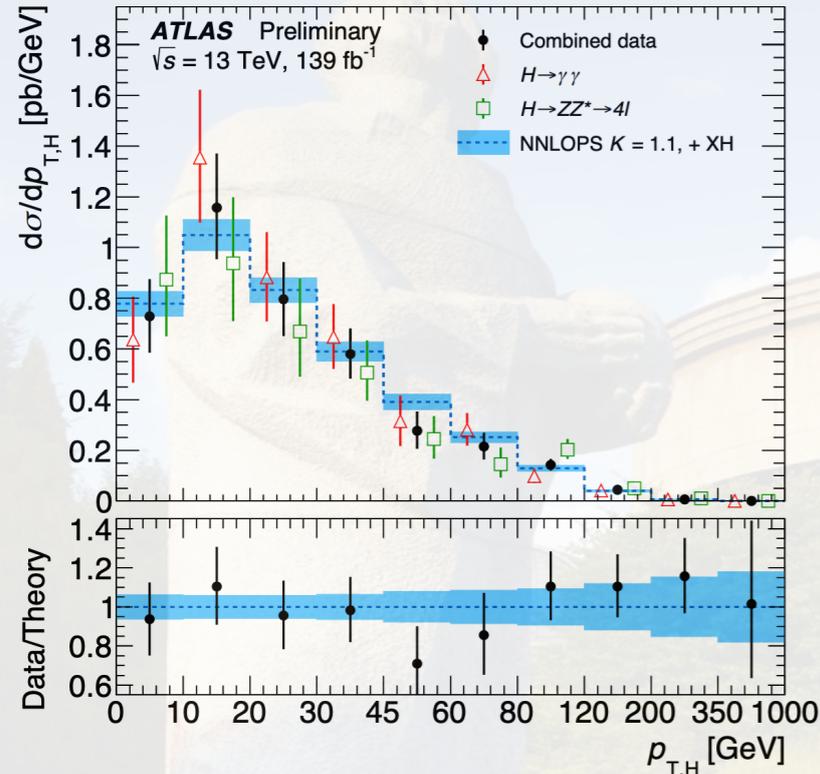
- Higgs boson properties in agreement with SM
 - Bosonic (Run I) and 3rd generation fermionic couplings (Run II) observed with current precision on coupling $\pm 10\text{-}20\%$ (EPS2019)
 - Higgs mass uncertainty at $\pm 0.2\%$ level (Run I + II)
 - Fiducial total cross section measured with $\pm 9\%$ accuracy (Run I + II)
 - 2nd generation fermion couplings still to be established
 - HH signal with 10 times SM exclusion limit
- Goal for the future: improve precision
 - Differential in production and decay channels
 - Projection to HL-LHC (estimate challenge)
 - Accelerate searches of new physics



1806.00242

ATLAS-CONF-2018-031

SUCCESS OF LHC HIGGS EXPERIMENTS



➤ Typical differential observables for Higgs (+jet) are:

$$\frac{d\sigma}{dp_T^H} \quad \frac{d\sigma}{d|y^H|} \quad \frac{d\sigma}{dp_T^{j1}} \quad \frac{d\sigma}{dN_{jets}}$$

➤ Inclusive decay observables are reconstructed from individual decay channel

➤ Combined results with $\pm 20\text{-}40\%$ uncertainties (EPS2019)

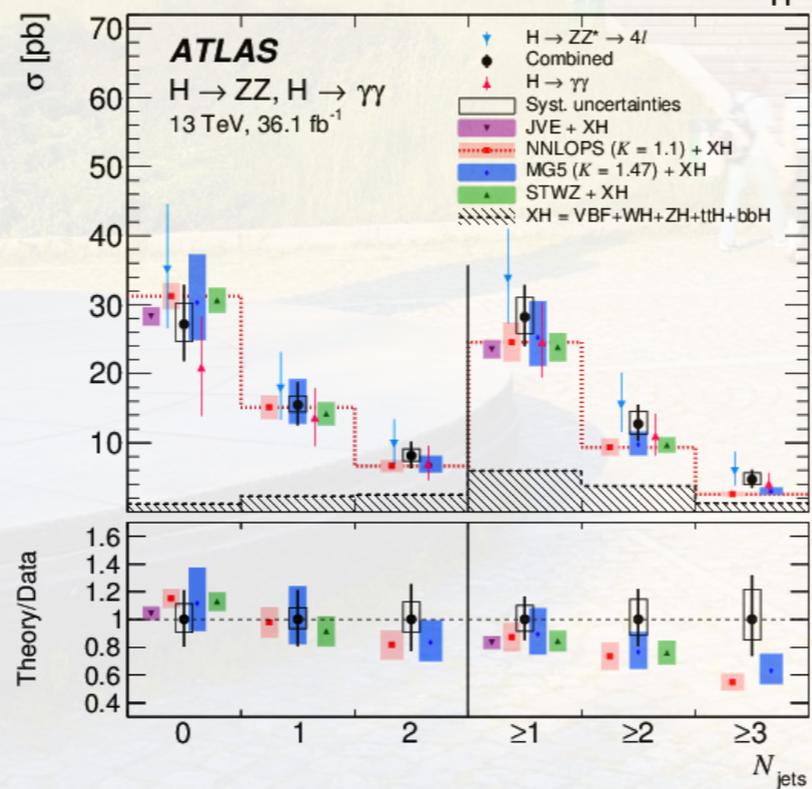
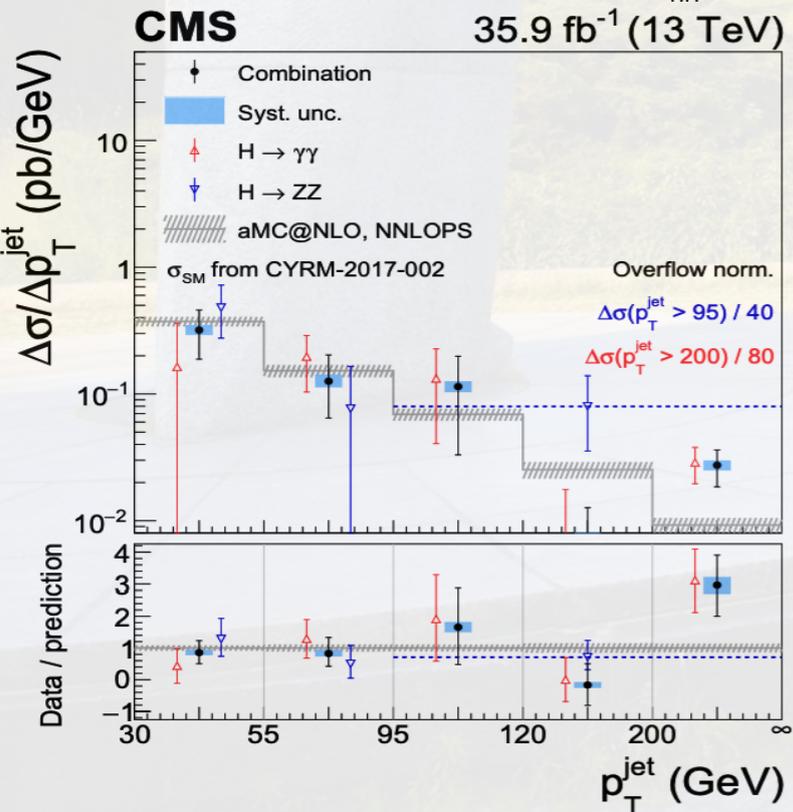
(ATLAS 1805.10197, CMS 1812.06504, EPS2019)

➤ Breakdown in production channels through Simplified Template Cross Section (STXS)

➤ All Higgs production and decay channels contribute

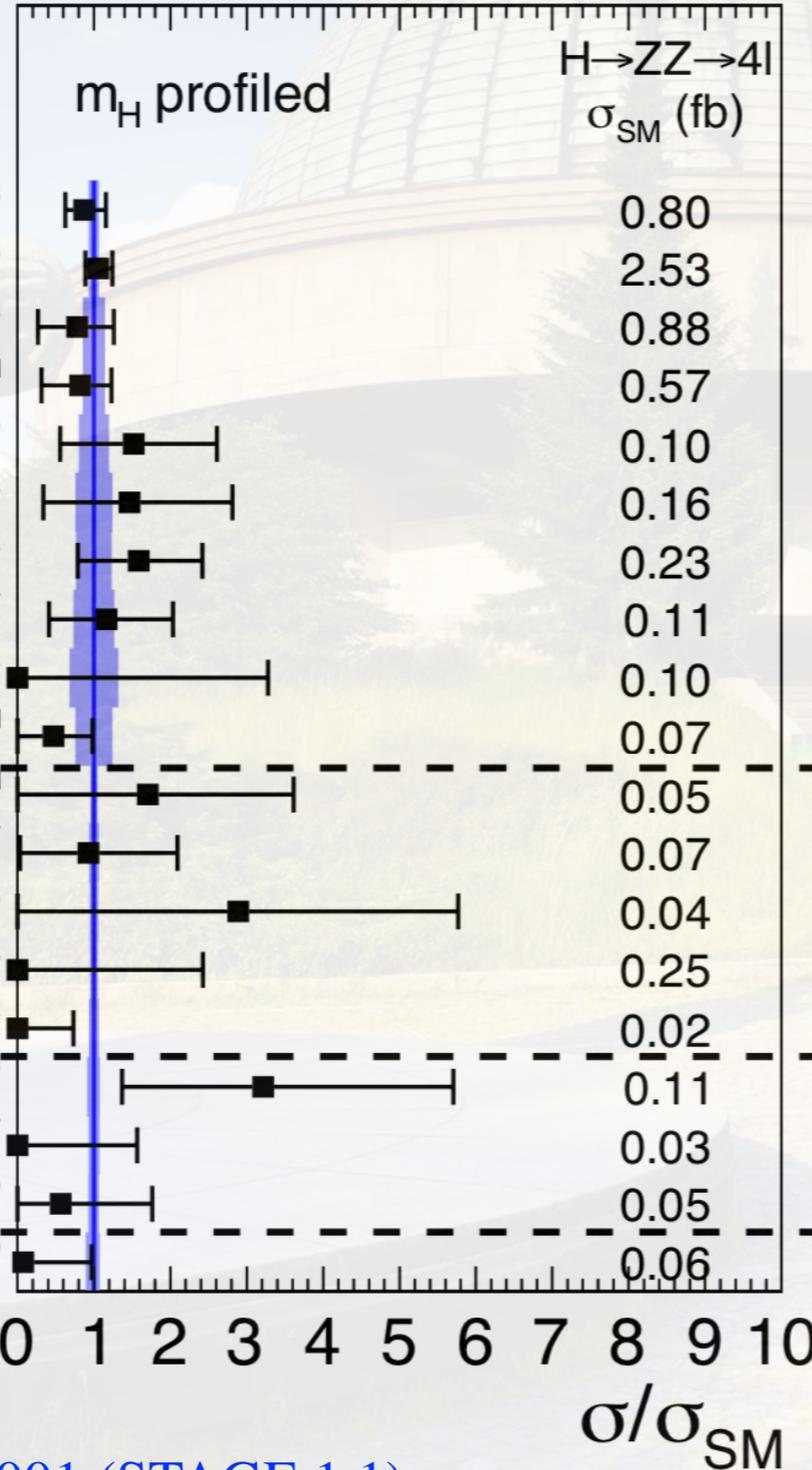
➤ Complexity increase from Stage

$0 \rightarrow 1 \rightarrow 1.1 \rightarrow \dots$



SUCCESS OF LHC HIGGS EXPERIMENTS

CMS Preliminary 137.1 fb⁻¹ (13 TeV)



ggH

VBF

VH

ttH

➤ Typical differential observables for Higgs (+jet) are:

$$\frac{d\sigma}{dp_T^H} \quad \frac{d\sigma}{d|y^H|} \quad \frac{d\sigma}{dp_T^{j1}} \quad \frac{d\sigma}{dN_{jets}}$$

➤ Inclusive decay observables are reconstructed from individual decay channel

➤ Combined results with $\pm 30-50\%$ uncertainties (ATLAS 1805.10197, CMS 1812.06504, EPS2019)

➤ Breakdown in production channels through Simplified Template Cross Section (STXS)

➤ All Higgs production and decay channels contribute

➤ Complexity increase from Stage

0 → 1 → 1.1 → ...

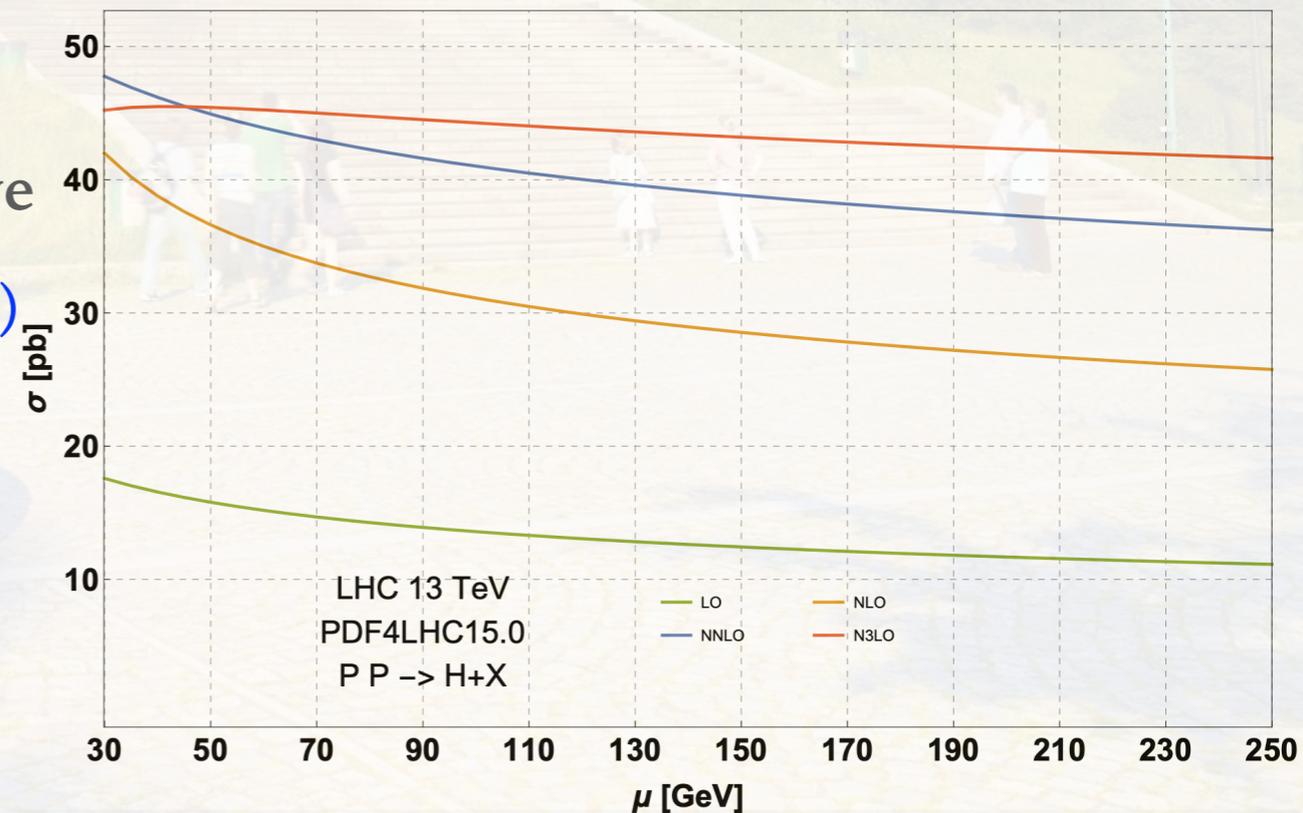
CMS-PAS-HIG-19-001 (STAGE 1.1)

SUCCESS OF HIGGS THEORY (GLUON FUSION)

$\sigma_{PP \rightarrow H+X}$	=	16.00 pb	(+32.87%)	LO, rEFT
	+	20.84 pb	(+42.82%)	NLO, rEFT
	+	9.56 pb	(+19.64%)	NNLO, rEFT
	+	1.62 pb	(+3.32%)	N ³ LO, rEFT
	-	2.07 pb	(-4.25%)	(t,b,c) corr. to exact NLO
	+	0.34 pb	(+0.70%)	1/ m_t corr. to NNLO
	+	2.37 pb	(+4.87%)	EWK corr.
	=	48.67 pb.		

$\delta(\text{theory})$	=	+0.13pb	(+0.28%)	$\delta(\text{scale})$
		-1.20pb	(-2.50%)	
	+	$\pm 0.56pb$	($\pm 1.16\%$)	$\delta(\text{PDF-TH})$
	+	$\pm 0.49pb$	($\pm 1.00\%$)	$\delta(\text{EWK})$
	+	$\pm 0.41pb$	($\pm 0.85\%$)	$\delta(\text{t,b,c})$
	+	$\pm 0.49pb$	($\pm 1.00\%$)	$\delta(1/m_t)$
	=	+2.08pb	(+4.28%)	
		-3.16pb	(-6.5%)	
$\delta(\text{PDF})$	=	$\pm 0.89pb$	($\pm 1.85\%$)	
$\delta(\alpha_s)$	=	+1.25pb	(+2.59%)	
		-1.26pb	(-2.62%)	

- Total cross section with N3LO QCD corrections in heavy top limit (HTL) ([B. Mistlberger 1802.00833](#))
- QCD scale variation reduced significantly
- Public in iHixs2 code ([Dulat et al. 1802.00827](#))
- Uncertainty dominant by QCD ($\pm 4\%$) ([C. Anastasiou et al. 1602.00695](#))
- Three **short boards**: QCD scale, PDF, α_s

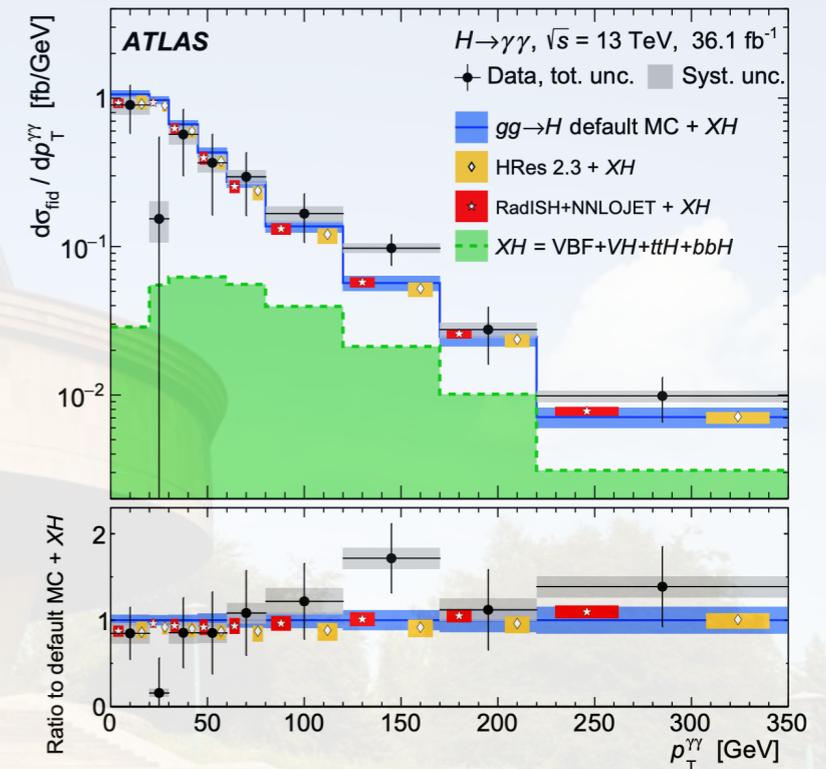


Need to attack on many fronts to further improve

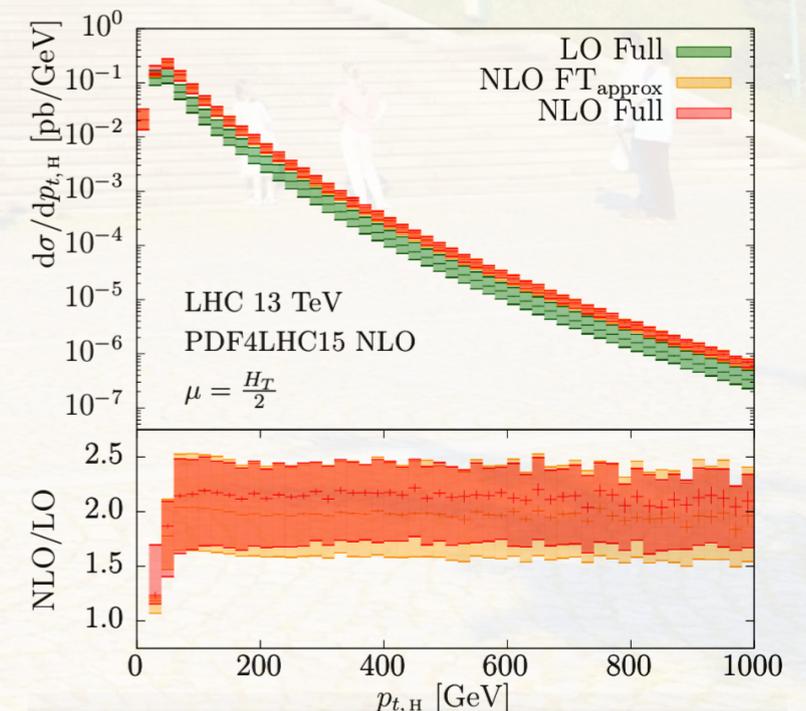
- Towards N3LO PDFs ([Britzger et al. 1906.05303](#))
- Top quark mass dependence ([Davies, Gröber, Maier et al. 1906.00982](#))
- Bottom quark fusion at N3LO ([Duhr, Dulat, Mistlberger 1904.09990](#))
- EWK corrections ([1801.10403](#), [1811.11211](#)) ...

SUCCESS OF HIGGS THEORY (GLUON FUSION)

- Differential predictions advance to new revolution
 - HpT (HTL) at **NNLO+N3LL accuracy** (details later)
 - Robust NNLO calculation at small pT
 - Resummation in two factorisation schemes
 - yH (HTL) at **N3LO accuracy** (details later)
 - Two methods with approximation in good agreement
 - New revolution to differential N3LO accuracy
 - H+J (full SM) at **NLO accuracy** (boosted pT region)
 - Still many aspects to improve:
 - Very time consuming at small pT ($\sim 7M$ CPU h)
 - Application with decay fiducial cuts
 - Join with parton shower beyond LO



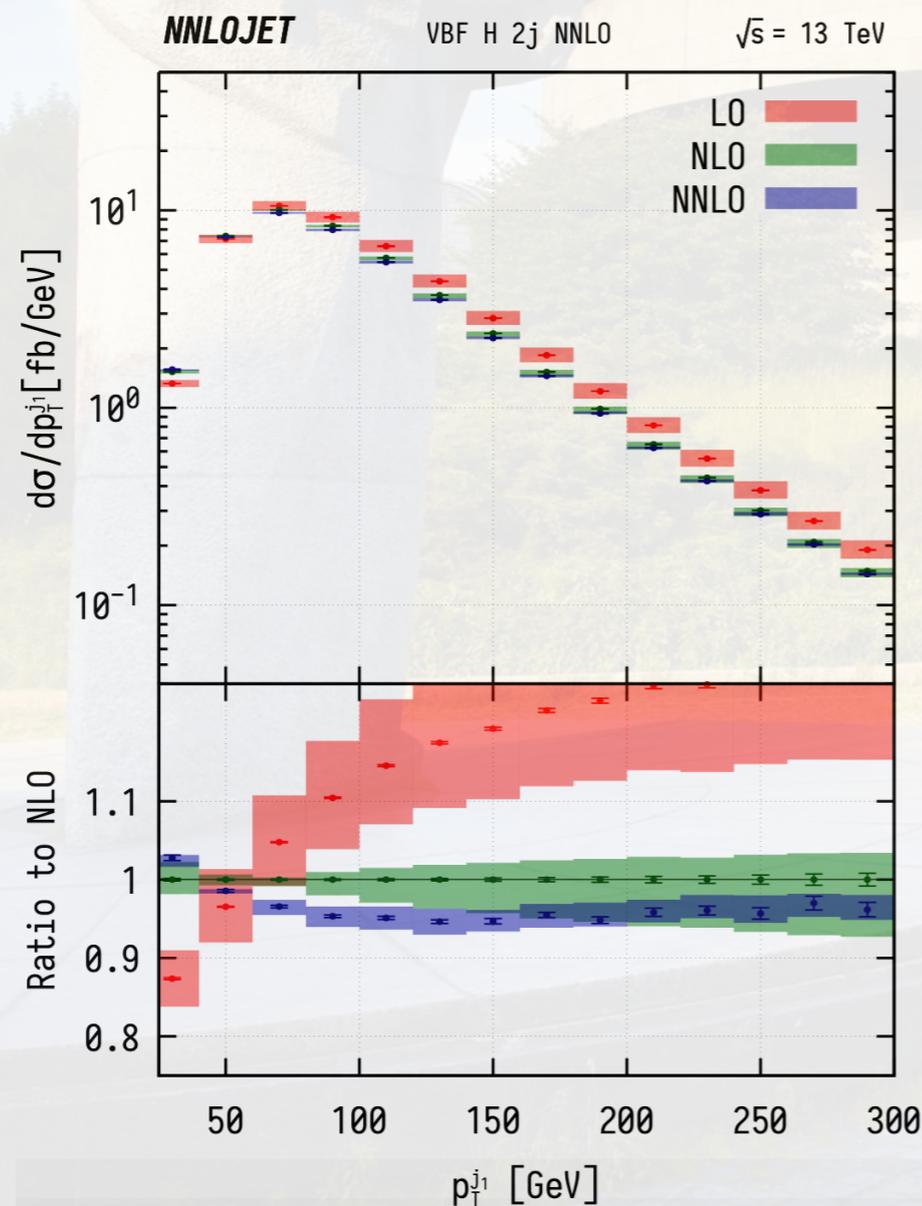
ATLAS 1802.04146



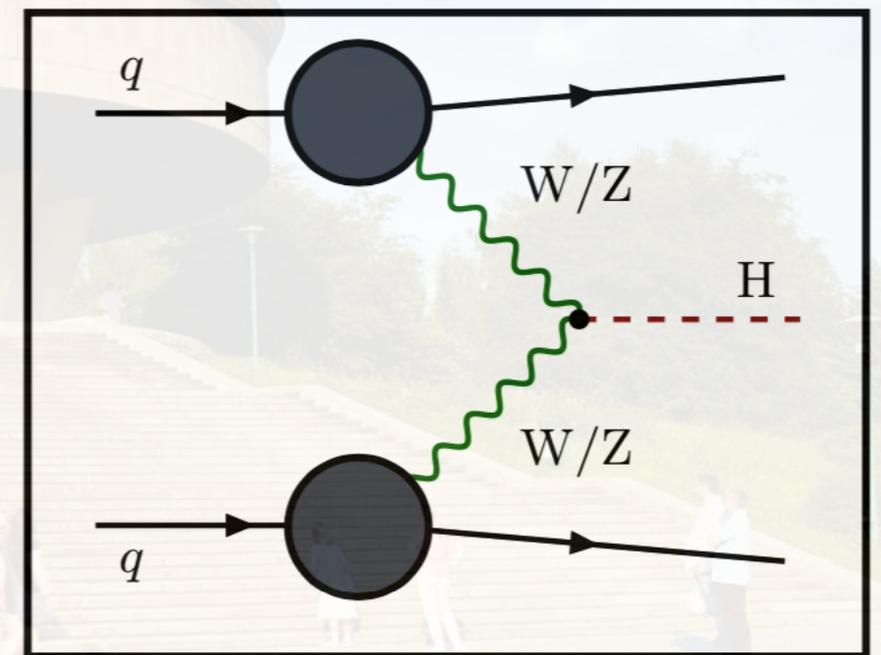
Jones et al. 1802.00349

SUCCESS OF HIGGS THEORY (VECTOR BOSON FUSION)

- Differential NNLO corrections to VBF-2J production and NLO corrections to VBF-3J production using **structure function approach** (Cruz-Martinez et al. 1802.02445)
- Uncovered error in earlier NNLO calculation stemming from VBF-3J piece (now fixed) (Cacciari, Dreyer et al. 1506.02660) (Jager, Schissler et al. 1405.6950)



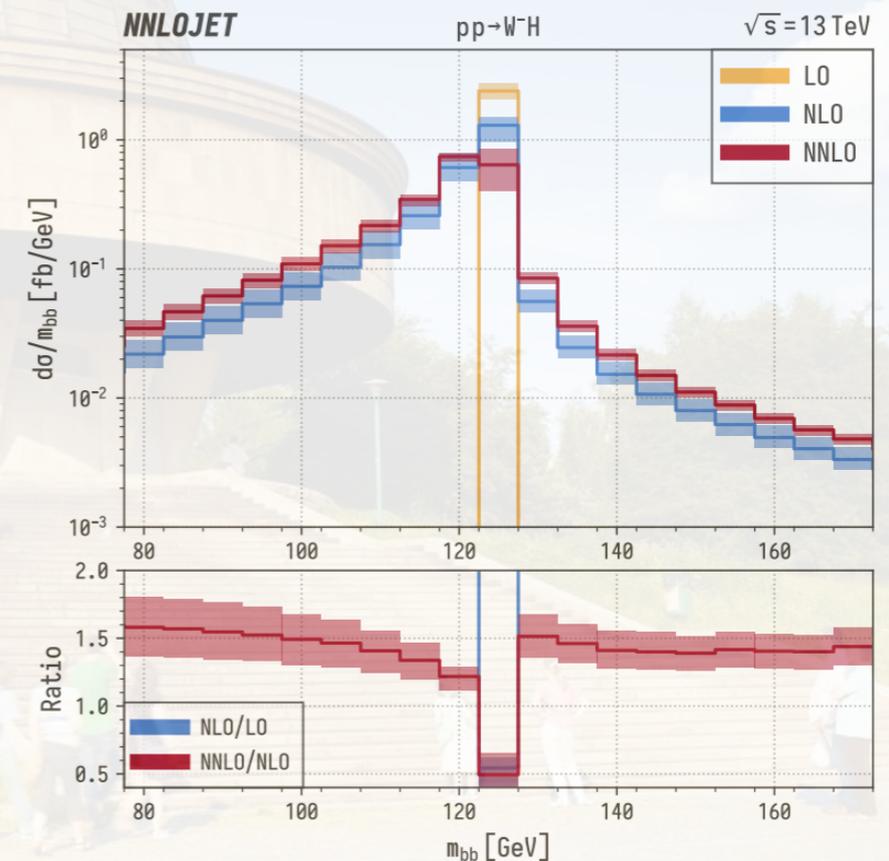
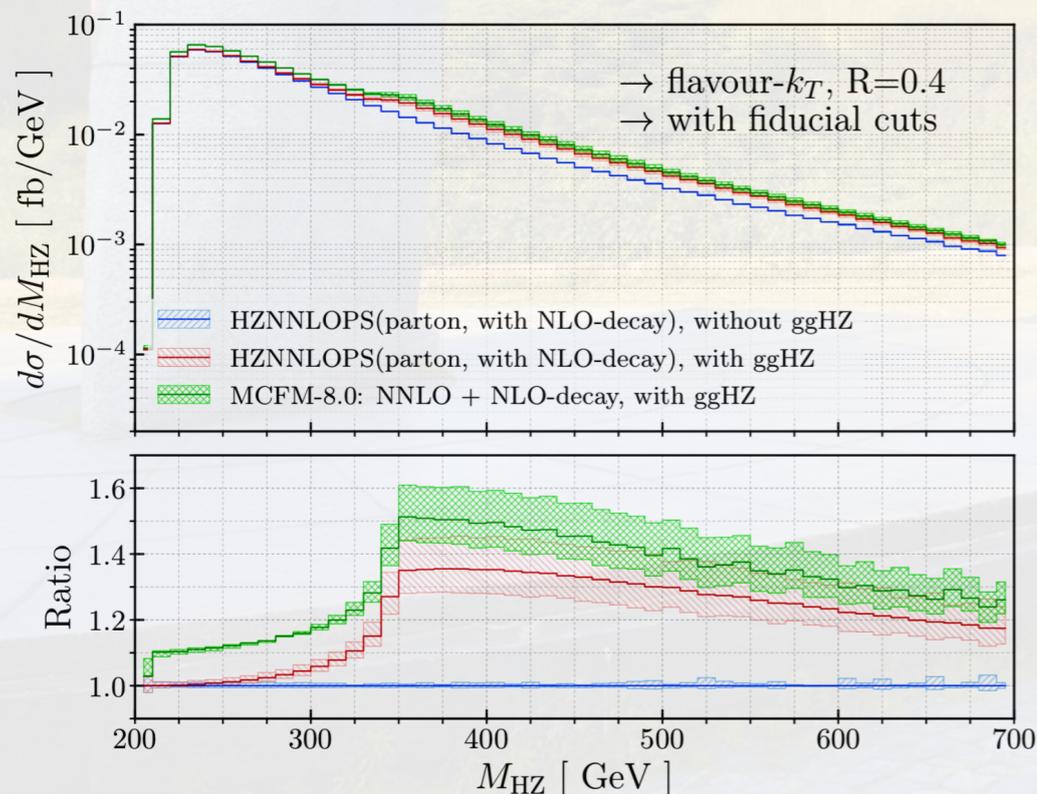
$DIS \otimes DIS$



- NNLO cross section is **4%** smaller than NLO (VBF cuts)
- Scale variation now reduced to $\pm 3\%$
- Contribute significantly at boosted Higgs $p_T \sim 20\%$
- Large overlap in fiducial volume with gluon fusion H+2J
- Inclusive cross section at N3LO (Dreyer et al. 1606.00840)

SUCCESS OF HIGGS THEORY (VH)

- Current precision with NNLO QCD corrections in both production and decay to process $pp \rightarrow W(l\nu) + H(b\bar{b})$ with narrow width approximation and massless b quark (Ferrera et al. 1705.10304), (Caola et al. 1712.06954), (Gauld, Majer et al. 1907.05836)
- NNLO corrects NLO $H \rightarrow b\bar{b}$ decay in both below and above Higgs mass threshold regions
- New **interference** at NNLO from $H \rightarrow gg$
- N3LO $H \rightarrow b\bar{b}$ decay now available (Mondini, Schiavi, Williams 1904.08960)
- Future work with b mass and EXP flavour kT jet



Gauld, Majer et al. 1907.05836

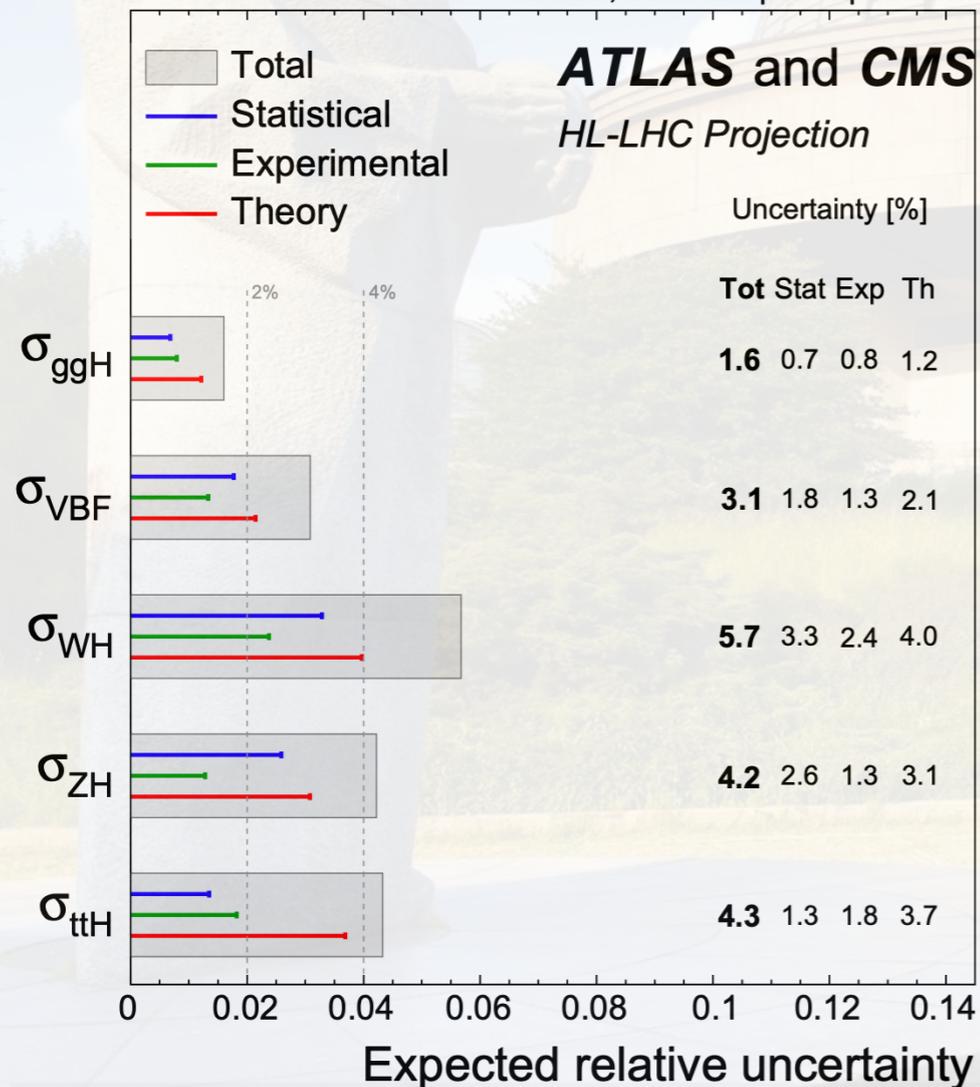
- NNLOPS accurate $pp \rightarrow Z(l^+l^-) + H(b\bar{b})$ (Astill, Bizoń et al. 1804.08141)
- Sizeable impact of loop induced $gg \rightarrow Z(l^+l^-) + H(b\bar{b})$ above top mass threshold
- NLO corrections includes **interference** with qg and $q\bar{q}$ channels (need two-loop massive top for through study)

CHALLENGE FROM HL-LHC PROJECTION (20 YEARS)

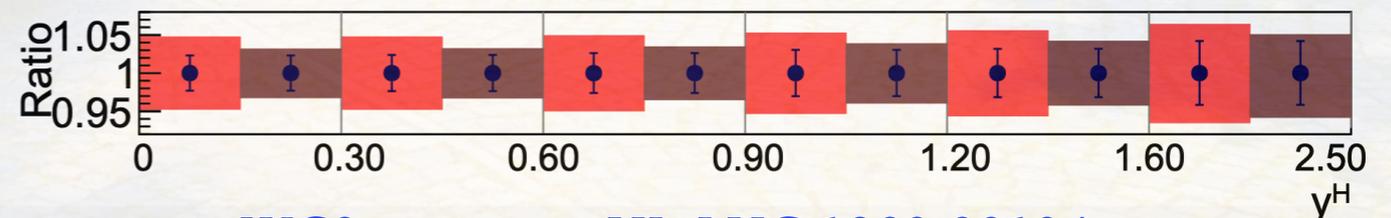
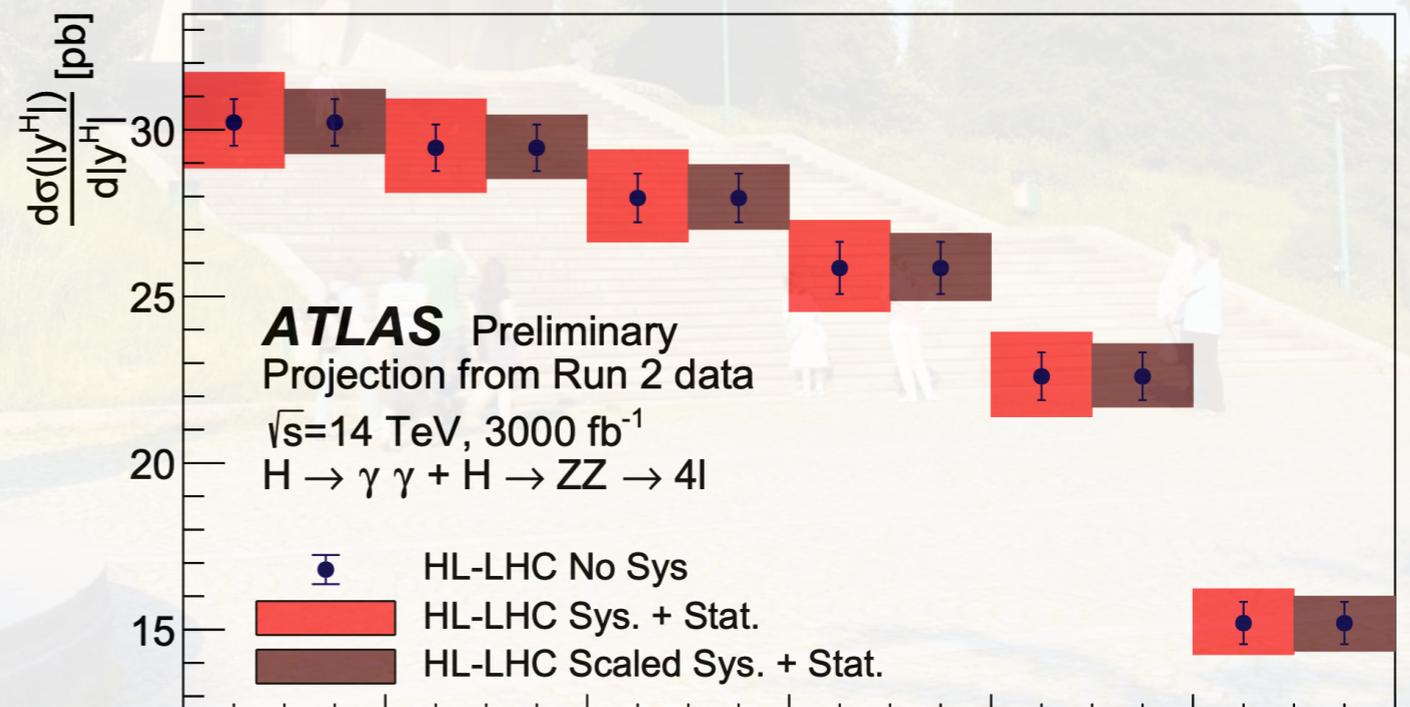
➤ Is it precise enough? **Not yet** according to HL-LHC Projections!

➤ Theory complexity scales up exponentially, EXP error scales down by $1/\sqrt{\mathcal{L}}$

$\sqrt{s} = 14 \text{ TeV}, 3000 \text{ fb}^{-1}$ per experiment



- Differential observables (S2) HL-LHC projections: $y^H \pm 3\%$ $H_pT \pm 5\%$ (more details in this talk)
- Theory need consistent upgrade to reduce PDF and α_s uncertainties

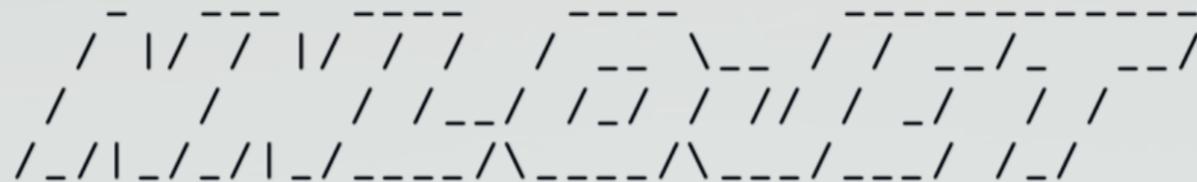


➤ HL-LHC expects $\pm 1.6\%$ in two decades

➤ Current N3LO has $\pm 4\%$ for QCD alone!

[WG2 report on HL-LHC 1902.00134](#)

[WG2 report on HL-LHC 1902.00134](#)



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* NNLOJET: A multiprocess parton level event generator at O(alpha_s^3)*
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X. Chen, J. Cruz-Martinez, J. Currie, R. Gauld, A. Gehrmann-De Ridder, T. Gehrmann, E.W.N. Glover, M. Höfer, A. Huss, I. Majer, J. Mo, T. Morgan, J. Niehues, J. Pires, R. Schürmann, D. Walker, J. Whitehead

LHC Higgs Production channels		
$H + J$ (ggF) NNLO HTL \otimes LO SM		1408.5325, 1607,08817, 1805.00736, 1805.05916
H (ggF) N3LO HTL (approx.)		1807.11501
$H + JJ$ (VBF) NNLO		1802.02445
$H + V$ (VH) NNLO		1907.05836

Higgs Decay channels		
$b\bar{b}$	NNLO	b-tagging
$WW^* \rightarrow 2l2\nu$	LO	Lepton isolation
$\tau^+\tau^-$	LO	Massive final states
$ZZ^* \rightarrow 4l$	LO	Lepton isolation
$\gamma\gamma$	LO	Photon isolation
$Z(\rightarrow 2l)\gamma$	LO	Photon + lepton iso.

- Parton level event generator with NNLO antenna subtraction method
- **NNLOJET** provides many cutting-edge predictions of the Higgs boson phenomenology.
- ggF and VH channels are linked with limited decay channels.
- Identification of EW and QCD final states using EXP algorithms.



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$H + V$ (VH) NNLO	1907.05836	$ZZ^* \rightarrow 4l$	LO Lepton isolation
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- Parton level event generator with NNLO antenna subtraction method
- **NNLOJET** provides many cutting-edge predictions of the Higgs boson phenomenology.
- ggF, VBF and VH channels are linked with various decay channels.
- Identification of EW and QCD final states using EXP algorithms.

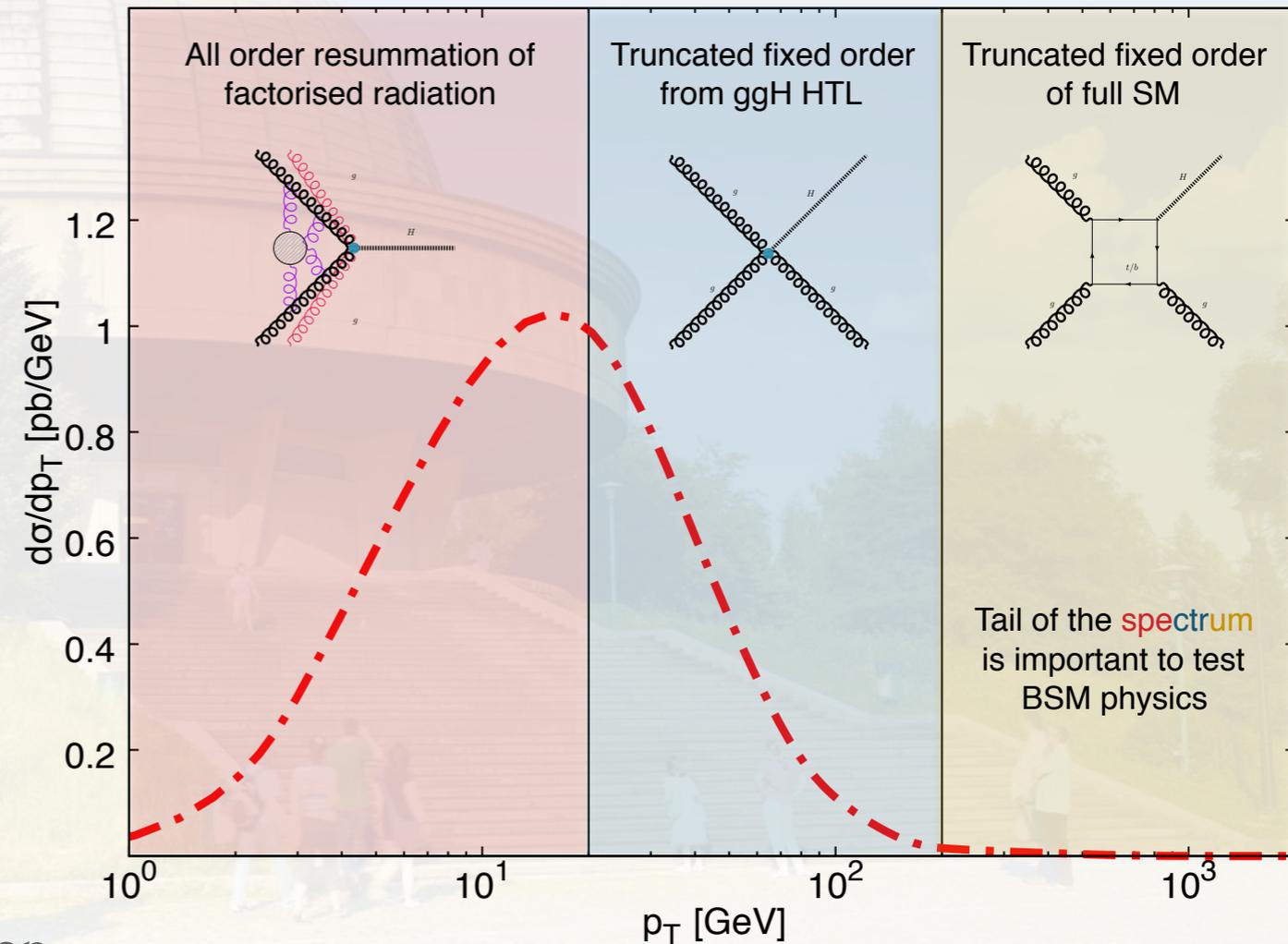


HIGGS TRANSVERSE MOMENTUM DISTRIBUTION IN FULL SPECTRUM

HIGGS TRANSVERSE MOMENTUM SPECTRUM

- Higgs p_T **spectrum** tests SM in various aspects
- **Small p_T region** (< 20 GeV):
 - Singular log terms spoil any reliable fixed order predictions $\ln^k(m_H^2/p_T^2)/p_T^2$
 - Resummation of log terms and match to fixed order: $d\sigma^{FO} \ominus d\sigma^S \oplus d\sigma^R$
- **Medium p_T region** ($20 \sim 200$ GeV):
 - Reliable with heavy top limit (HTL)
 - Current best precision is H+J NNLO HTL
- **Boosted p_T region** (> 200 GeV)
 - Energy scale resolve mass effect of quark loop
 - Best ggF precision is H+J at NLO SM
 - VBF, VH and ttH channels equally important
- Many other effects involved: top-bottom interference, heavy quark Yukawa couplings, resummation of logs involving quark mass etc.

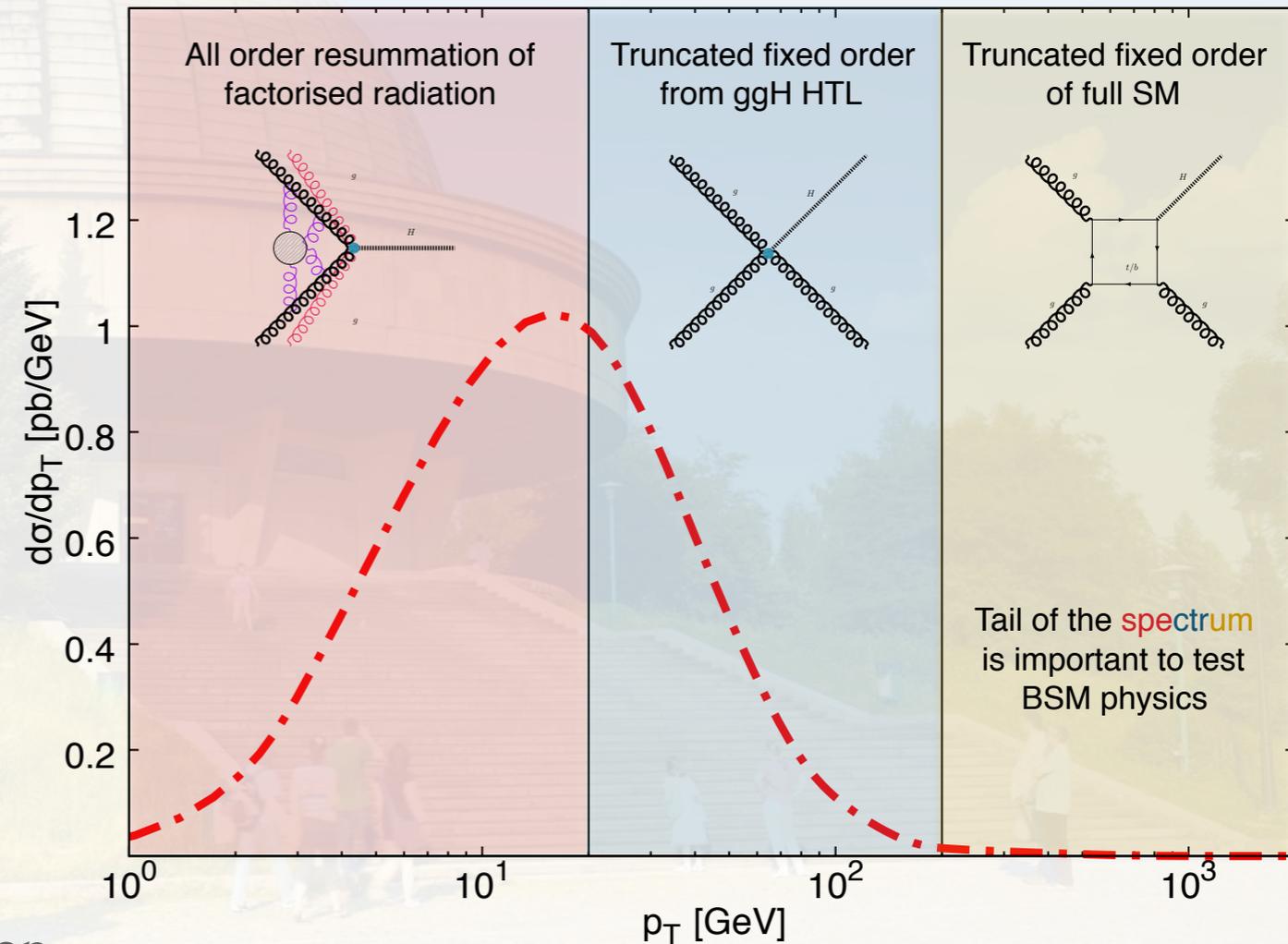
Higgs p_T Spectrum from Gluon Fusion at the LHC



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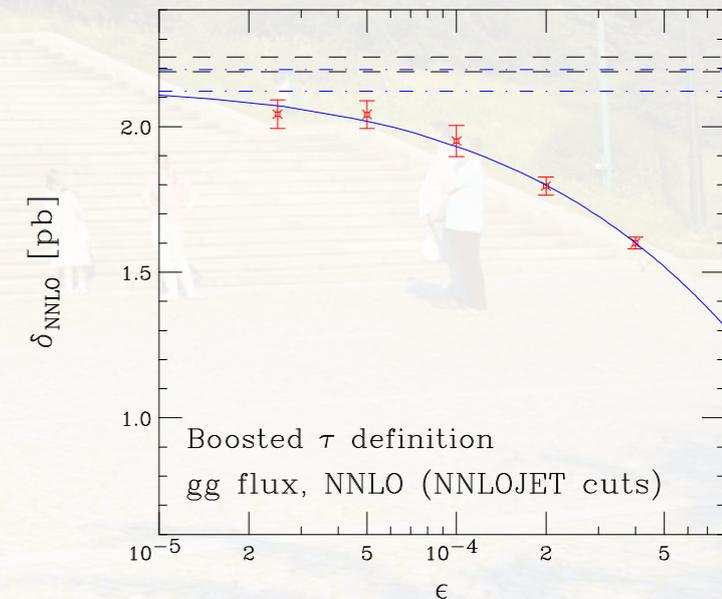
Will separately discuss each $H p_T$ region for the rest of this talk

HIGGS TRANSVERSE MOMENTUM AT MEDIUM PT

- H+J Computed at NNLO QCD (HTL) by 4 groups using 3 methods
 - Antenna subtraction (NNLOJET) [XC, Gehrmann, Glover et al. \(1408.5325, 1607.08817\)](#)
 - Sector improved subtraction (STRIPPER) [Boughezal, Caola et al. \(1302.6216, 1504.07922\)](#)
 - N-Jettiness (BFGLP and MCFM) [Boughezal, Focke et al. \(1505.03893\)](#) [Campbell et al. \(1906.01020\)](#)
- It was the **battle ground for the first** LHC process with single jet + colourless @ NNLO
- Long-standing discrepancy between N-Jettiness and other methods

	$\sigma_{H(\rightarrow\gamma\gamma)+\geq 1jet, NNLO}^{EFT}$	$\sigma_{H+\geq 1jet, NNLO}^{EFT}$	$\sigma_{H+\geq 1jet, NNLO}^{EFT}$
NNLOJET	$9.44^{+0.59}_{-0.85}$ fb	$16.8^{+0.9}_{-1.5}$ pb	$5.81^{+0.51}_{-0.62}$ pb
STRIPPER	$9.45^{+0.58}_{-0.82}$ fb	-	-
STRIPPER	-	$16.7^{+1.0}_{-}$ pb	-
BFGLP	-	-	$5.5^{+0.3}_{-0.4}$ pb

[XC, Gehrmann, Glover et al. \(1408.5325, 1607.08817\)](#)



- Finally resolved with MCFM revisit study in this year

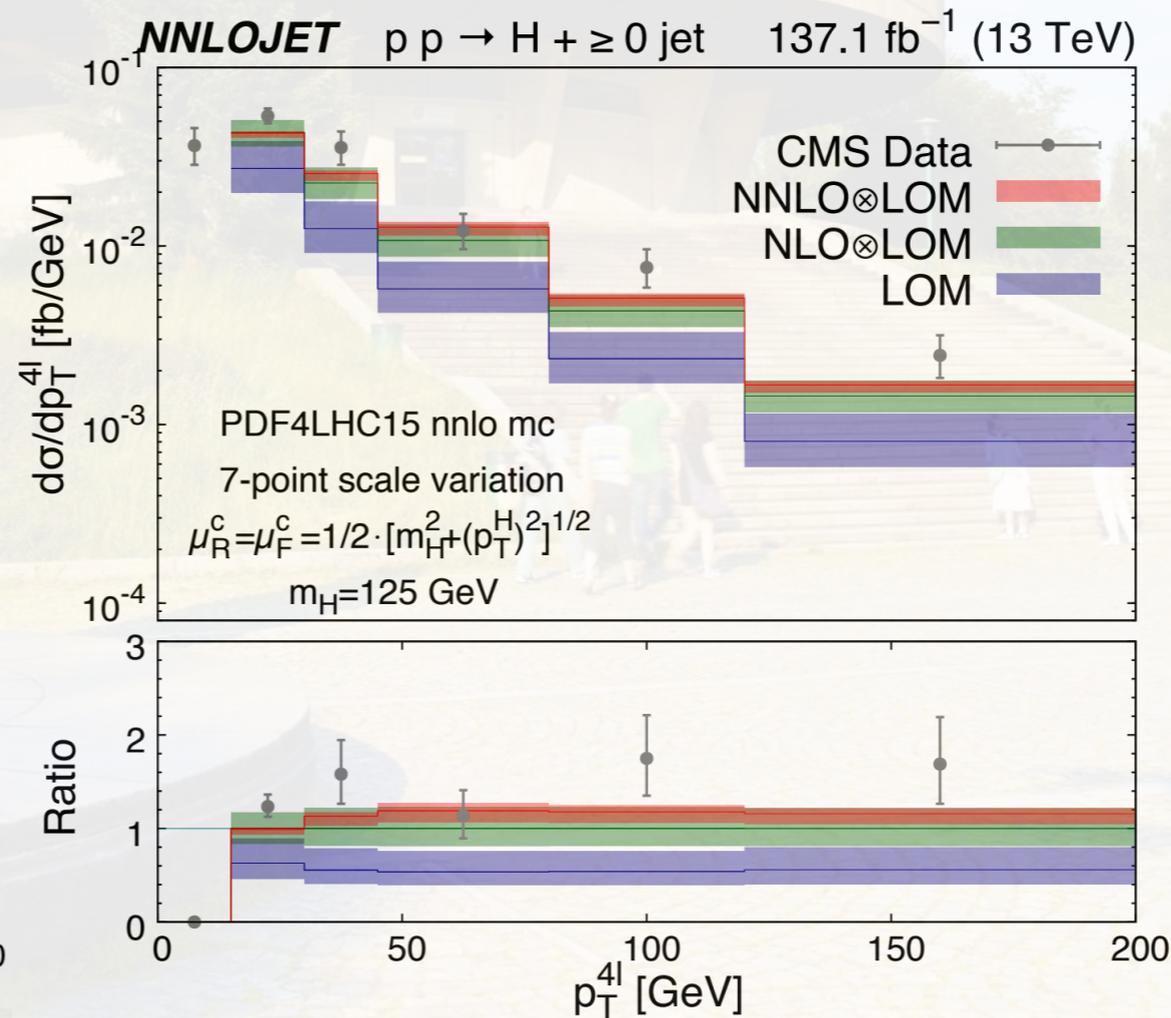
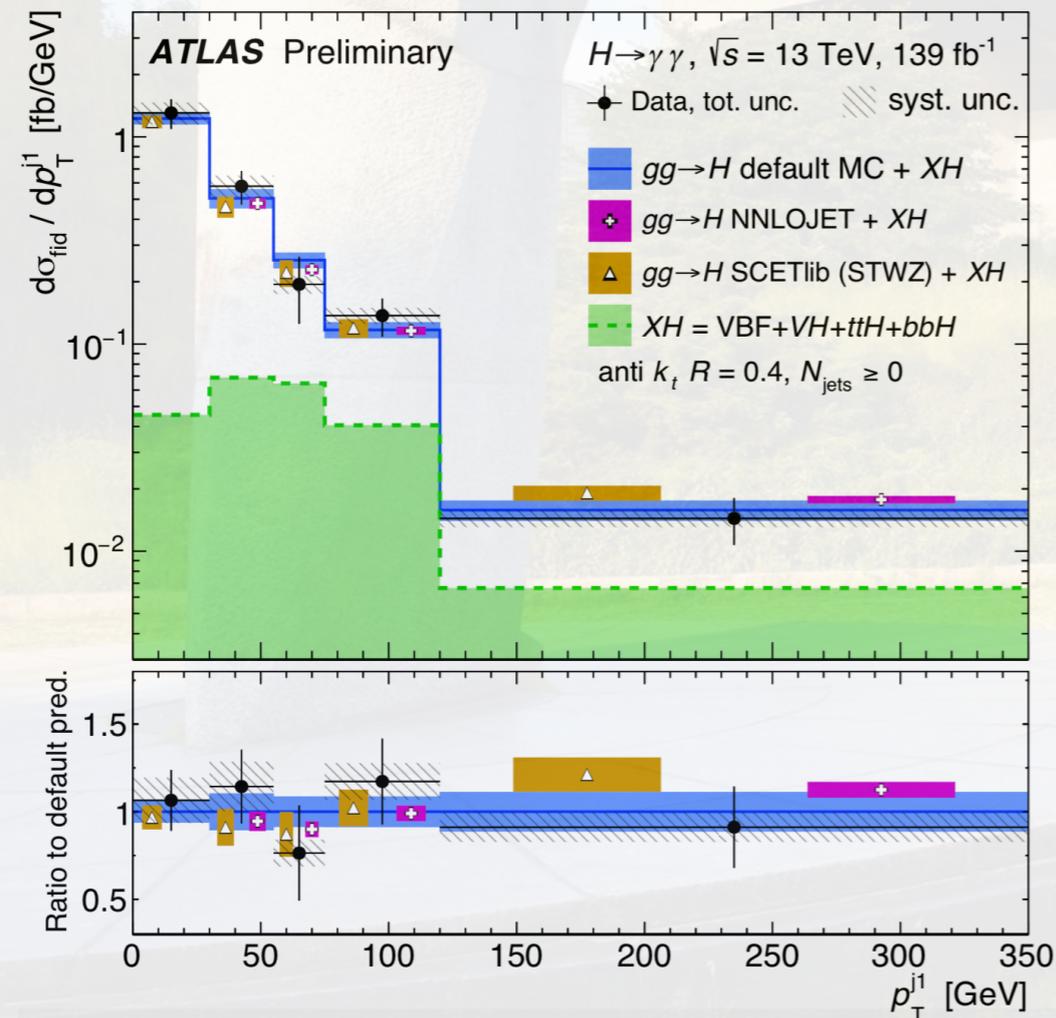
- Jettiness cut **20 times smaller** than in BFGLP
- extrapolate to zero (**~5% @ NNLO**)
- Desire sub-leading power correction at NNLO

$$\sigma_{NNLO}(\text{NNLOJET}) = 16.73 \pm 0.05^{+1.00}_{-1.51} \text{ pb}$$

$$\sigma_{NNLO}(\text{MCFM, fit}) = 16.71 \pm 0.05^{+1.03}_{-1.52} \text{ pb}$$

HIGGS TRANSVERSE MOMENTUM AT MEDIUM PT

- Fiducial cross section for H+J now known at NNLO QCD for:
 - $H \rightarrow \gamma\gamma$ Caola, Melnikov, Schulze (1508.02684), XC, Gehrmann, Glover et al. (1607.08817)
 - $H \rightarrow WW^* \rightarrow 2l2\nu$ Caola, Melnikov, Schulze (1508.02684)
 - $H \rightarrow ZZ^* \rightarrow 4l$ XC, Gehrmann, Glover, Huss (1905.13738)



Exact EXP fiducial region with:

- Photon isolation
- Lepton isolation
- Jet identification
- Top mass @ LO

Good agreement!

HIGGS TRANSVERSE MOMENTUM AT **SMALL PT**

- FO break down, where is the problem come from?

- Take $d\sigma_{NLO}^H$ as example:

$$A_{2gH}^0(\hat{g}, \hat{g}, H) + A_{3gH}^0(\hat{g}, \hat{g}, g, H) - F_3^0(\hat{g}, g, \hat{g})A_{2gH}^0(\tilde{g}, \tilde{g}, \tilde{H}) + A_{2gH}^1(\hat{g}, \hat{g}, H) + \mathcal{F}_3^0(\hat{g}, \hat{g})A_{2gH}^0(\tilde{g}, \tilde{g}, \tilde{H})$$

↓
 $\delta(p_T^H)$

↓
 p_T^H

↓
 $\delta(p_T^H)$

↓
 $\delta(p_T^H)$

↓
 $\delta(p_T^H)$

- Finite p_T^H region has no IR regulator → fixed order predictions break down
- How to make reliable predictions of $d\sigma/dp_T^H$ at 1 GeV?
- Use QCD factorisation to distinguish radiations from Born kinematics.

$$d\sigma = \sigma_{LO} \otimes H \otimes B \otimes B \otimes S \otimes J$$

- Replace IR subtraction by IR renormalisation (IR poles removed).
- Find and solve RGE of factorised functions to include all order effects.

HIGGS TRANSVERSE MOMENTUM AT **SMALL PT**

- FO break down, where is the problem come from?

- Take $d\sigma_{NLO}^H$ as example:

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↓
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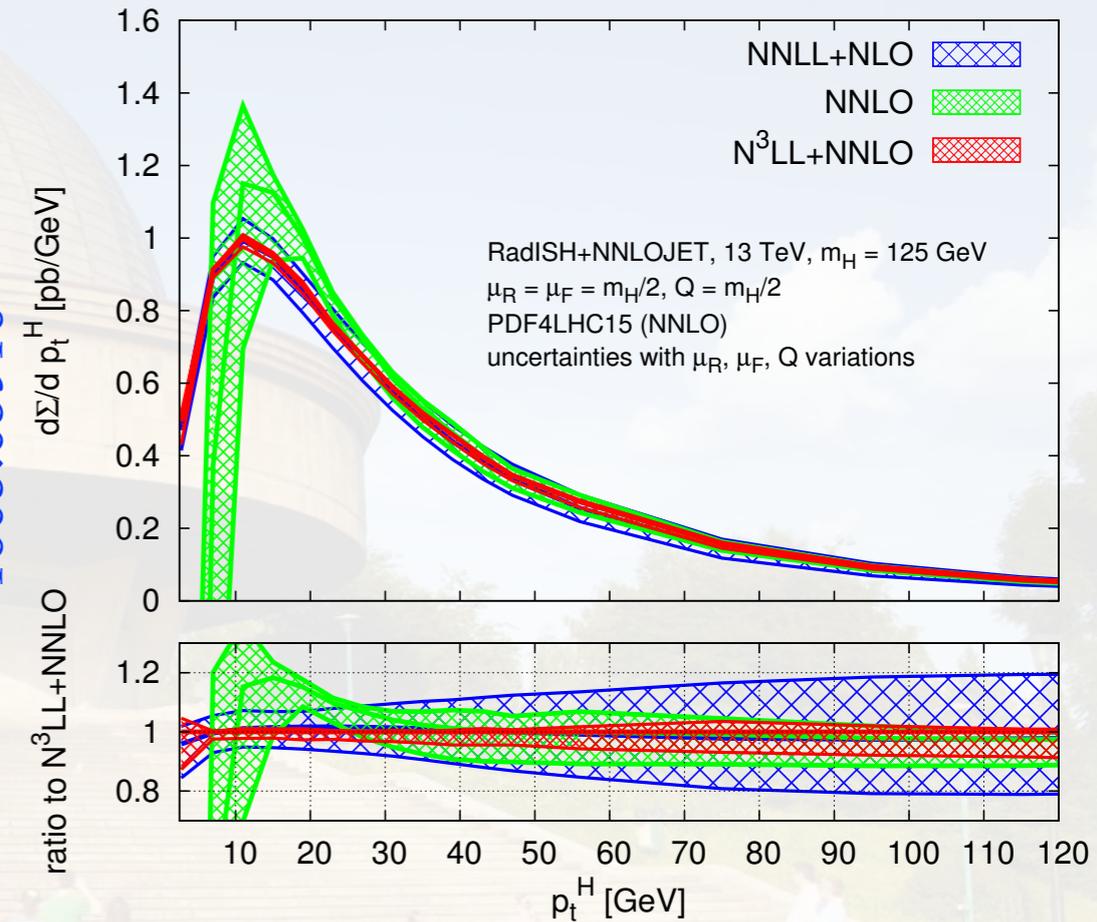
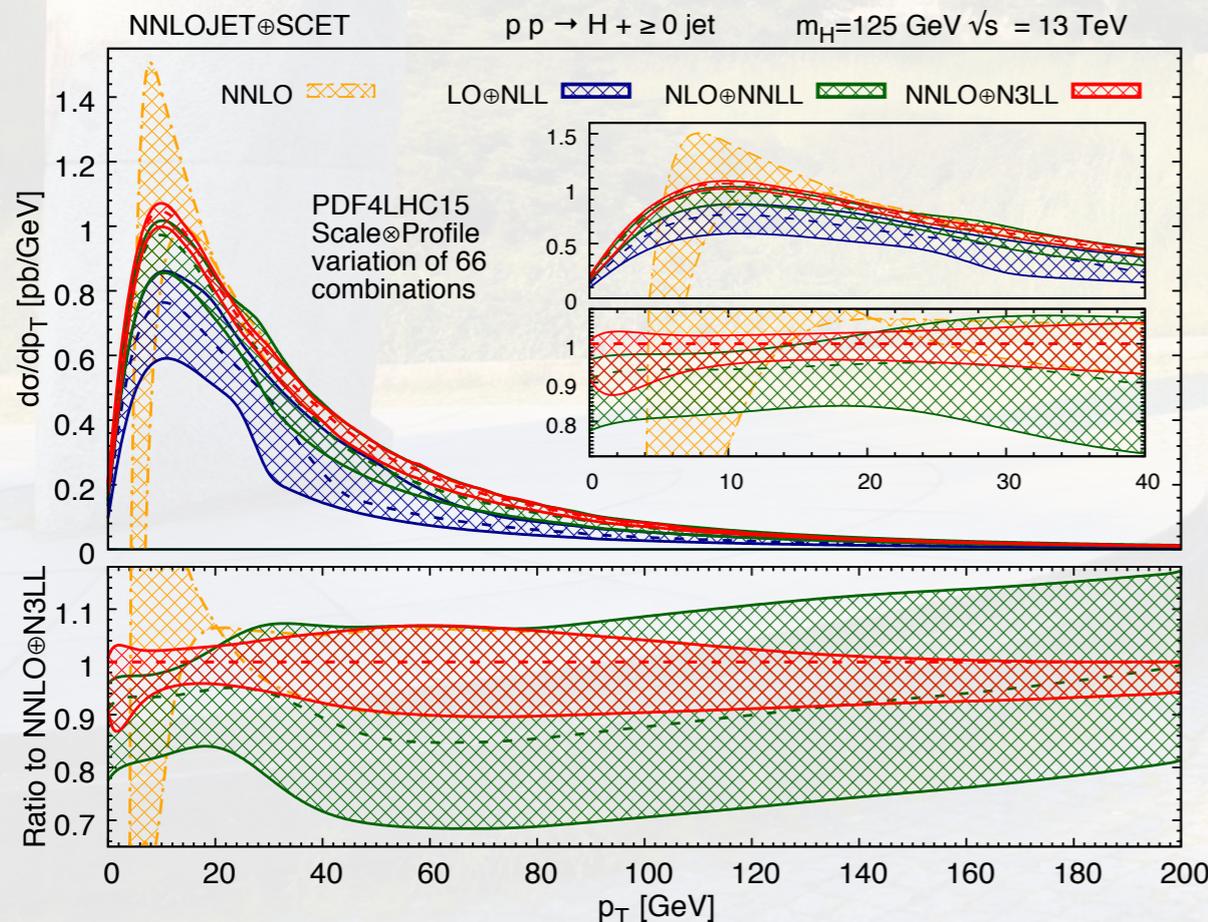
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HIGGS TRANSVERSE MOMENTUM SPECTRUM (SMALL+MEDIUM)

- NNLO + N3LL Resummation with SCET and RadISH
 - RadISH + NNLOJET at N3LL + NNLO
 - Multiplicative matching to NNLO total X.S.
 - Substantial regulation from NNLO+N3LL at the peak of spectrum
 - Scale variation reduced by **60%** from NLO+NNLL to NNLO+N3LL

RadISH+NNLOJET
1805.05916

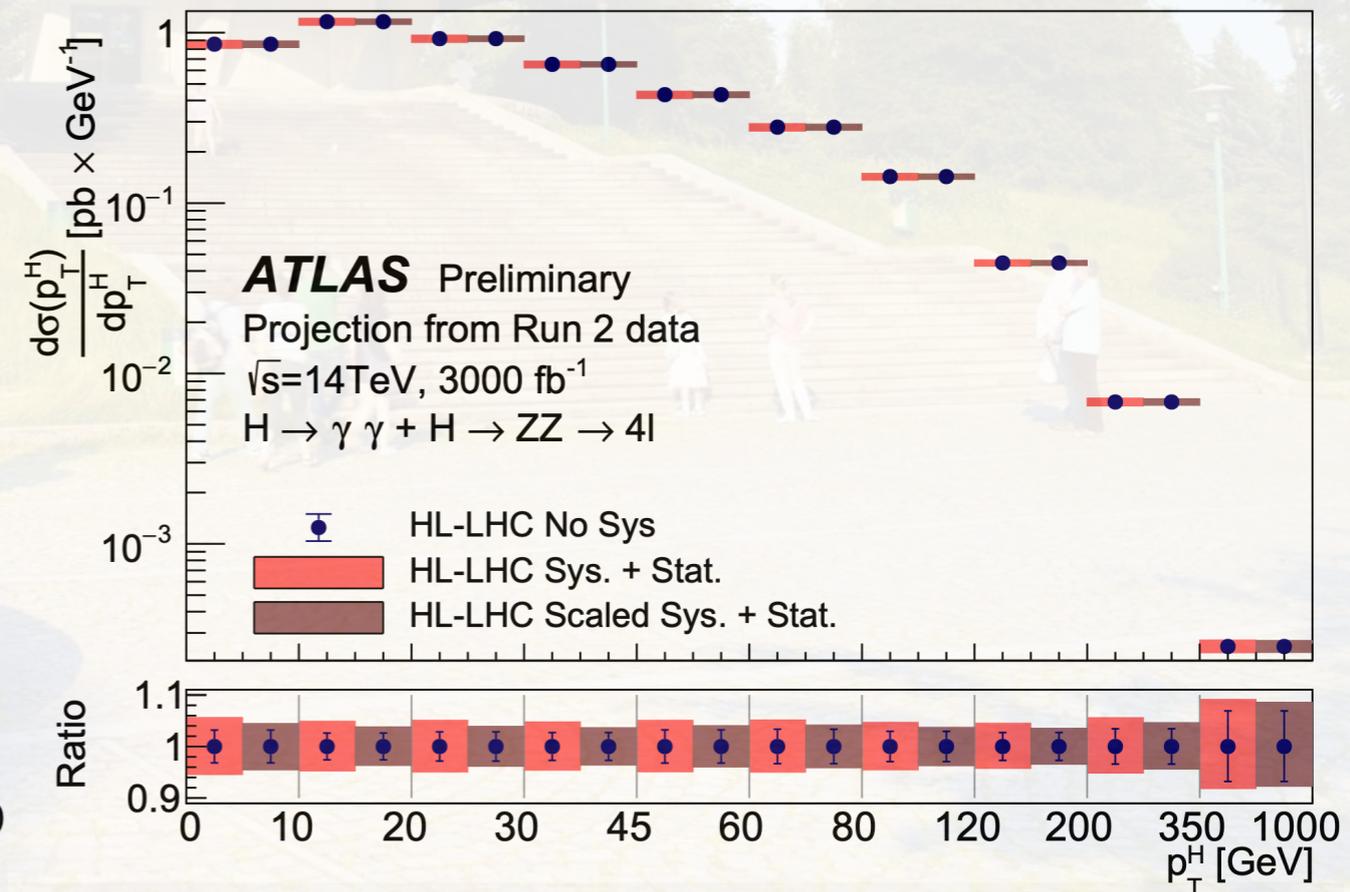
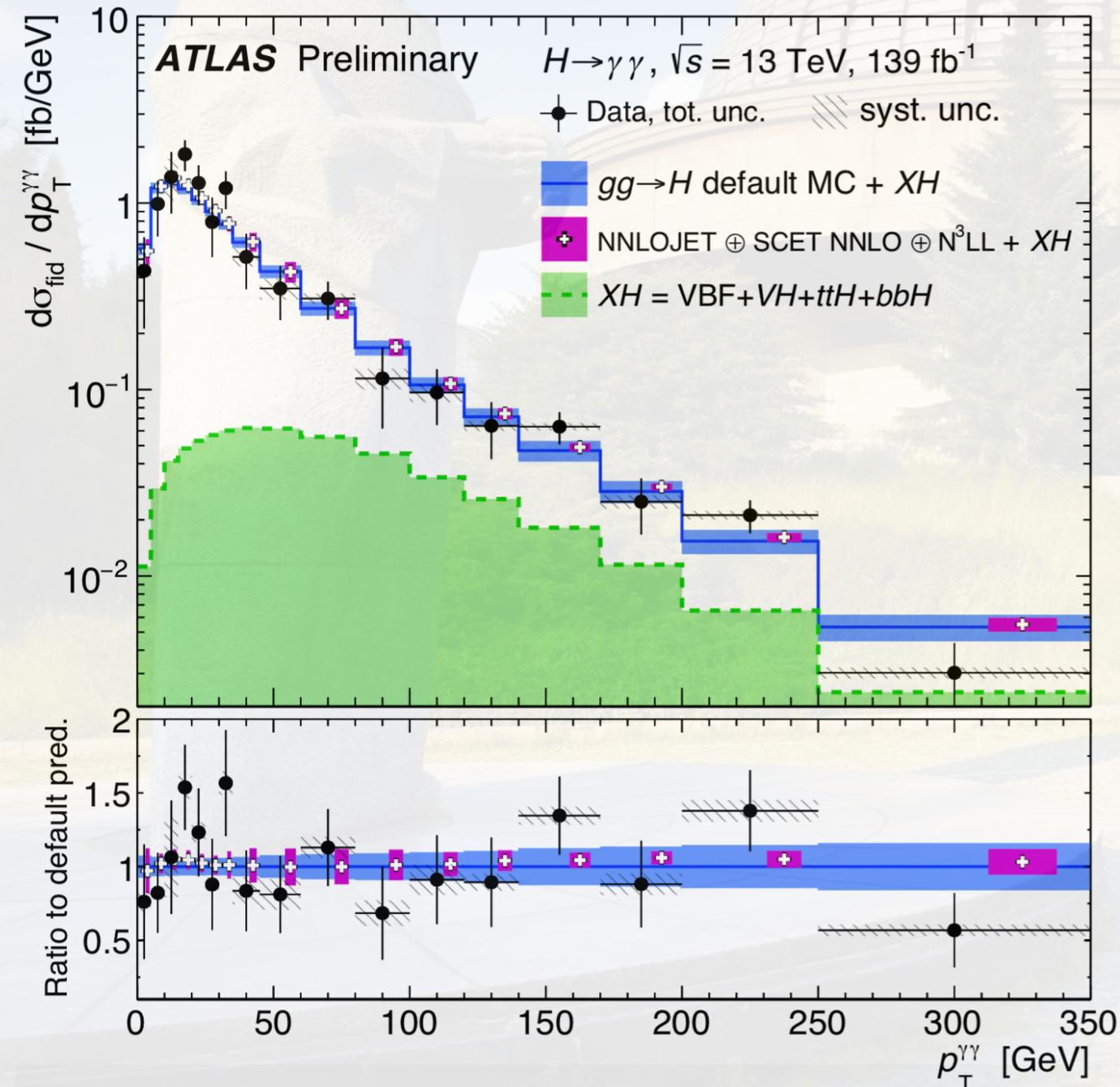


- SCET + NNLOJET at N3LL + NNLO
- Additive matching using profile functions
- Conservative uncertainty estimation involving 11 scale variation choices times 6 profile functions
- Noticeable deviation between NNLO and NNLO+N3LL starting from **30 GeV**
- Future extension to include m_t and m_b effect

HIGGS TRANSVERSE MOMENTUM SPECTRUM (SMALL+MEDIUM)

► Comparison with LHC data and HL-LHC projection

- SCET + NNLOJET at N3LL + NNLO
- Consistent with LHC full Run II data
- EXP uncertainty $\pm 40\%$, TH uncertainty $\pm 8\%$
- Close to HL-LHC projection uncertainty $\pm 5\%$ (S2)



HIGGS TRANSVERSE MOMENTUM AT BOOSTED REGION

➤ Expect HTL approximation fail for $p_T > 200$ GeV

➤ Two approaches to include top mass effects

➤ Expansion valid for $m_H^2, m_t^2 \ll |s| \sim |t| \sim |u|$

Lindert, Kudashkin, et al (1703.03886); Neumann (1802.02981)

➤ Exact results (numerical in SecDec)

Jones, Kerner, Luisoni (1802.00349)

➤ Joint effort in HH: exact numerical+expansion

Davies, Heinrich, Jones, et al. (1907.06408)

➤ Large NLO/LO K-factor ~ 2

➤ K-factor very similar to HTL

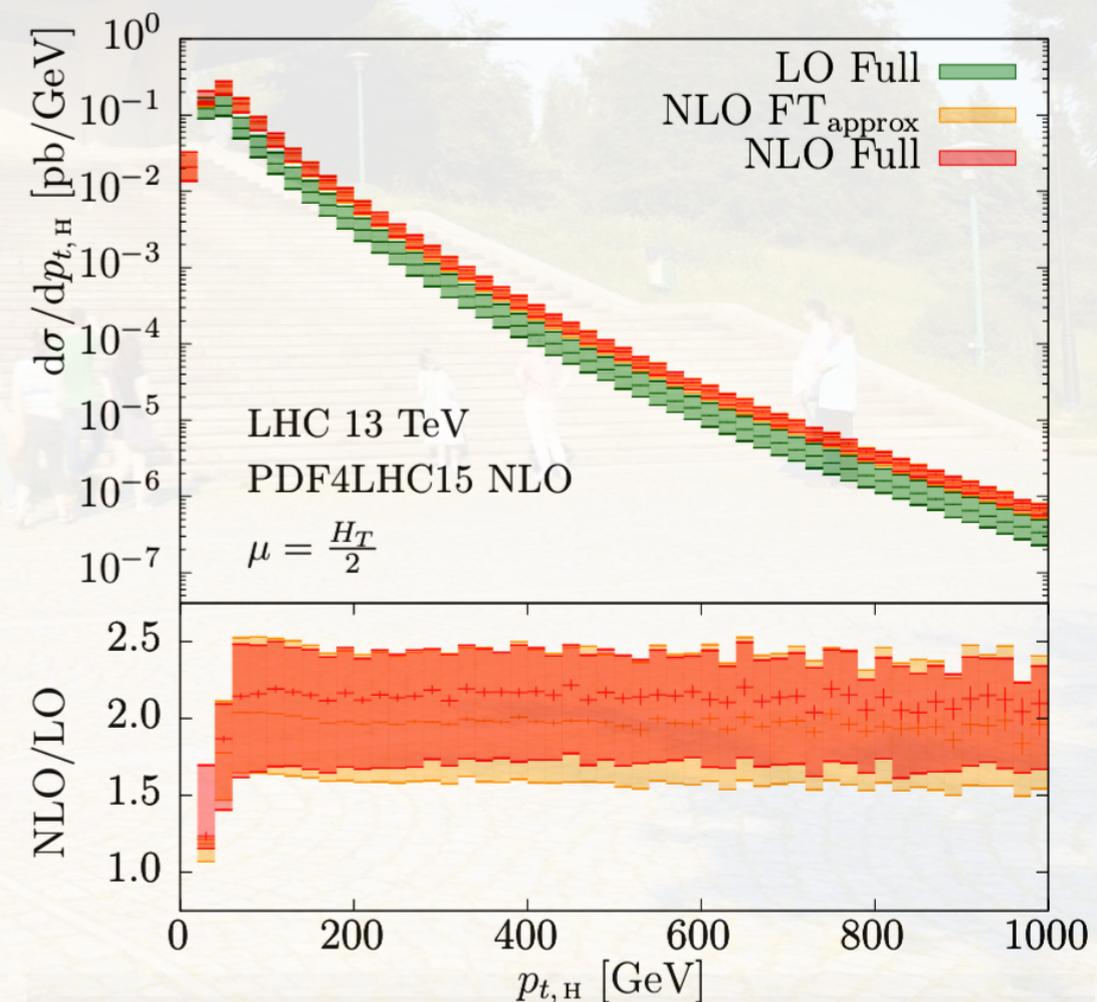
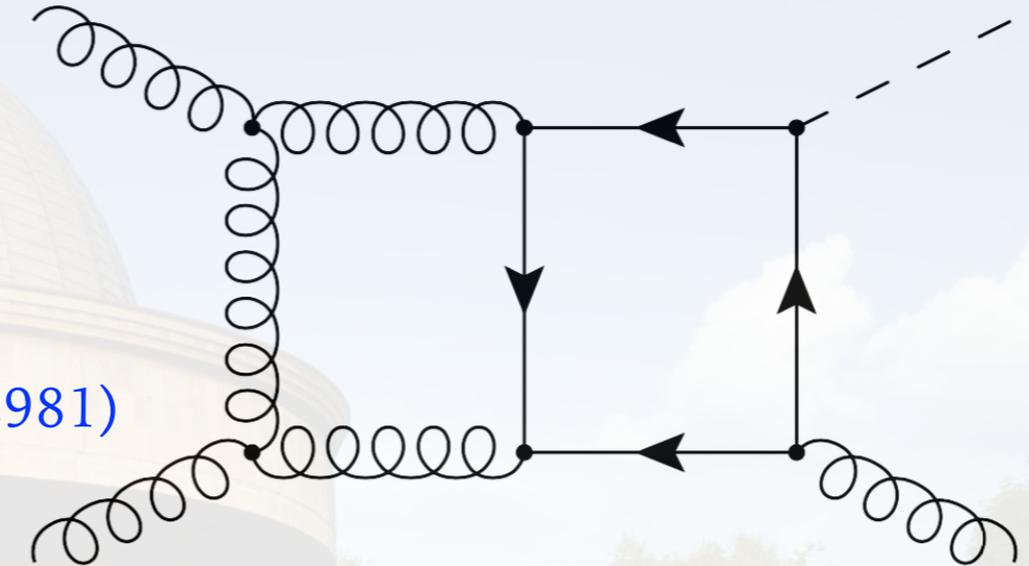
➤ K-factor **nearly flat** at large p_T

➤ Several open questions.....

➤ Combination with NNLO HTL

➤ Top-quark mass scheme uncertainty OS/MSbar

➤ Numerical stability of P.S. at large p_T



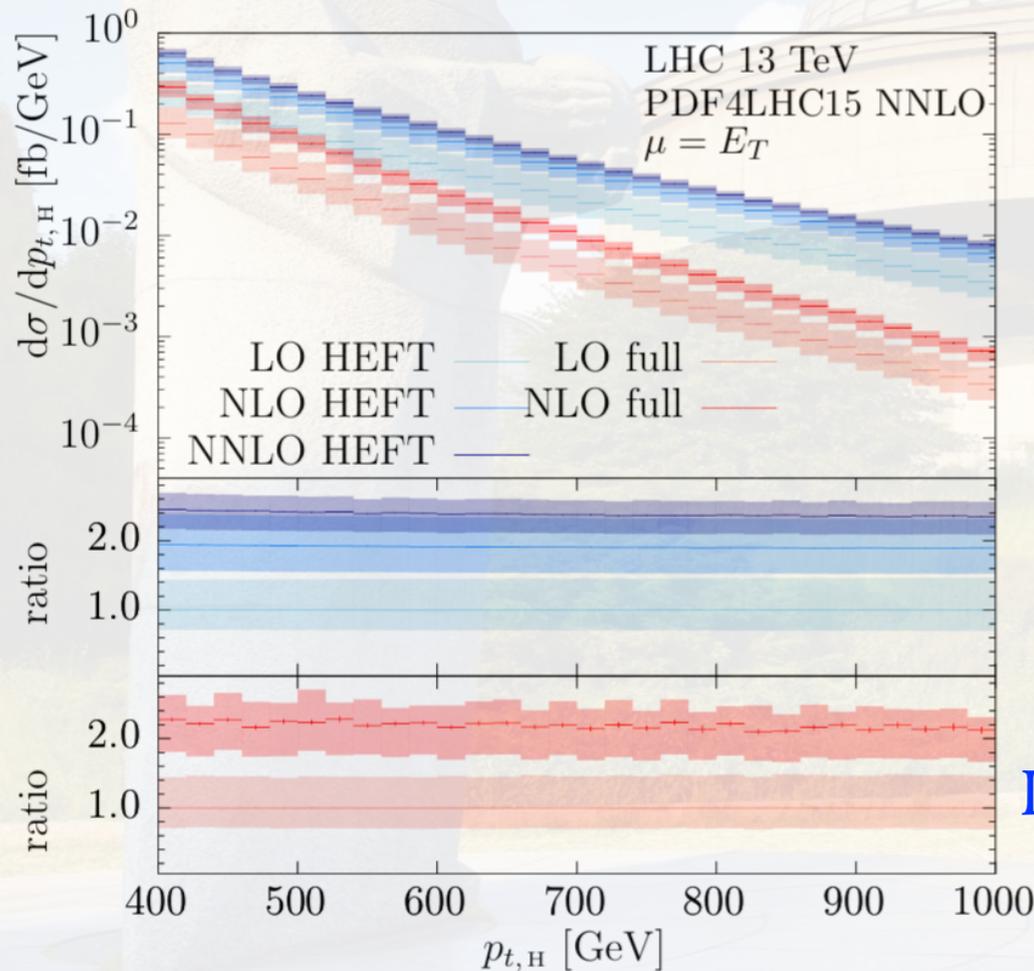
Jones, Kerner, Luisoni (1802.00349)

HIGGS TRANSVERSE MOMENTUM AT BOOSTED REGION

- Extension to NNLO HTL/NLO SM combined distributions in boosted region:

Rescale NLO by $K_{NNLO} = NNLO_{HTL}/NLO_{HTL}$ $d\sigma^{EFT-improved(1), NNLO} = \frac{d\sigma^{QCD, NLO}}{dp_{\perp}} \frac{d\sigma^{EFT, NNLO}}{dp_{\perp}}$

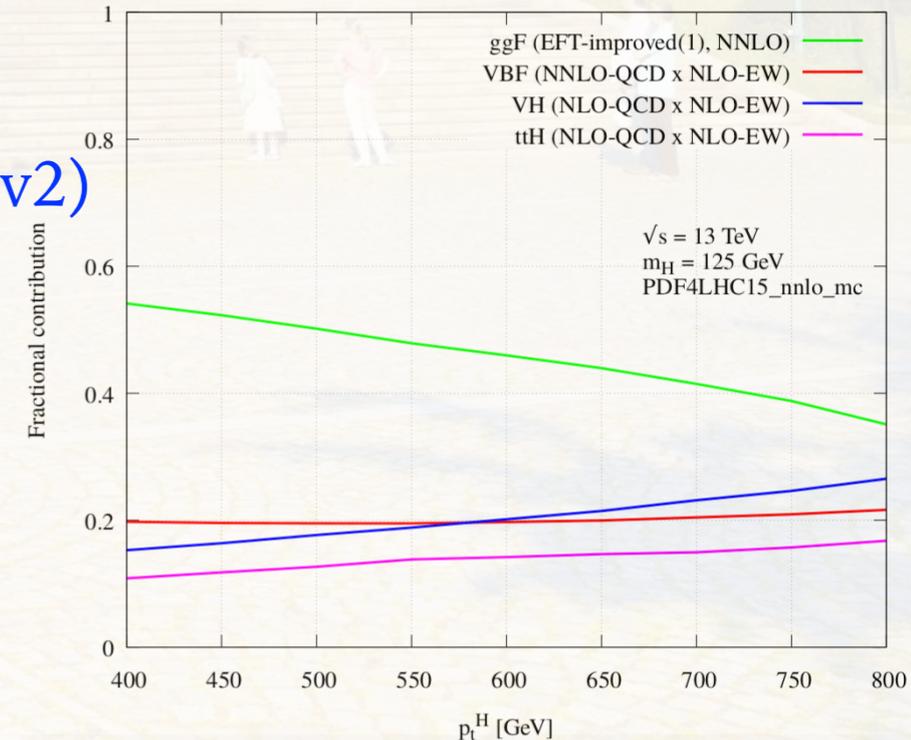
Assumes SM/HTL K-factors similar

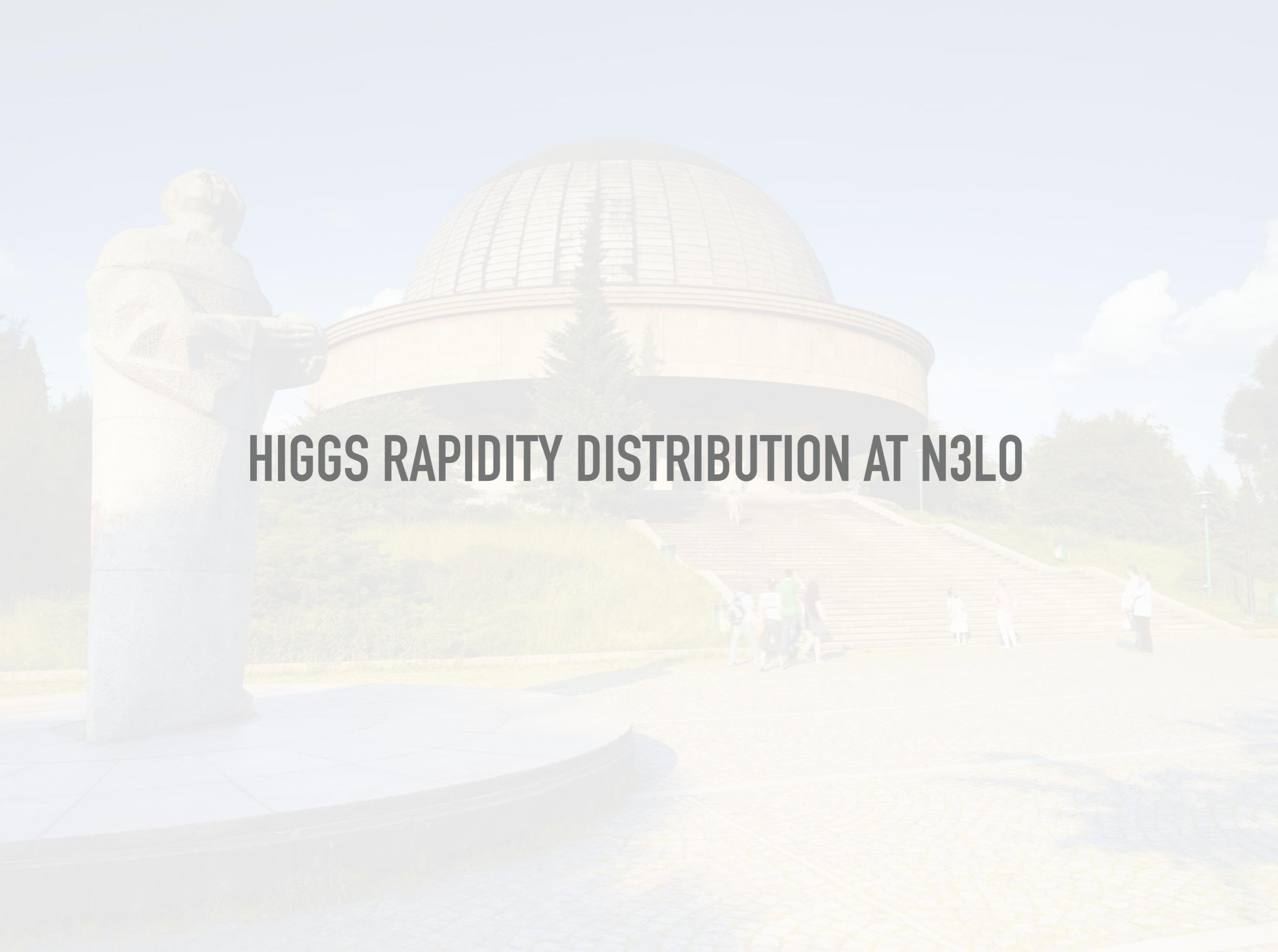


p_T^{cut}	LO _{full}	NLO _{full}	K_{full}^{NLO}	LO _{EFT}	NLO _{EFT}	NNLO _{EFT}	K_{EFT}^{NLO}	K_{EFT}^{NNLO}
400	11.9 ^{+45%} _{-29%}	27 ^{+15%} _{-20%}	2.23	32 ^{+44%} _{-29%}	63 ^{+23%} _{-19%}	78 ^{+9.2%} _{-12%}	1.93	1.25
430	8.2 ^{+45%} _{-29%}	18.3 ^{+14%} _{-21%}	2.22	25 ^{+44%} _{-29%}	48 ^{+22%} _{-19%}	60 ^{+9.1%} _{-11%}	1.92	1.25
450	6.5 ^{+45%} _{-29%}	14.5 ^{+14%} _{-21%}	2.22	21 ^{+45%} _{-29%}	41 ^{+22%} _{-19%}	51 ^{+9.1%} _{-11%}	1.92	1.25
500	3.7 ^{+45%} _{-29%}	8.1 ^{+14%} _{-21%}	2.22	14.2 ^{+45%} _{-29%}	27 ^{+22%} _{-20%}	34 ^{+9%} _{-11%}	1.91	1.25
550	2.1 ^{+45%} _{-30%}	4.7 ^{+13%} _{-21%}	2.19	9.8 ^{+45%} _{-29%}	18.6 ^{+22%} _{-20%}	23 ^{+8.9%} _{-11%}	1.91	1.25
600	1.28 ^{+46%} _{-30%}	2.8 ^{+14%} _{-21%}	2.18	6.8 ^{+45%} _{-29%}	13.0 ^{+22%} _{-20%}	16.2 ^{+8.8%} _{-11%}	1.90	1.25
650	0.79 ^{+46%} _{-30%}	1.71 ^{+14%} _{-21%}	2.17	4.9 ^{+46%} _{-29%}	9.3 ^{+22%} _{-20%}	11.5 ^{+8.7%} _{-11%}	1.90	1.24
700	0.49 ^{+47%} _{-30%}	1.06 ^{+14%} _{-21%}	2.15	3.5 ^{+46%} _{-29%}	6.7 ^{+22%} _{-20%}	8.3 ^{+8.7%} _{-11%}	1.90	1.24
750	0.32 ^{+47%} _{-30%}	0.67 ^{+13%} _{-21%}	2.14	2.6 ^{+46%} _{-30%}	4.9 ^{+22%} _{-20%}	6.1 ^{+8.6%} _{-11%}	1.90	1.24
800	0.20 ^{+47%} _{-30%}	0.43 ^{+13%} _{-21%}	2.12	1.90 ^{+46%} _{-30%}	3.6 ^{+22%} _{-20%}	4.5 ^{+8.6%} _{-11%}	1.90	1.24
850	0.135 ^{+47%} _{-30%}	0.28 ^{+13%} _{-21%}	2.10	1.42 ^{+47%} _{-30%}	2.7 ^{+22%} _{-20%}	3.3 ^{+8.6%} _{-11%}	1.89	1.24

LHCHXSWG-2019-002(v2)

- Considerable contribution from VH, VBF and ttH.
- State-of-the-art precision at NNLO except ttH (NLO).
- Sensitive to BSM models like new generation of quark





HIGGS RAPIDITY DISTRIBUTION AT N³LO

HIGGS PRODUCTION AT N3LO (APPROXIMATED)

- Extend qT-subtraction method to N3LO (Cieri, XC et al. 1807.11501).

In qT (CSS) factorisation to Higgs production at N3LO:

$$\frac{d\sigma}{dp_T^2 dy} = \frac{m_H^2}{s} \sigma_{LO}^H \int_0^{+\infty} db \frac{b}{2} J_0(bp_T) S_g(m_H, b) \sum_{a_1, a_2} \int_{x_1}^1 \frac{dz_1}{z_1} \int_{x_2}^1 \frac{dz_2}{z_2} [HC_1 C_2]_{gg:a_1 a_2} \prod_{i=1,2} f_{a_i/h_i}(x_i/z_i, b_0^2/b^2)$$

$$S_c(M, b) = \exp \left[- \int_{b_0^2/b^2}^{M^2} \frac{dq^2}{q^2} \left(A_c(\alpha_s(q^2)) \ln \frac{M^2}{q^2} + B_c(\alpha_s(q^2)) \right) \right]$$

- Apply q_T^{cut} to factorise full N3LO into two parts.

$$d\sigma_{N^3LO}^H = \mathcal{H}_{N^3LO}^H \otimes d\sigma_{LO}^H \Big|_{\delta(p_T)} + \left[d\sigma_{NNLO}^{H+jet} - d\sigma_{N^3LO}^{H CT} \right]_{p_T > q_T^{cut}}$$

- Above q_T^{cut} , recycle H+jet at NNLO from NNLOJET with qT counter terms (CT) to regulate IR divergence.

- Below q_T^{cut} , factorise real radiations from hard coefficient functions at $\delta(p_T)$ in HN3LO package.

- Most of the factorised components of $\delta(p_T)$ contribution are known analytically at N3LO.

- We use a constant $C_{N3} \delta_{ga} \delta_{gb} (1-z)$ to approximate the unknown pieces.

- Numerically abstract the C_{N3} coefficient using exact N3LO total cross section (1802.00833, 1802.00827).

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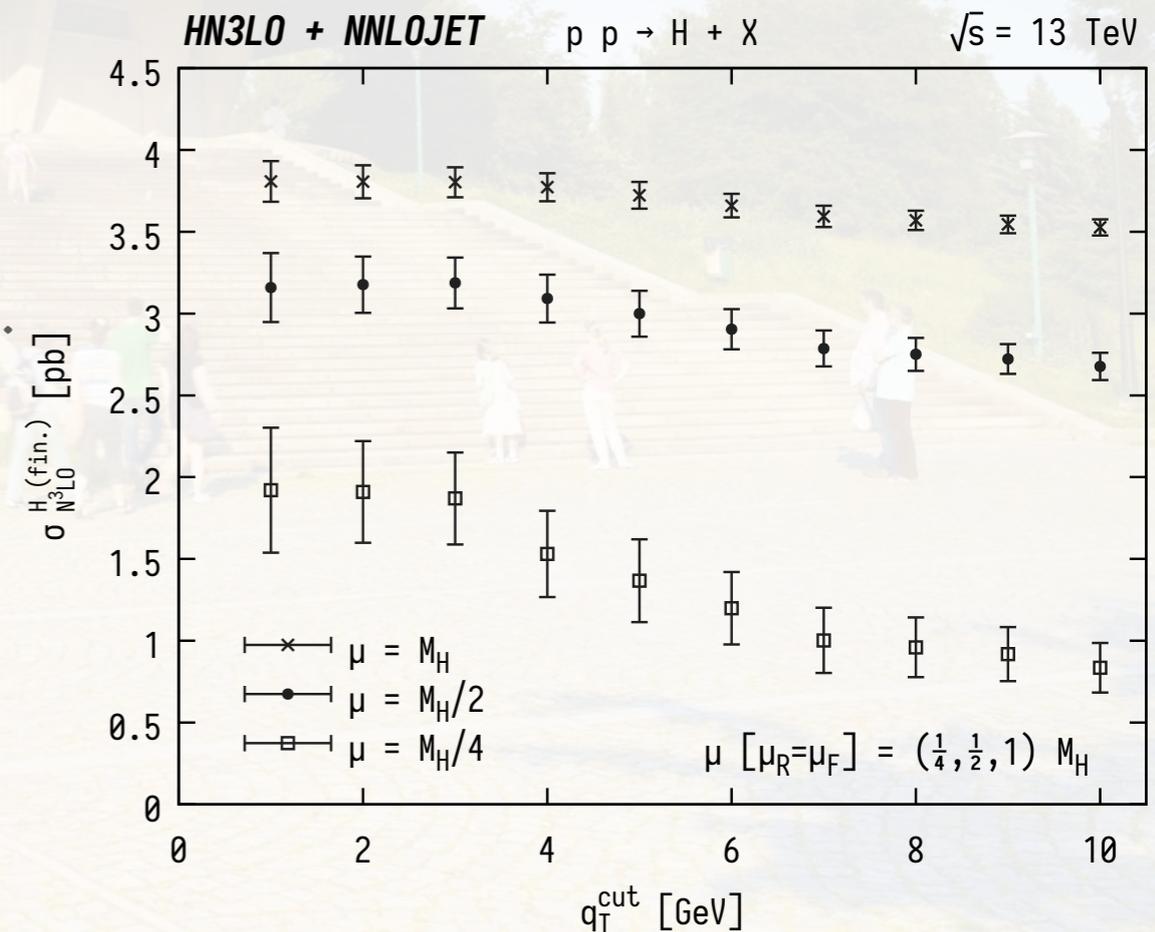
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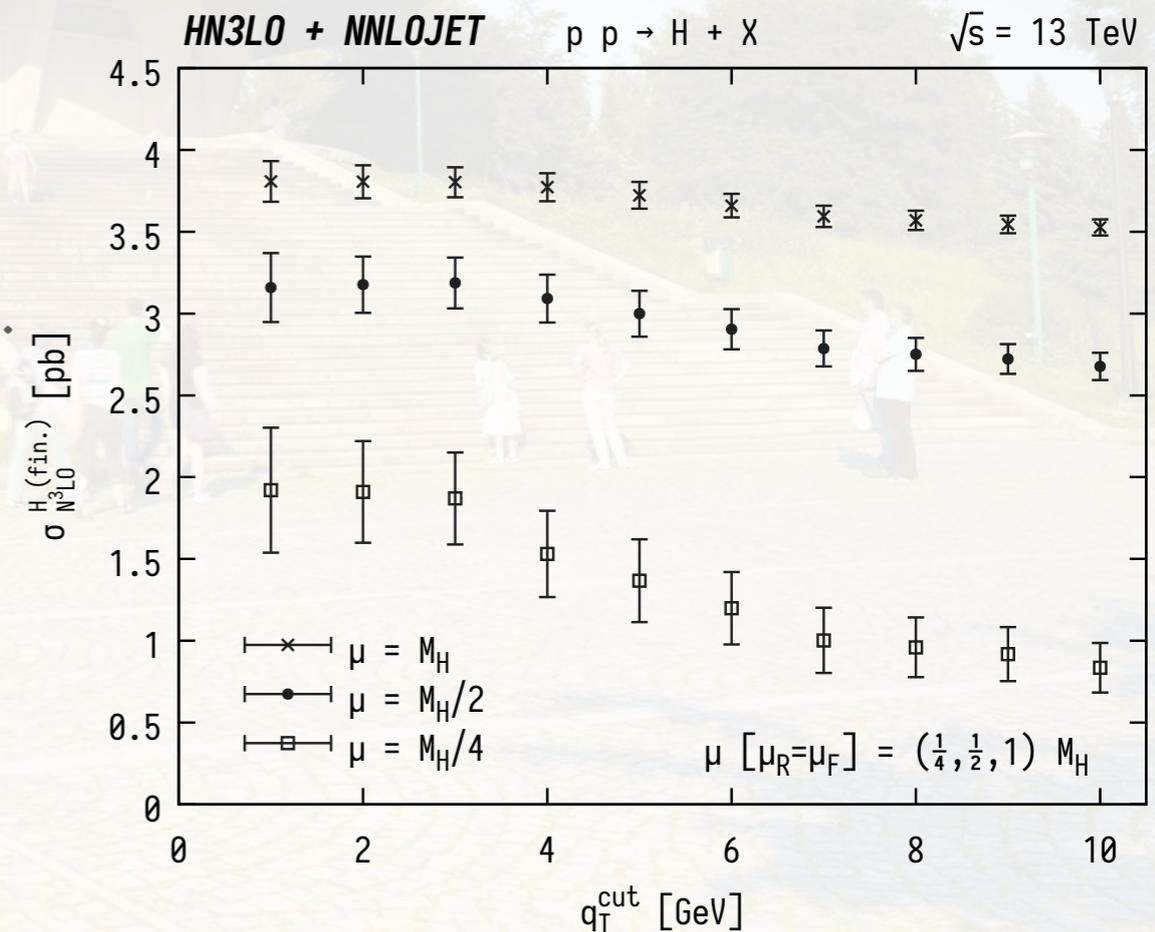
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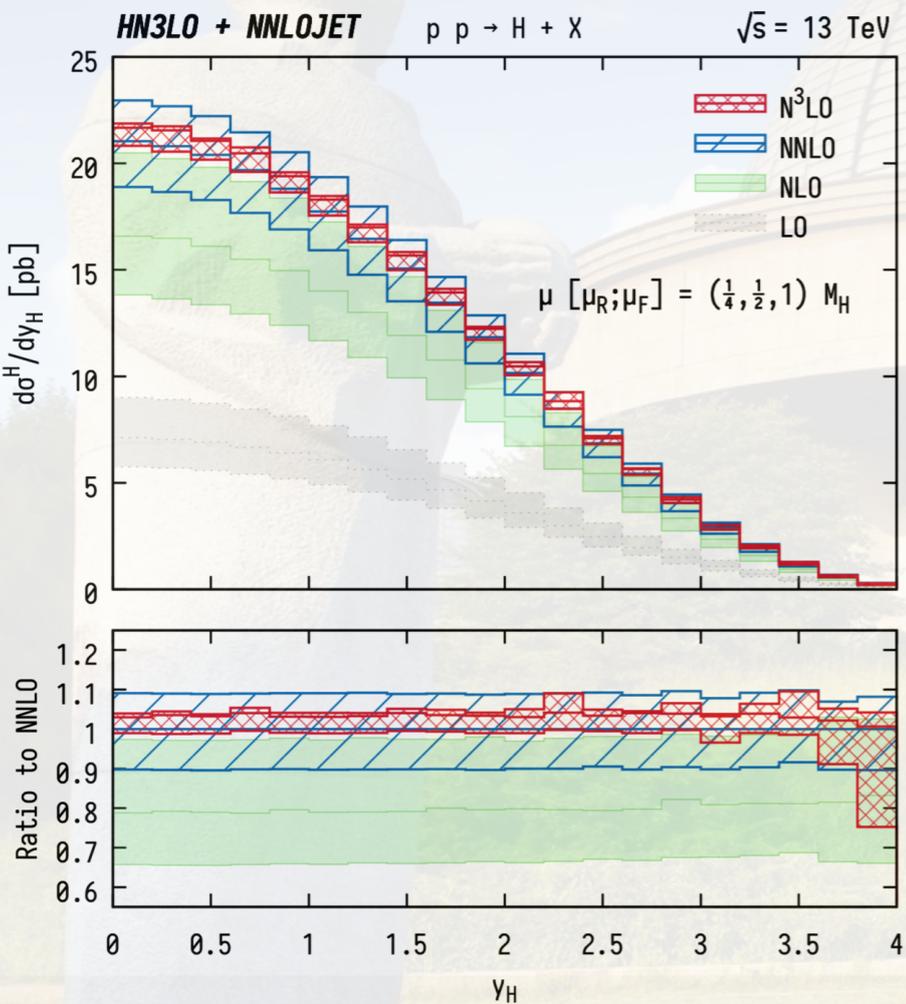
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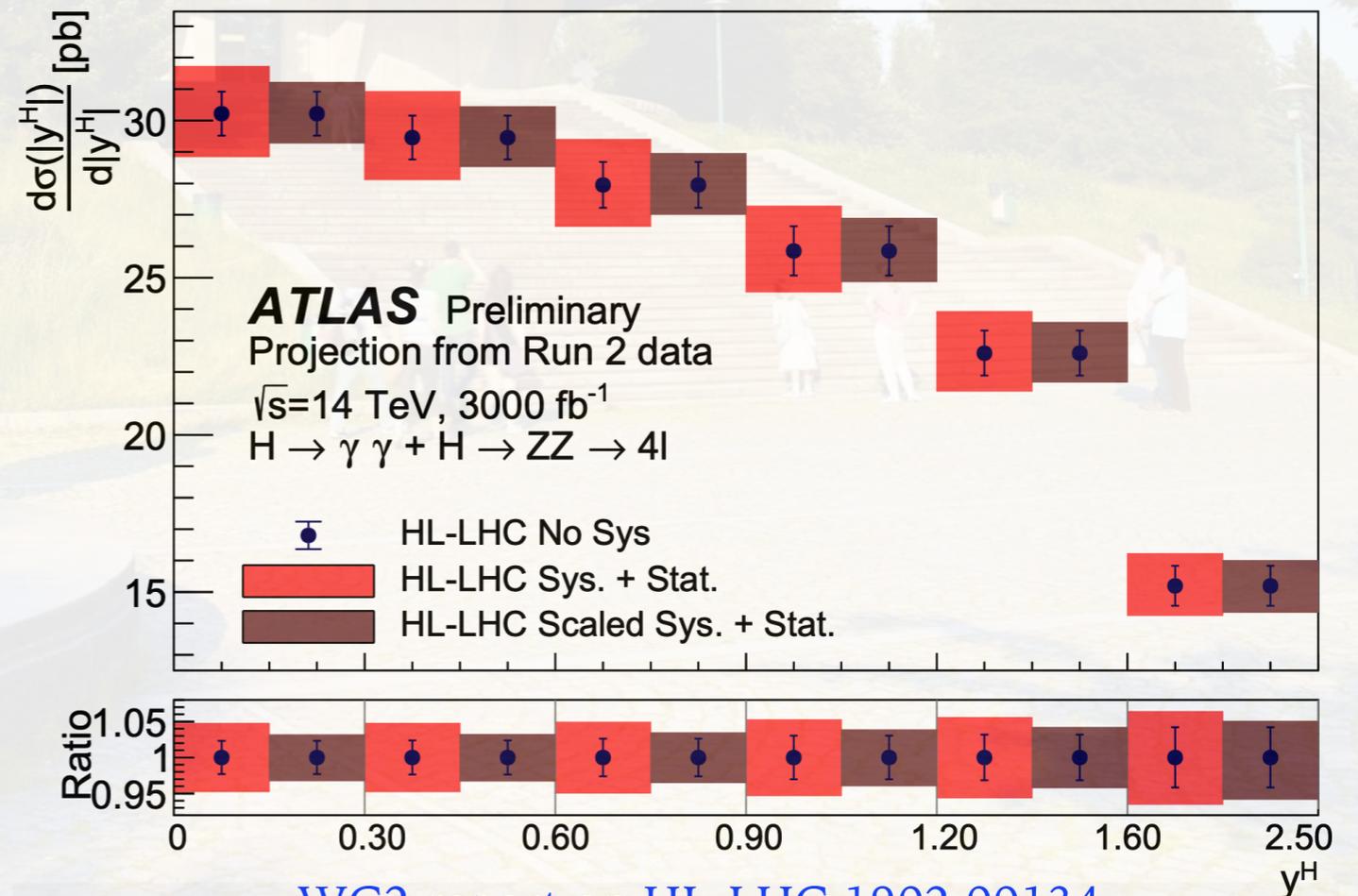


HIGGS RAPIDITY DISTRIBUTIONS AT N3LO (APPROXIMATED)

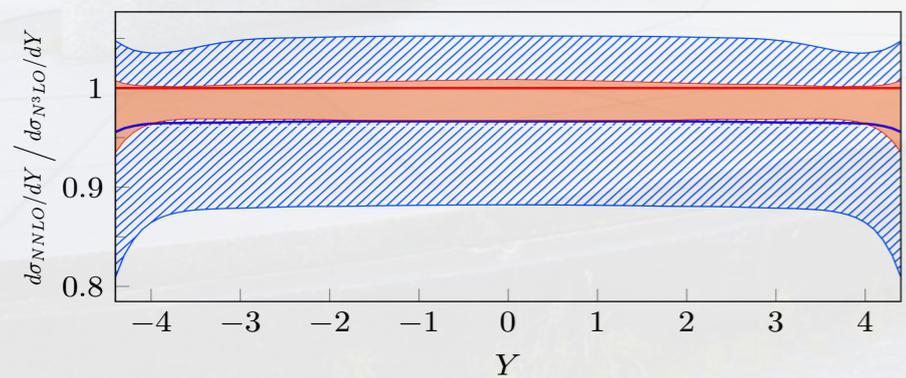
➤ **N3LO differential observables** at the LHC from **qT-subtraction** and **threshold expansion**



- Remarkably flat K-factor (as expected)
- QCD scale uncertainty reduced to $+1\%$ -3%
- Comparable to (S2) HL-LHC projections $\pm 3\%$
- Future upgrade to reduce PDF and α_s uncertainties



Cieri, XC, Gehrmann, Glover, Huss 1807.11501



Dulat, Mistlberger, Pelloni 1810.09462

WG2 report on HL-LHC 1902.00134

SUMMARY

- High Energy Physics is advancing to precision study at a steady speed (Target set for the next 20 years)
- Higgs boson precision measurements focus on differential observables and distinguishing production and decay channels
- Higgs boson precision theory studies focus on reducing uncertainties from all sources. Major factor still from QCD
- NNLO QCD is the new standard for Higgs production channel, more consistent update to PDF and α_s will be available soon
- NNLO+N3LL and N3LO precision are available for limited observables and are already promising for HL-LHC accuracy
- Many important studies are still missing: quark mass, NLO parton shower, $\alpha\alpha_s$ mixing, interference contributions

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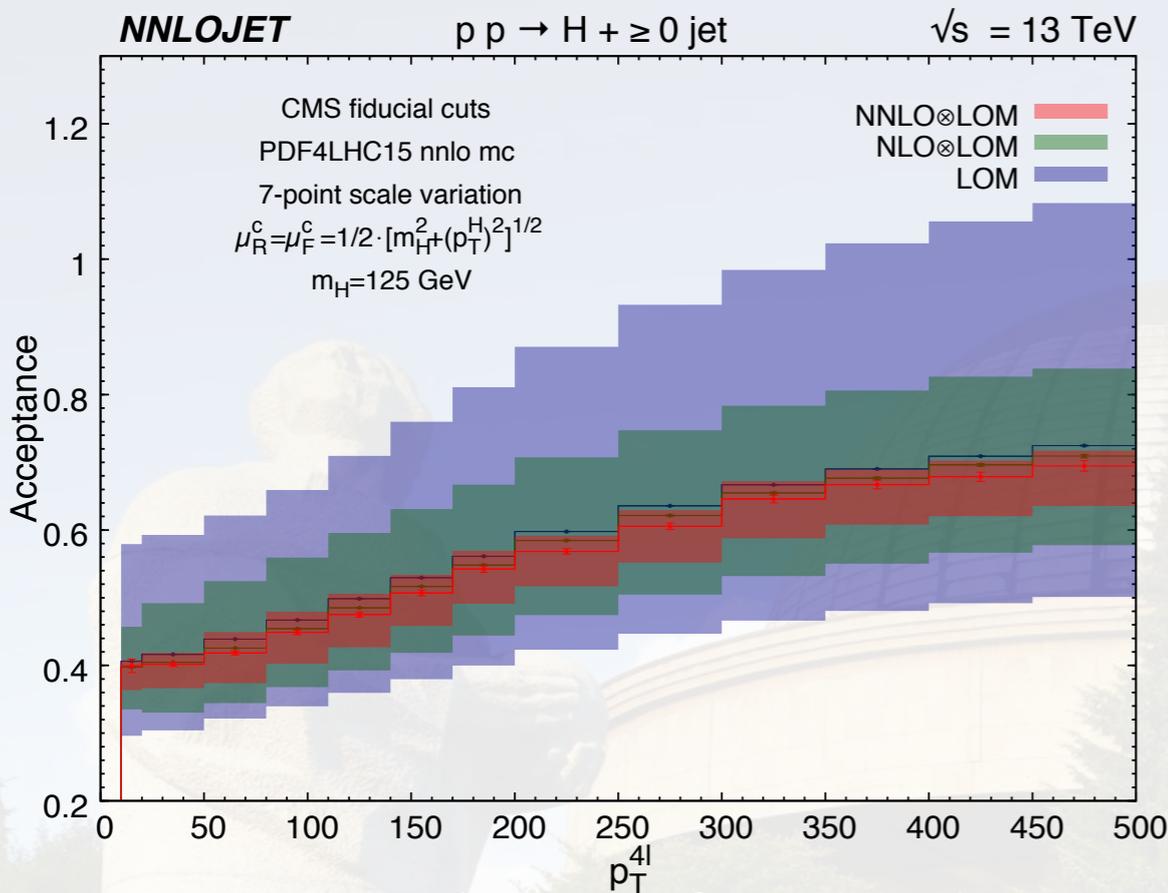
Thank You for Your Attention

Total time (int. dimension Of the tree level)	LO	NLO	NNLO
H	1 min (3)	30 min (6)	300h (9)
H→di-photon	1 min (3)	40 min (6)	400h (9)
H→4l (2e2mu, 4e, 4mu require at least two separate runs)	2~3 min (9)	2h (12)	1000h (15)
H+j	3 min (6)	1.5h (9)	70000h (12)
H→di-photon + jet	4 min (6)	2h (9)	90000h (12)
H→4l (2e2mu, 4e, 4mu require at least two separate runs)+jet	20 min (12)	10h (15)	600000h (18)
H_qT	20 min (6)	5h (9)	7000000h (12)

ACCEPTANCE STUDY

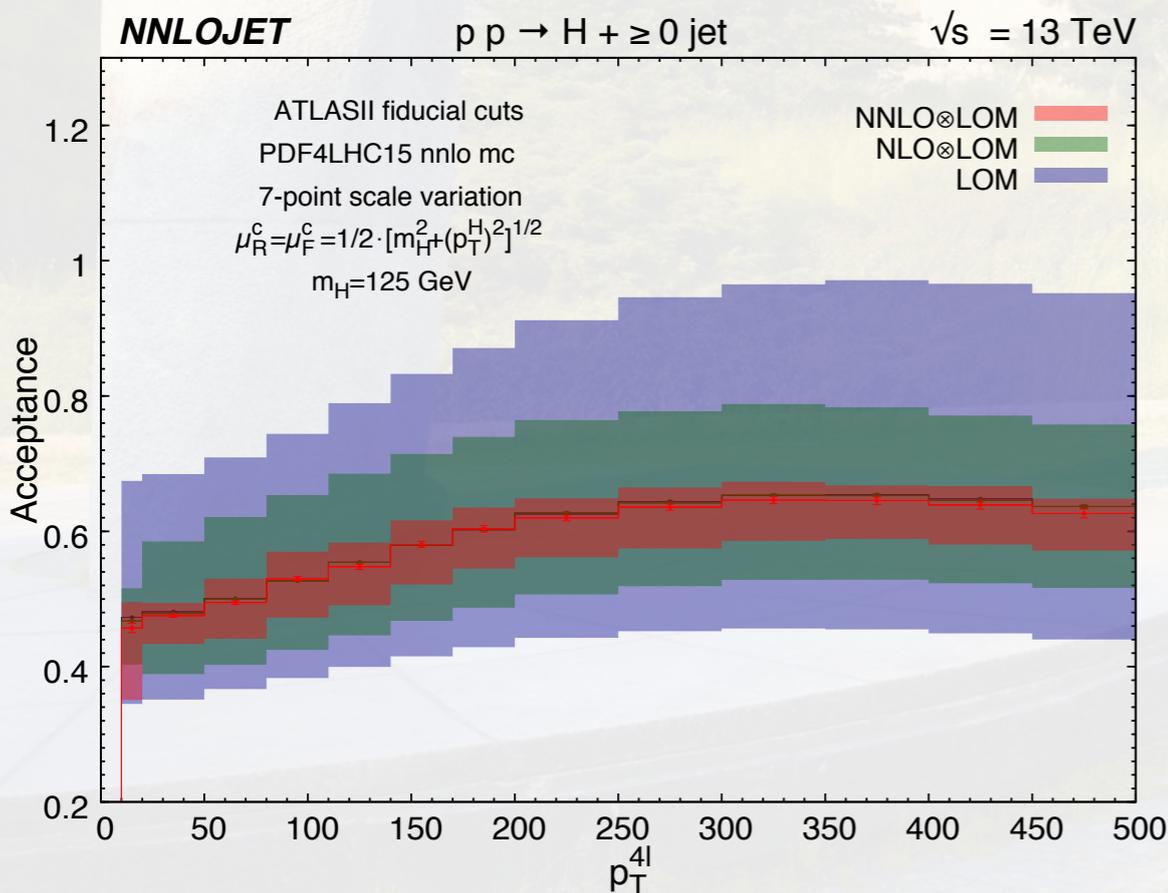
$$H \rightarrow ZZ^* \rightarrow 4l$$

CMS cuts



Acceptance deviate from each FO

ATLAS cuts



Acceptance consistent for each FO

- CMS (1706.09936) and ATLAS (1708.02810) use different lepton isolation algorithm in $ZZ^* \rightarrow 4l$

Fiducial Cuts	CMS	ATLAS
Lepton Isolation		
Cone size R^l	0.3	—
$\sum p_T^i / p_T^l (i \in R^l)$	< 35%	—
$\Delta R^{SF(DF)}(l_i, l_j)$	> 0.02	> 0.1 (0.2)
Jet Definition (anti-kT with R=0.4)		
p_T^{jets} (GeV)	> 30	> 30
$ y^{jets} $	< 2.5	< 4.4
$\Delta R(jet, e(\mu))$	—	> 0.2 (0.1)

- Fixed order study of acceptance reveals detailed structures

$$A_{FO}(\mathcal{O}) = \frac{d\sigma_{FO}^{H(\rightarrow ZZ^* \rightarrow 4l) + jet} / d\mathcal{O}}{d\sigma_{FO}^{H+jet} / d\mathcal{O} \times (BR_{2e2\mu} + BR_{4\mu} + BR_{4e})}$$