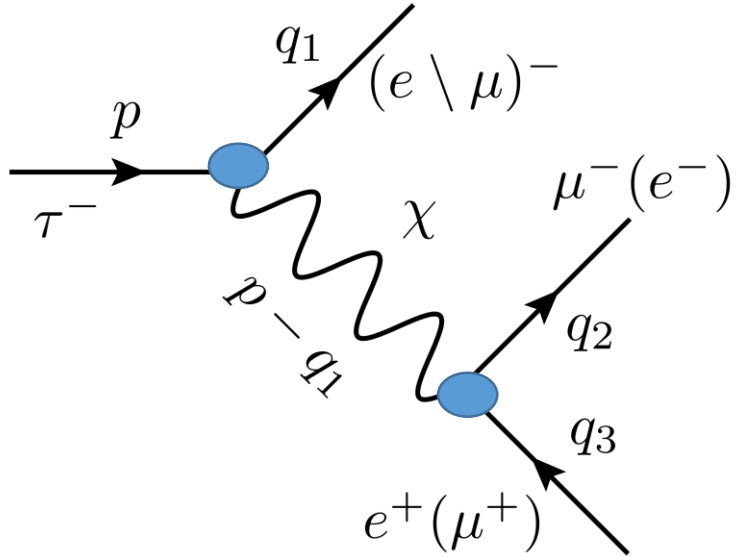
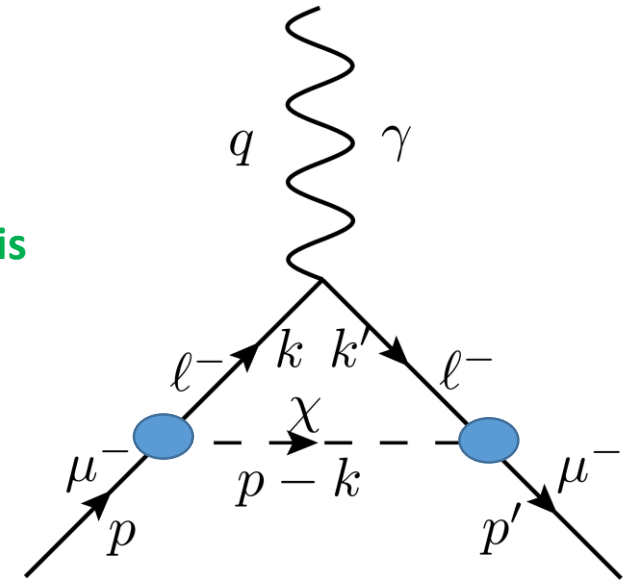


Effective Lagrangians for LFV interactions involving a boson (χ)



Work done as part of the Ph. D. Thesis
of Marcela Marín
Cinvestav (Mexico City)

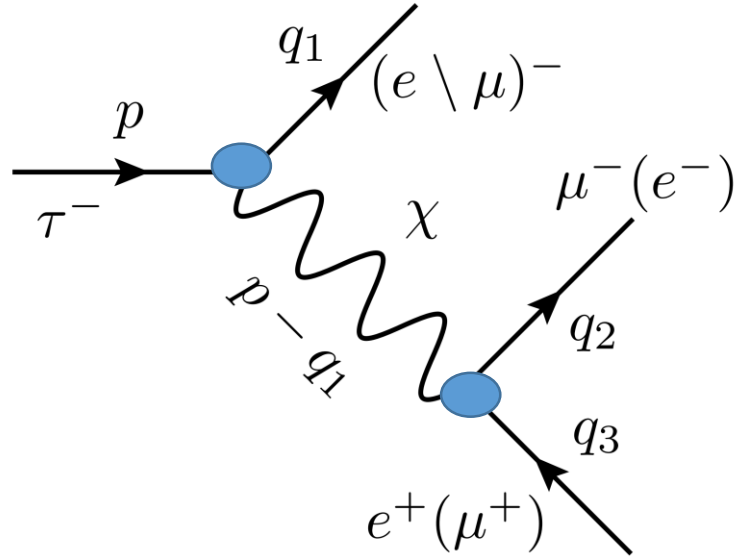
Pablo Roig



Matter To The Deepest
Recent Developments In Physics Of Fundamental Interactions
XLIII International Conference of Theoretical Physics

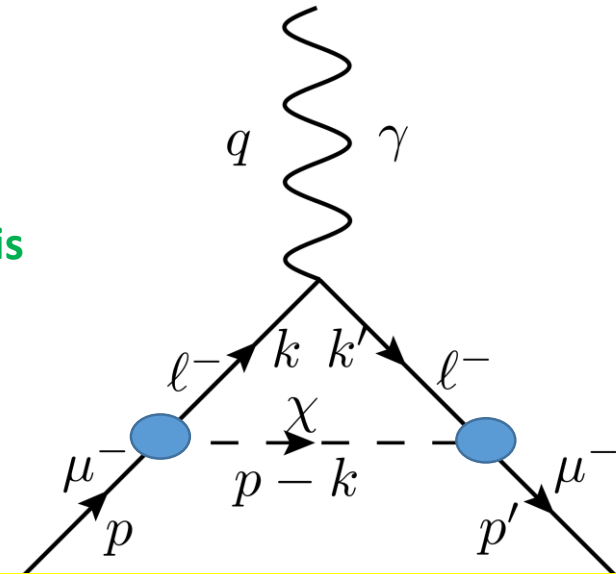
Katowice, Poland, 1-6 Sept. 2019

Effective Lagrangians for LFV interactions involving a boson (χ)



Work done as part of the Ph. D. Thesis
of Marcela Marín
Cinvestav (Mexico City)

Pablo Roig



We should upload the pre-print to arXiv soon, so suggestions for improvements are very welcome!!

Matter To The Deepest
Recent Developments In Physics Of Fundamental Interactions
XLIII International Conference of Theoretical Physics

Katowice, Poland, 1-6 Sept. 2019

CONTENTS

- **MOTIVATION**
- **EFFECTIVE LAGRANGIANS**
- **PHENOMENOLOGY**
- **CONCLUSIONS**

MOTIVATION

DESY 95-071
April 1995

ISSN 0418-9833

A Search for the lepton-flavour violating Decays

$$\tau \rightarrow e\alpha, \tau \rightarrow \mu\alpha$$

The ARGUS Collaboration

Request by Denis Epifanov (Belle) to develop theory for this analysis.

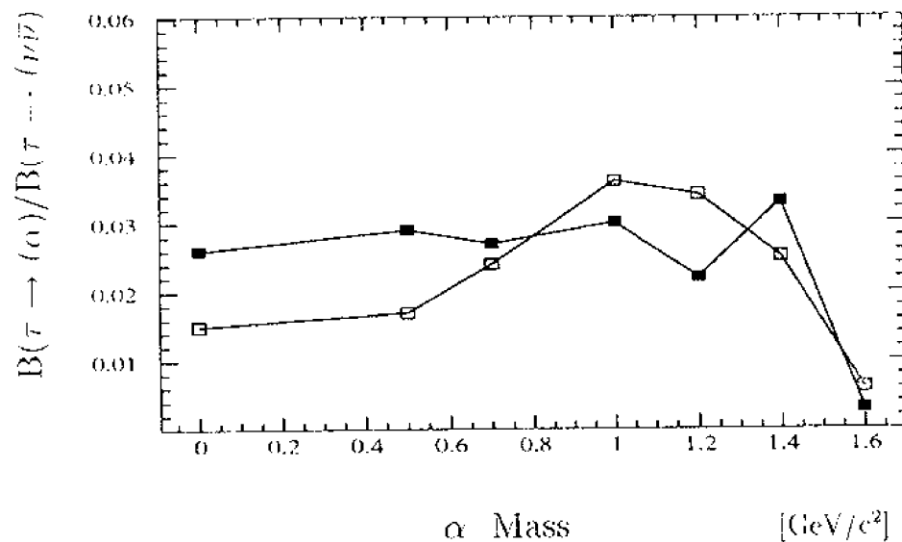


Figure 1: The upper limits at 95% confidence level on the ratio $B(\tau \rightarrow \ell\alpha)/B(\tau \rightarrow \ell\nu\bar{\nu})$ for electrons (open squares) and muons (full squares)

MOTIVATION

DESY 95-071
April 1995

ISSN 0418-9833

A Search for the lepton-flavour violating Decays

$$\tau \rightarrow e\alpha, \tau \rightarrow \mu\alpha$$

The ARGUS Collaboration

These limits (permille level) contrast a lot with most of the upper bounds on LFV decays

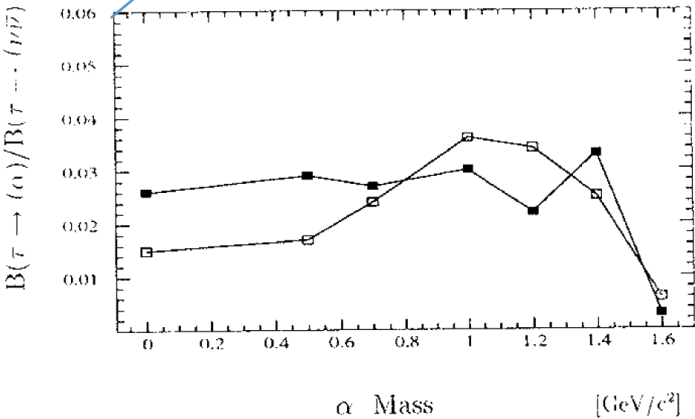
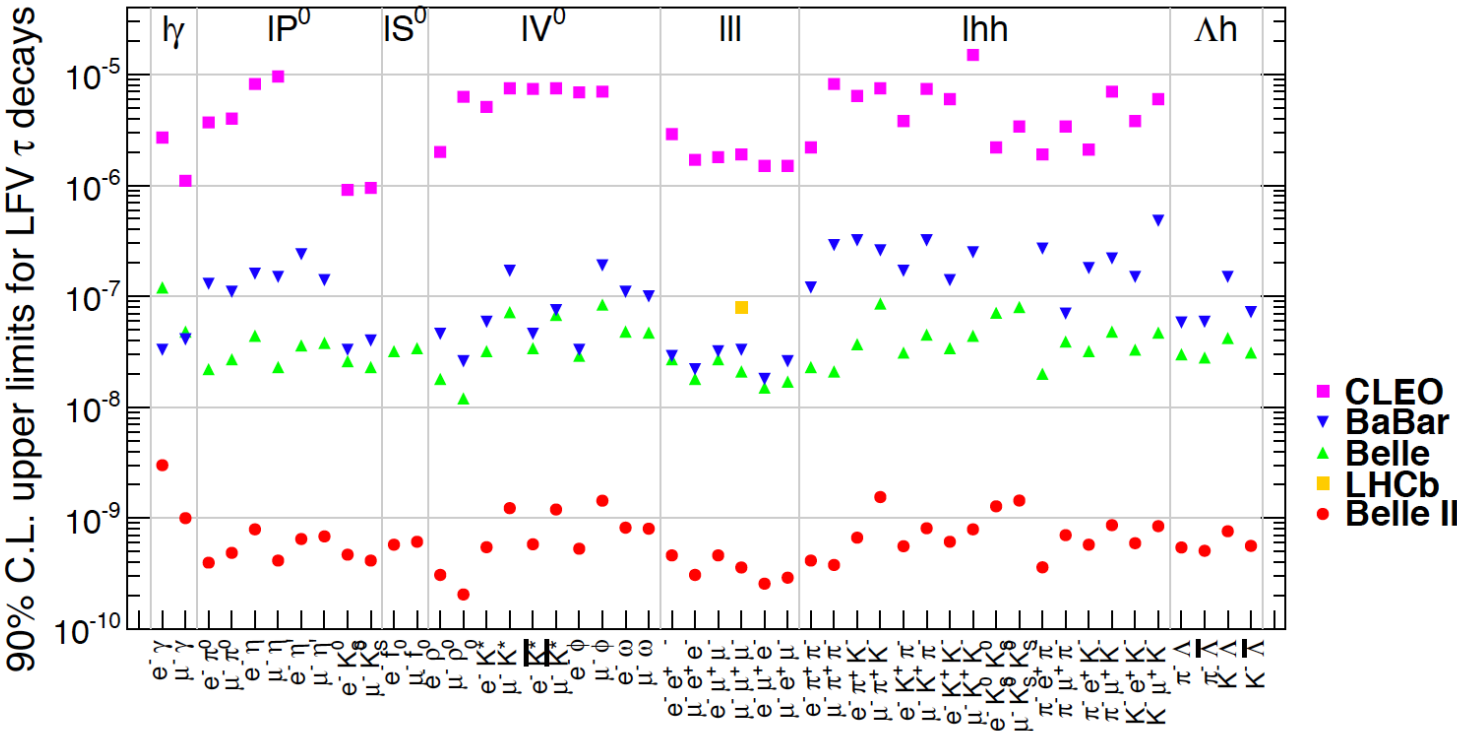


Figure 1: The upper limits at 95% confidence level on the ratio $B(\tau \rightarrow \ell\alpha)/B(\tau \rightarrow \ell\nu\bar{\nu})$ for electrons (open squares) and muons (full squares)



Effective LFV interactions involving a boson (χ)

Pablo Roig (Cinvestav)

MOTIVATION: Why LFV?

SM was built originally without RH neutrinos \Rightarrow LF (& LN) is conserved

MOTIVATION: Why LFV?

SM was built originally without RH neutrinos \Rightarrow LF (& LN) is conserved

Neutrino oscillations \Rightarrow Neutrino masses are non-zero \Rightarrow LF (& maybe LN) are not conserved

MOTIVATION: Why LFV?

SM was built originally without RH neutrinos \Rightarrow LF (& LN) is conserved

Neutrino oscillations \Rightarrow Neutrino masses are non-zero \Rightarrow LF (& maybe LN) are not conserved

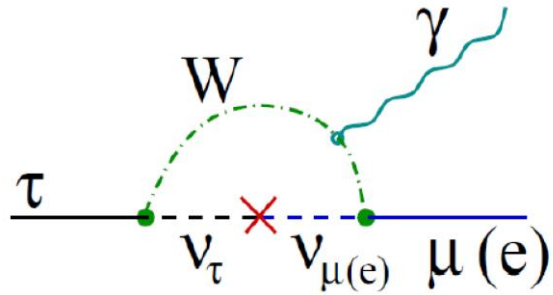
SM minimally extended with ν masses \Rightarrow Unobservable cLFV

MOTIVATION: Why LFV?

SM was built originally without RH neutrinos => LF (& LN) is conserved

Neutrino oscillations => Neutrino masses are non-zero => LF (& maybe LN) are not conserved

SM minimally extended with ν masses => Unobservable cLFV



$$BR(\mu \rightarrow e \gamma) \simeq \frac{\Gamma(\mu \rightarrow e \gamma)}{\Gamma(\mu \rightarrow e \nu \bar{\nu})} = \frac{3\alpha}{32\pi} \left| \sum_{k=1,3} \frac{U_{\mu k} U_{ek}^* m_{\nu k}^2}{m_W^2} \right|^2 \sim 10^{-54}$$

UL @ 10^{-13} level

Cheng-Li, Petcov '77

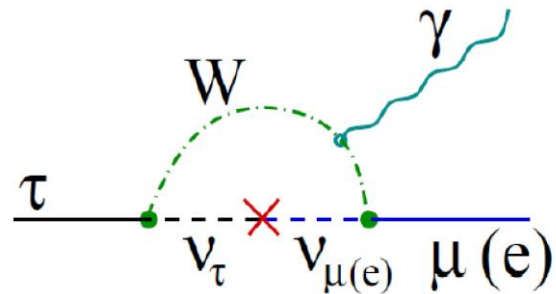
GIM-like

MOTIVATION: Why LFV?

SM was built originally without RH neutrinos => LF (& LN) is conserved

Neutrino oscillations => Neutrino masses are non-zero => LF (& maybe LN) are not conserved

SM minimally extended with ν masses => Unobservable cLFV



Present limits

$10^{-6}, 10^{-5}$

$10^{-4}, 10^{-2}$

$10^{-12}, 10^{-8}$

SM predictions

$BR(Z \rightarrow l l') \sim 10^{-54}$ Illana & Riemann '01

$BR(H \rightarrow l l') \sim 10^{-55}$ Arganda, Curiel, Herrero & Temes '05

$BR(\mu \rightarrow 3e) \sim 10^{-54}$ $BR(\tau \rightarrow 3l) \sim 10^{-55}$ Hernández-Tomé, López-Castro & Roig '19

$$BR(\mu \rightarrow e \gamma) \simeq \frac{\Gamma(\mu \rightarrow e \gamma)}{\Gamma(\mu \rightarrow e \nu \bar{\nu})} = \frac{3\alpha}{32\pi} \left| \sum_{k=1,3} \frac{U_{\mu k} U_{ek}^* m_{\nu k}^2}{m_W^2} \right|^2 \sim 10^{-54}$$

UL @ 10^{-13} level

Cheng-Li, Petcov '77

GIM-like

LFV Process	Future Sensitivity
$\mu \rightarrow e \gamma$	6×10^{-14}
$\tau \rightarrow e \gamma$	$\sim 3 \times 10^{-9}$
$\tau \rightarrow \mu \gamma$	$\sim 3 \times 10^{-9}$
$\mu \rightarrow e e e$	$\sim 10^{-16}$
$\tau \rightarrow \mu \mu \mu$	$\sim 10^{-9}$

Effective LFV interactions involving a boson (χ)

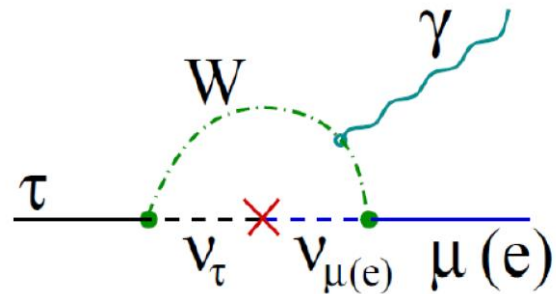
Pablo Roig (Cinvestav)

MOTIVATION: Why LFV?

SM was built originally without RH neutrinos => LF (& LN) is conserved

Neutrino oscillations => Neutrino masses are non-zero => LF (& maybe LN) are not conserved

SM minimally extended with ν masses => Unobservable cLFV



Present limits

$10^{-6}, 10^{-5}$

$10^{-4}, 10^{-2}$

$10^{-12}, 10^{-8}$

SM predictions

$BR(Z \rightarrow l l') \sim 10^{-54}$ Illana & Riemann '01

$BR(H \rightarrow l l') \sim 10^{-55}$ Arganda, Curiel, Herrero & Temes '05

$BR(\mu \rightarrow 3e) \sim 10^{-54}$ $BR(\tau \rightarrow 3l) \sim 10^{-55}$ Hernández-Tomé, López-Castro & Roig '19

$$BR(\mu \rightarrow e \gamma) \simeq \frac{\Gamma(\mu \rightarrow e \gamma)}{\Gamma(\mu \rightarrow e \nu \bar{\nu})} = \frac{3\alpha}{32\pi} \left| \sum_{k=1,3} \frac{U_{\mu k} U_{ek}^* m_{\nu k}^2}{m_W^2} \right|^2 \sim 10^{-54}$$

UL @ 10^{-13} level

Cheng-Li, Petcov '77

GIM-like

LFV Process	Future Sensitivity
$\mu \rightarrow e \gamma$	6×10^{-14}
$\tau \rightarrow e \gamma$	$\sim 3 \times 10^{-9}$
$\tau \rightarrow \mu \gamma$	$\sim 3 \times 10^{-9}$
$\mu \rightarrow e e e$	$\sim 10^{-16}$
$\tau \rightarrow \mu \mu \mu$	$\sim 10^{-9}$

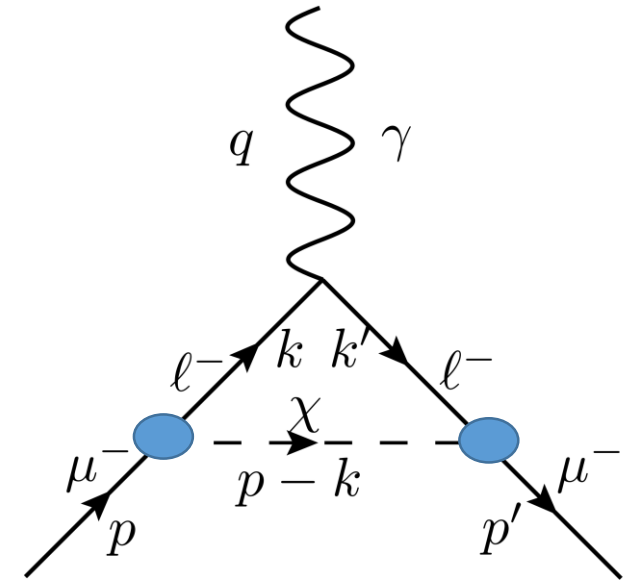
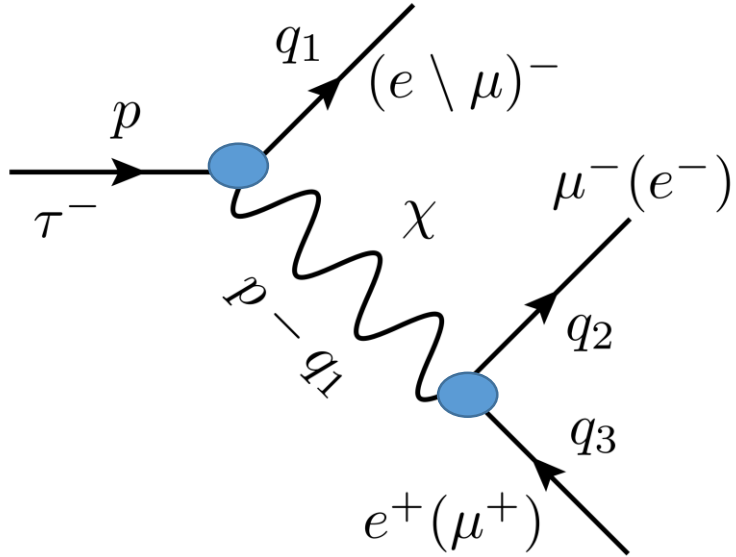
It is easy for reasonable BSM extensions to reach it

Effective LFV interactions involving a boson (χ)

Pablo Roig (Cinvestav)

MOTIVATION: Why effective LFV for $L \rightarrow l \chi$?

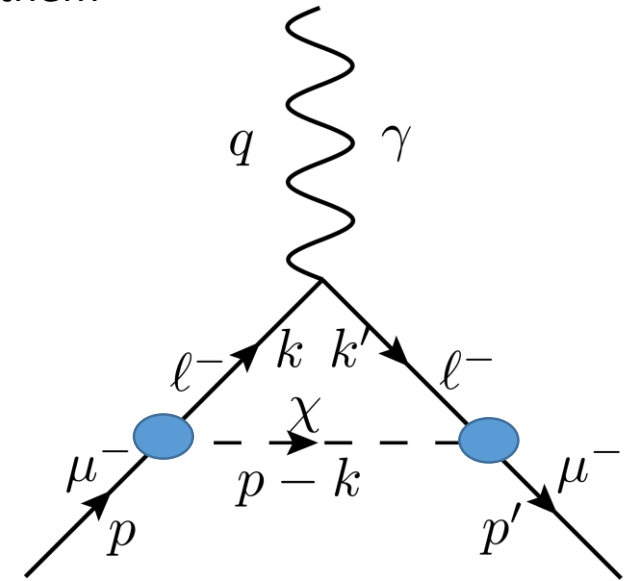
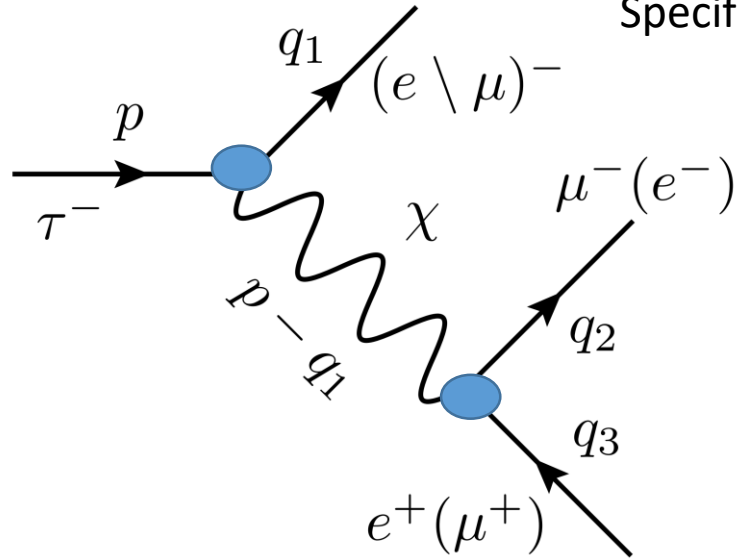
Effective Lagrangians offer the most general description of Physics that has not been resolved yet.



MOTIVATION: Why effective LFV for $L \rightarrow l \chi$?


Effective Lagrangians offer the most general description of Physics that has not been resolved yet.

Specific BSM models are given realizations of them




EFFECTIVE LAGRANGIANS

$$\mathcal{L}_{int} = g_{L\ell}^S \bar{L}\ell S + ig_{L\ell}^P \bar{L}\gamma_5\ell P + g_{L\ell}^V \bar{L}\gamma^\mu\ell V_\mu + g_{L\ell}^A \bar{L}\gamma^\mu\gamma_5\ell A_\mu + g_{L\ell}^T \bar{L}\sigma^{\mu\nu}\ell B_{\mu\nu} + \text{h.c.},$$

 $J^{PC} = 1^{+-}$

EFFECTIVE LAGRANGIANS

$$\mathcal{L}_{int} = g_{L\ell}^S \bar{L}\ell S + ig_{L\ell}^P \bar{L}\gamma_5\ell P + g_{L\ell}^V \bar{L}\gamma^\mu\ell V_\mu + g_{L\ell}^A \bar{L}\gamma^\mu\gamma_5\ell A_\mu + g_{L\ell}^T \bar{L}\sigma^{\mu\nu}\ell B_{\mu\nu} + \text{h.c.},$$



$$J^{PC} = 1^{+-}$$

$\chi = S, P, V, A, B_{\mu\nu}$

We will consider $m_\chi < M_\tau$, but *this is not necessary*

EFFECTIVE LAGRANGIANS

$$\mathcal{L}_{int} = g_{L\ell}^S \bar{L}\ell S + ig_{L\ell}^P \bar{L}\gamma_5\ell P + g_{L\ell}^V \bar{L}\gamma^\mu\ell V_\mu + g_{L\ell}^A \bar{L}\gamma^\mu\gamma_5\ell A_\mu + g_{L\ell}^T \bar{L}\sigma^{\mu\nu}\ell B_{\mu\nu} + \text{h.c.},$$


$$J^{PC} = 1^{+-}$$

$\chi = S, P, V, A, B_{\mu\nu}$

We will consider $m_\chi < M_\tau$, but this is not necessary

 This Lagrangian is not invariant under $SU(2)_L \times U(1)_Y$ (but *it does not have to be!*)

EFFECTIVE LAGRANGIANS

$$\mathcal{L}_{int} = g_{L\ell}^S \bar{L}\ell S + ig_{L\ell}^P \bar{L}\gamma_5\ell P + g_{L\ell}^V \bar{L}\gamma^\mu\ell V_\mu + g_{L\ell}^A \bar{L}\gamma^\mu\gamma_5\ell A_\mu + g_{L\ell}^T \bar{L}\sigma^{\mu\nu}\ell B_{\mu\nu} + \text{h.c.},$$

$\chi = S, P, V, A, B_{\mu\nu}$

We will consider $m_\chi < M_\tau$, but this is not necessary

$J^{PC} = 1^{+-}$

➡ This Lagrangian is not invariant under $SU(2)_L \times U(1)_Y$ (but it does not have to be!). However, we can consider instead

$$\begin{aligned} \mathcal{L}'_{int} = & \left(\frac{g'_{LR}{}^S}{\Lambda} \bar{\mathbb{L}}_L \Phi \ell_R + \frac{g'_{RL}{}^S}{\Lambda} \bar{L}_R \Phi^\dagger \ell_L \right) S + i \left(\frac{g'_{LR}{}^P}{\Lambda} \bar{\mathbb{L}}_L \Phi \gamma_5 \ell_R + \frac{g'_{RL}{}^P}{\Lambda} \bar{L}_R \gamma_5 \Phi^\dagger \ell_L \right) P \\ & + \left(g'_{LL}{}^V \bar{\mathbb{L}}_L \gamma^\mu \ell_L + g'_{RR}{}^V \bar{L}_R \gamma^\mu \ell_R \right) V_\mu + \left(g'_{LL}{}^A \bar{\mathbb{L}}_L \gamma^\mu \gamma_5 \ell_L + g'_{RR}{}^A \bar{L}_R \gamma^\mu \gamma_5 \ell_R \right) A_\mu \\ & + \left(\frac{g'_{LR}{}^T}{\Lambda} \bar{\mathbb{L}}_L \Phi \sigma^{\mu\nu} \ell_R + \frac{g'_{RL}{}^T}{\Lambda} \bar{L}_R \sigma^{\mu\nu} \Phi^\dagger \ell_L \right) B_{\mu\nu} + \text{h.c.}, \end{aligned}$$

$L\ell$ is omitted

EFFECTIVE LAGRANGIANS

$$\mathcal{L}_{int} = g_{L\ell}^S \bar{L} \ell S + i g_{L\ell}^P \bar{L} \gamma_5 \ell P + g_{L\ell}^V \bar{L} \gamma^\mu \ell V_\mu + g_{L\ell}^A \bar{L} \gamma^\mu \gamma_5 \ell A_\mu + g_{L\ell}^T \bar{L} \sigma^{\mu\nu} \ell B_{\mu\nu} + \text{h.c.},$$

$$J^{PC} = 1^{+-}$$

$\chi = S, P, V, A, B_{\mu\nu}$

We will consider $m_\chi < M_\tau$, but this is not necessary

➡ This Lagrangian is not invariant under $SU(2)_L \times U(1)_Y$ (but it does not have to be!). However, we can consider instead

$$\begin{aligned} \mathcal{L}'_{int} = & \left(\frac{g'_{LR}{}^S}{\Lambda} \bar{\mathbb{L}}_L \Phi \ell_R + \frac{g'_{RL}{}^S}{\Lambda} \bar{L}_R \Phi^\dagger \ell_L \right) S + i \left(\frac{g'_{LR}{}^P}{\Lambda} \bar{\mathbb{L}}_L \Phi \gamma_5 \ell_R + \frac{g'_{RL}{}^P}{\Lambda} \bar{L}_R \gamma_5 \Phi^\dagger \ell_L \right) P \\ & + \left(g'_{LL}{}^V \bar{\mathbb{L}}_L \gamma^\mu \ell_L + g'_{RR}{}^V \bar{L}_R \gamma^\mu \ell_R \right) V_\mu + \left(g'_{LL}{}^A \bar{\mathbb{L}}_L \gamma^\mu \gamma_5 \ell_L + g'_{RR}{}^A \bar{L}_R \gamma^\mu \gamma_5 \ell_R \right) A_\mu \\ & + \left(\frac{g'_{LR}{}^T}{\Lambda} \bar{\mathbb{L}}_L \Phi \sigma^{\mu\nu} \ell_R + \frac{g'_{RL}{}^T}{\Lambda} \bar{L}_R \sigma^{\mu\nu} \Phi^\dagger \ell_L \right) B_{\mu\nu} + \text{h.c.}, \end{aligned}$$

$v \sim 246 \text{ GeV}$

$$\mathbb{L}_L(\ell_L) = \begin{pmatrix} \nu_L(\nu_L) \\ L_L(\ell_L) \end{pmatrix}$$

EFFECTIVE LAGRANGIANS

$$\mathcal{L}'_{int} = \left(\frac{g'_{LR}}{\Lambda} \bar{\mathbb{L}}_L \Phi \ell_R + \frac{g'_{RL}}{\Lambda} \bar{L}_R \Phi^\dagger \ell_{\mathbb{L}} \right) S + i \left(\frac{g'_{LR}}{\Lambda} \bar{\mathbb{L}}_L \Phi \gamma_5 \ell_R + \frac{g'_{RL}}{\Lambda} \bar{L}_R \gamma_5 \Phi^\dagger \ell_{\mathbb{L}} \right) P$$

$$+ \left(g'_{LL} \bar{\mathbb{L}}_L \gamma^\mu \ell_{\mathbb{L}} + g'_{RR} \bar{L}_R \gamma^\mu \ell_R \right) V_\mu + \left(g'_{LL} \bar{\mathbb{L}}_L \gamma^\mu \gamma_5 \ell_{\mathbb{L}} + g'_{RR} \bar{L}_R \gamma^\mu \gamma_5 \ell_R \right) A_\mu$$

$$+ \left(\frac{g'_{LR}}{\Lambda} \bar{\mathbb{L}}_L \Phi \sigma^{\mu\nu} \ell_R + \frac{g'_{RL}}{\Lambda} \bar{L}_R \sigma^{\mu\nu} \Phi^\dagger \ell_{\mathbb{L}} \right) B_{\mu\nu} + \text{h.c.},$$

$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + H \end{pmatrix},$
 $v \sim 246 \text{ GeV}$

$\mathbb{L}_L(\ell_{\mathbb{L}}) = \begin{pmatrix} \nu_L(\nu_L) \\ L_L(\ell_L) \end{pmatrix}$

SEWSB

$$\mathcal{L}'_{int} = \left(g'_{LR} \bar{L}_L \ell_R + g'_{RL} \bar{L}_R \ell_L \right) S \frac{v + H}{\sqrt{2}\Lambda}$$

$$+ i \left(g'_{LR} \bar{L}_L \gamma_5 \ell_R + g'_{RL} \bar{L}_R \gamma_5 \ell_L \right) P \frac{v + H}{\sqrt{2}\Lambda} + \left(g'_{LL} \bar{\nu}_L \gamma^\mu \nu_L \right) V_\mu + \left(g'_{LL} \bar{\nu}_L \gamma^\mu \gamma_5 \nu_L \right) A_\mu$$

$$+ \left(g'_{LL} \bar{L}_L \gamma^\mu \ell_L + g'_{RR} \bar{L}_R \gamma^\mu \ell_R \right) V_\mu + \left(g'_{LL} \bar{L}_L \gamma^\mu \gamma_5 \ell_L + g'_{RR} \bar{L}_R \gamma^\mu \gamma_5 \ell_R \right) A_\mu$$

$$+ \left(g'_{LR} \bar{L}_L \sigma^{\mu\nu} \ell_R + g'_{RL} \bar{L}_R \sigma^{\mu\nu} \ell_L \right) B_{\mu\nu} \frac{v + H}{\sqrt{2}\Lambda} + \text{h.c.}$$

EFFECTIVE LAGRANGIANS

$$\begin{aligned} \mathcal{L}'_{int} = & \left(g'_{LR}{}^S \bar{L}_L \ell_R + g'_{RL}{}^S \bar{L}_R \ell_L \right) S \frac{v+H}{\sqrt{2}\Lambda} \\ & + i \left(g'_{LR}{}^P \bar{L}_L \gamma_5 \ell_R + g'_{RL}{}^P \bar{L}_R \gamma_5 \ell_L \right) P \frac{v+H}{\sqrt{2}\Lambda} + \left(g'_{LL}{}^V \bar{\nu}_L \gamma^\mu \nu_L \right) V_\mu + \left(g'_{LL}{}^A \bar{\nu}_L \gamma^\mu \gamma_5 \nu_L \right) A_\mu \\ & + \left(g'_{LL}{}^V \bar{L}_L \gamma^\mu \ell_L + g'_{RR}{}^V \bar{L}_R \gamma^\mu \ell_R \right) V_\mu + \left(g'_{LL}{}^A \bar{L}_L \gamma^\mu \gamma_5 \ell_L + g'_{RR}{}^A \bar{L}_R \gamma^\mu \gamma_5 \ell_R \right) A_\mu \\ & + \left(g'_{LR}{}^T \bar{L}_L \sigma^{\mu\nu} \ell_R + g'_{RL}{}^T \bar{L}_R \sigma^{\mu\nu} \ell_L \right) B_{\mu\nu} \frac{v+H}{\sqrt{2}\Lambda} + \text{h.c.} \end{aligned}$$

$$\mathcal{L}_{int} = g_{L\ell}^S \bar{L} \ell S + i g_{L\ell}^P \bar{L} \gamma_5 \ell P + g_{L\ell}^V \bar{L} \gamma^\mu \ell V_\mu + g_{L\ell}^A \bar{L} \gamma^\mu \gamma_5 \ell A_\mu + g_{L\ell}^T \bar{L} \sigma^{\mu\nu} \ell B_{\mu\nu} + \text{h.c.},$$

EFFECTIVE LAGRANGIANS

$$\mathcal{L}'_{int} = \left(g'_{LR}{}^S \bar{L}_L \ell_R + g'_{RL}{}^S \bar{L}_R \ell_L \right) S \frac{v+H}{\sqrt{2}\Lambda} \\ + i \left(g'_{LR}{}^P \bar{L}_L \gamma_5 \ell_R + g'_{RL}{}^P \bar{L}_R \gamma_5 \ell_L \right) P \frac{v+H}{\sqrt{2}\Lambda} + \left(g'_{LL}{}^V \bar{\nu}_L \gamma^\mu \nu_L \right) V_\mu + \left(g'_{LL}{}^A \bar{\nu}_L \gamma^\mu \gamma_5 \nu_L \right) A_\mu \\ + \left(g'_{LL}{}^V \bar{L}_L \gamma^\mu \ell_L + g'_{RR}{}^V \bar{L}_R \gamma^\mu \ell_R \right) V_\mu + \left(g'_{LL}{}^A \bar{L}_L \gamma^\mu \gamma_5 \ell_L + g'_{RR}{}^A \bar{L}_R \gamma^\mu \gamma_5 \ell_R \right) A_\mu \\ + \left(g'_{LR}{}^T \bar{L}_L \sigma^{\mu\nu} \ell_R + g'_{RL}{}^T \bar{L}_R \sigma^{\mu\nu} \ell_L \right) B_{\mu\nu} \frac{v+H}{\sqrt{2}\Lambda} + \text{h.c.}$$

$$\mathcal{L}_{int} = g_{L\ell}^S \bar{L} \ell S + i g_{L\ell}^P \bar{L} \gamma_5 \ell P + g_{L\ell}^V \bar{L} \gamma^\mu \ell V_\mu + g_{L\ell}^A \bar{L} \gamma^\mu \gamma_5 \ell A_\mu + g_{L\ell}^T \bar{L} \sigma^{\mu\nu} \ell B_{\mu\nu} + \text{h.c.},$$

If we **IMPOSE**

- $g'_{LR}{}^{(S,P,T)} = g'_{RL}{}^{(S,P,T)} \equiv g'_{L\ell}{}^{(S,P,T)},$
- $g'_{LL}{}^{(V,A)} = g'_{RR}{}^{(V,A)} \equiv g'_{L\ell}{}^{(V,A)},$

EFFECTIVE LAGRANGIANS

$$\mathcal{L}'_{int} = \left(g'_{LR}{}^S \bar{L}_L \ell_R + g'_{RL}{}^S \bar{L}_R \ell_L \right) S \frac{v+H}{\sqrt{2}\Lambda} \\ + i \left(g'_{LR}{}^P \bar{L}_L \gamma_5 \ell_R + g'_{RL}{}^P \bar{L}_R \gamma_5 \ell_L \right) P \frac{v+H}{\sqrt{2}\Lambda} + \left(g'_{LL}{}^V \bar{\nu}_L \gamma^\mu \nu_L \right) V_\mu + \left(g'_{LL}{}^A \bar{\nu}_L \gamma^\mu \gamma_5 \nu_L \right) A_\mu \\ + \left(g'_{LL}{}^V \bar{L}_L \gamma^\mu \ell_L + g'_{RR}{}^V \bar{L}_R \gamma^\mu \ell_R \right) V_\mu + \left(g'_{LL}{}^A \bar{L}_L \gamma^\mu \gamma_5 \ell_L + g'_{RR}{}^A \bar{L}_R \gamma^\mu \gamma_5 \ell_R \right) A_\mu \\ + \left(g'_{LR}{}^T \bar{L}_L \sigma^{\mu\nu} \ell_R + g'_{RL}{}^T \bar{L}_R \sigma^{\mu\nu} \ell_L \right) B_{\mu\nu} \frac{v+H}{\sqrt{2}\Lambda} + \text{h.c.}$$

$$\mathcal{L}_{int} = g_{L\ell}^S \bar{L} \ell S + i g_{L\ell}^P \bar{L} \gamma_5 \ell P + g_{L\ell}^V \bar{L} \gamma^\mu \ell V_\mu + g_{L\ell}^A \bar{L} \gamma^\mu \gamma_5 \ell A_\mu + g_{L\ell}^T \bar{L} \sigma^{\mu\nu} \ell B_{\mu\nu} + \text{h.c.},$$

If we **IMPOSE**

- $g'_{LR}{}^{(S,P,T)} = g'_{RL}{}^{(S,P,T)} \equiv g_{L\ell}{}^{(S,P,T)}$, \mathcal{L}'_{int} includes the interactions of \mathcal{L}_{int} provided
- $g'_{LL}{}^{(V,A)} = g'_{RR}{}^{(V,A)} \equiv g_{L\ell}{}^{(V,A)}$

$$g_{L\ell}^{(V,A)} \equiv g_{L\ell}'^{(V,A)}$$

$$g_{L\ell}^{(S,P,T)} \equiv \frac{g_{L\ell}'^{(S,P,T)} v}{\sqrt{2}\Lambda}$$

EFFECTIVE LAGRANGIANS

$\chi = S, P, V, A, B_{\mu\nu}$

$$\mathcal{L}'_{int} = \left(g'_{LR}{}^S \bar{L}_L \ell_R + g'_{RL}{}^S \bar{L}_R \ell_L \right) S \frac{v+H}{\sqrt{2}\Lambda} + i \left(g'_{LR}{}^P \bar{L}_L \gamma_5 \ell_R + g'_{RL}{}^P \bar{L}_R \gamma_5 \ell_L \right) P \frac{v+H}{\sqrt{2}\Lambda} + \left(g'_{LL}{}^V \bar{\nu}_L \gamma^\mu \nu_L \right) V_\mu + \left(g'_{LL}{}^A \bar{\nu}_L \gamma^\mu \gamma_5 \nu_L \right) A_\mu + \left(g'_{LL}{}^V \bar{L}_L \gamma^\mu \ell_L + g'_{RR}{}^V \bar{L}_R \gamma^\mu \ell_R \right) V_\mu + \left(g'_{LL}{}^A \bar{L}_L \gamma^\mu \gamma_5 \ell_L + g'_{RR}{}^A \bar{L}_R \gamma^\mu \gamma_5 \ell_R \right) A_\mu + \left(g'_{LR}{}^T \bar{L}_L \sigma^{\mu\nu} \ell_R + g'_{RL}{}^T \bar{L}_R \sigma^{\mu\nu} \ell_L \right) B_{\mu\nu} \frac{v+H}{\sqrt{2}\Lambda} + \text{h.c.}$$

New interactions of the Higgs field with $L\ell\chi$ (and with ν_S)

$$\mathcal{L}_{int} = g_{L\ell}^S \bar{L} \ell S + i g_{L\ell}^P \bar{L} \gamma_5 \ell P + g_{L\ell}^V \bar{L} \gamma^\mu \ell V_\mu + g_{L\ell}^A \bar{L} \gamma^\mu \gamma_5 \ell A_\mu + g_{L\ell}^T \bar{L} \sigma^{\mu\nu} \ell B_{\mu\nu} + \text{h.c.},$$

If we **IMPOSE**

- $g'_{LR}{}^{(S,P,T)} = g'_{RL}{}^{(S,P,T)} \equiv g'_{L\ell}{}^{(S,P,T)}$, \mathcal{L}'_{int} includes the interactions of \mathcal{L}_{int} provided
- $g'_{LL}{}^{(V,A)} = g'_{RR}{}^{(V,A)} \equiv g'_{L\ell}{}^{(V,A)}$

$$g_{L\ell}^{(V,A)} \equiv g'_{L\ell}{}^{(V,A)}$$

$$g_{L\ell}^{(S,P,T)} \equiv \frac{g'_{L\ell}{}^{(S,P,T)} v}{\sqrt{2}\Lambda}$$

Effective LFV interactions involving a boson (χ)

Pablo Roig (Cinvestav)

EFFECTIVE LAGRANGIANS

$\chi = S, P, V, A, B_{\mu\nu}$

$$\mathcal{L}'_{int} = \left(g'_{LR}{}^S \bar{L}_L \ell_R + g'_{RL}{}^S \bar{L}_R \ell_L \right) S \frac{v+H}{\sqrt{2}\Lambda} \quad \xrightarrow{\text{New interactions of the Higgs field with } L\ell\chi \text{ (and with } \nu\text{)}} \quad$$

$$+ i \left(g'_{LR}{}^P \bar{L}_L \gamma_5 \ell_R + g'_{RL}{}^P \bar{L}_R \gamma_5 \ell_L \right) P \frac{v+H}{\sqrt{2}\Lambda} + \left(g'_{LL}{}^V \bar{\nu}_L \gamma^\mu \nu_L \right) V_\mu + \left(g'_{LL}{}^A \bar{\nu}_L \gamma^\mu \gamma_5 \nu_L \right) A_\mu$$

$$+ \left(g'_{LL}{}^V \bar{L}_L \gamma^\mu \ell_L + g'_{RR}{}^V \bar{L}_R \gamma^\mu \ell_R \right) V_\mu + \left(g'_{LL}{}^A \bar{L}_L \gamma^\mu \gamma_5 \ell_L + g'_{RR}{}^A \bar{L}_R \gamma^\mu \gamma_5 \ell_R \right) A_\mu$$

$$+ \left(g'_{LR}{}^T \bar{L}_L \sigma^{\mu\nu} \ell_R + g'_{RL}{}^T \bar{L}_R \sigma^{\mu\nu} \ell_L \right) B_{\mu\nu} \frac{v+H}{\sqrt{2}\Lambda} + \text{h.c.}$$

$$\mathcal{L}_{int} = g_{L\ell}^S \bar{L} \ell S + i g_{L\ell}^P \bar{L} \gamma_5 \ell P + g_{L\ell}^V \bar{L} \gamma^\mu \ell V_\mu + g_{L\ell}^A \bar{L} \gamma^\mu \gamma_5 \ell A_\mu + g_{L\ell}^T \bar{L} \sigma^{\mu\nu} \ell B_{\mu\nu} + \text{h.c.},$$

If we **IMPOSE**

- $g'_{LR}{}^{(S,P,T)} = g'_{RL}{}^{(S,P,T)} \equiv g'_{L\ell}{}^{(S,P,T)}$, \mathcal{L}'_{int} includes the interactions of \mathcal{L}_{int} provided
- $g'_{LL}{}^{(V,A)} = g'_{RR}{}^{(V,A)} \equiv g'_{L\ell}{}^{(V,A)}$

$$g_{L\ell}^{(V,A)} \equiv g'_{L\ell}{}^{(V,A)}$$

$$g_{L\ell}^{(S,P,T)} \equiv \frac{g'_{L\ell}{}^{(S,P,T)} v}{\sqrt{2}\Lambda} \quad \text{Small!}$$

Effective LFV interactions involving a boson (χ)

Pablo Roig (Cinvestav)

MOTIVATION: Why effective LFV for $L \rightarrow l \chi$?

Effective Lagrangians offer the most general description of Physics that has not been resolved yet.

Specific BSM models are given realizations of them. **For instance:**

Invisible **axions** are pGbs accounting for the smallness of $\bar{\theta}$ & are viable with a large PQ SB scale.
They can be DM candidates & linked to the smallness of ν masses.

MOTIVATION: Why effective LFV for $L \rightarrow l \chi$?

Effective Lagrangians offer the most general description of Physics that has not been resolved yet.

Specific BSM models are given realizations of them. For instance:

Invisible **axions** are pGbs accounting for the smallness of $\bar{\theta}$ & are viable with a large PQ SB scale.
They can be DM candidates & linked to the smallness of ν masses.

Their couplings $\mathcal{L}_f = \frac{1}{F} \partial_\mu f^a J^{\mu a}$ can be written as our $\chi=P$ interactions
(also of S-type)

MOTIVATION: Why effective LFV for $L \rightarrow l \chi$?

Effective Lagrangians offer the most general description of Physics that has not been resolved yet.

Specific BSM models are given realizations of them. For instance:

Invisible **axions** are pGbs accounting for the smallness of $\bar{\theta}$ & are viable with a large PQ SB scale.
They can be DM candidates & linked to the smallness of ν masses.

Their couplings $\mathcal{L}_f = \frac{1}{F} \partial_\mu f^a J^{\mu a}$ can be written as our $\chi=P$ interactions
(also of S-type)
(on-shell fermions)

$$J^{\mu a} = \bar{\psi}_i \gamma^\mu (g_V + g_A \gamma_5) T_{ij}^a \psi_j$$

\downarrow

$$\mathcal{L}_f = -\frac{i}{F} f^a \bar{\psi}_i [g_V(m_i - m_j) + g_A(m_i + m_j) \gamma_5] T_{ij}^a \psi_j$$

MOTIVATION: Why effective LFV for $L \rightarrow l \chi$?

Effective Lagrangians offer the most general description of Physics that has not been resolved yet.

Specific BSM models are given realizations of them. For instance:

Invisible **axions** are pGBs accounting for the smallness of $\bar{\theta}$ & are viable with a large PQ SB scale.
They can be DM candidates & linked to the smallness of ν masses.

Their couplings $\mathcal{L}_f = \frac{1}{F} \partial_\mu f^a J^{\mu a}$ can be written as our $\chi=P$ interactions
(also of S-type)

If the breaking of LN is spontaneous, the corresponding pGB is the **Majoron/familon**

MOTIVATION: Why effective LFV for $L \rightarrow l \chi$?

Effective Lagrangians offer the most general description of Physics that has not been resolved yet.

Specific BSM models are given realizations of them. For instance:

Invisible **axions** are pGBs accounting for the smallness of $\bar{\theta}$ & are viable with a large PQ SB scale.
They can be DM candidates & linked to the smallness of ν masses.

Their couplings $\mathcal{L}_f = \frac{1}{F} \partial_\mu f^a J^{\mu a}$ can be written as our $\chi=P$ interactions
(also of S-type)

If the breaking of LN is spontaneous, the corresponding pGB is the **Majoron/familon**

Z' (with gauged flavor symmetry, for instance), that can explain LU anomalies, can fall into our description of $\chi=A/V$

MOTIVATION: Why effective LFV for $L \rightarrow l \chi$?

Effective Lagrangians offer the most general description of Physics that has not been resolved yet.

Specific BSM models are given realizations of them. For instance:

Invisible axions are pGBs accounting for the smallness of $\bar{\theta}$ & are viable with a large PQ SB scale.
They can be DM candidates & linked to the smallness of ν masses.

Their couplings $\mathcal{L}_f = \frac{1}{F} \partial_\mu f^a J^{\mu a}$ can be written as our $\chi=P$ interactions
(also of S-type)

If the breaking of LN is spontaneous, the corresponding pGB is the **Majoron/familon**

Z' (with gauged flavor symmetry, for instance), that can explain LU anomalies, can fall into our description of $\chi=A/V$

Any χ can also be the **mediator of SM-DM interactions**

...

(Refs. will be given in the proceedings)

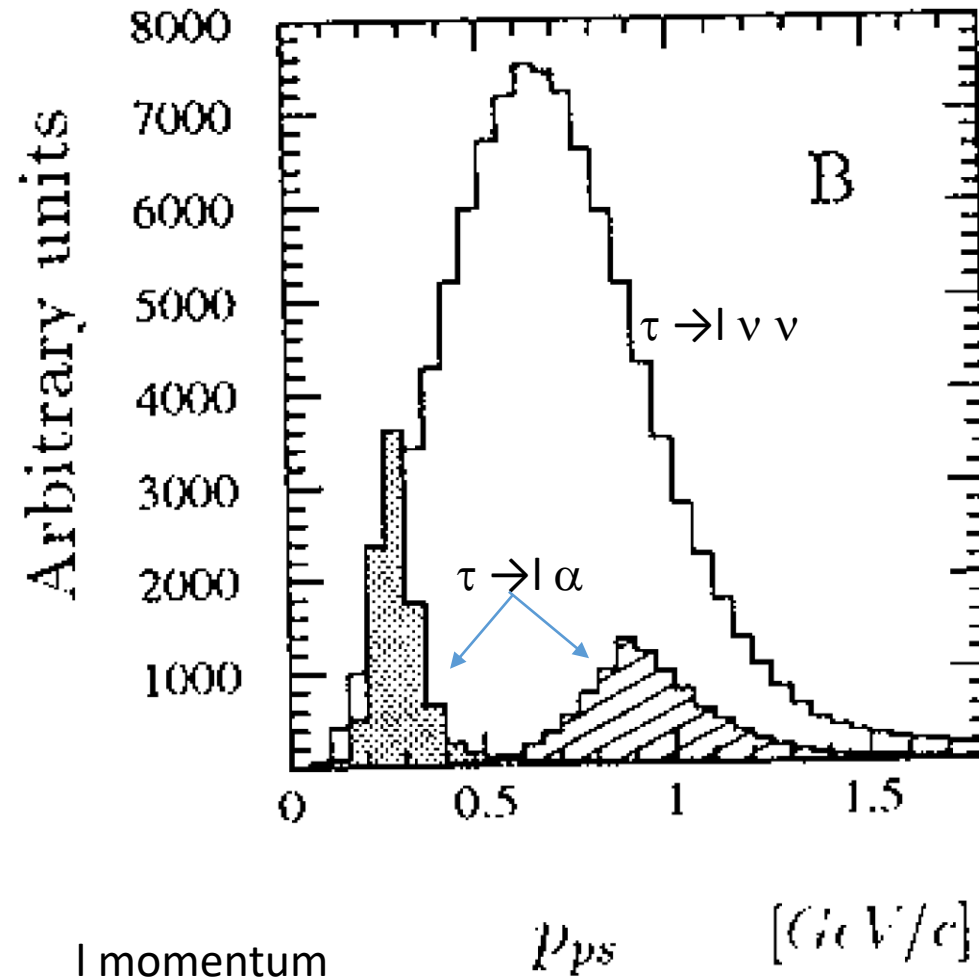
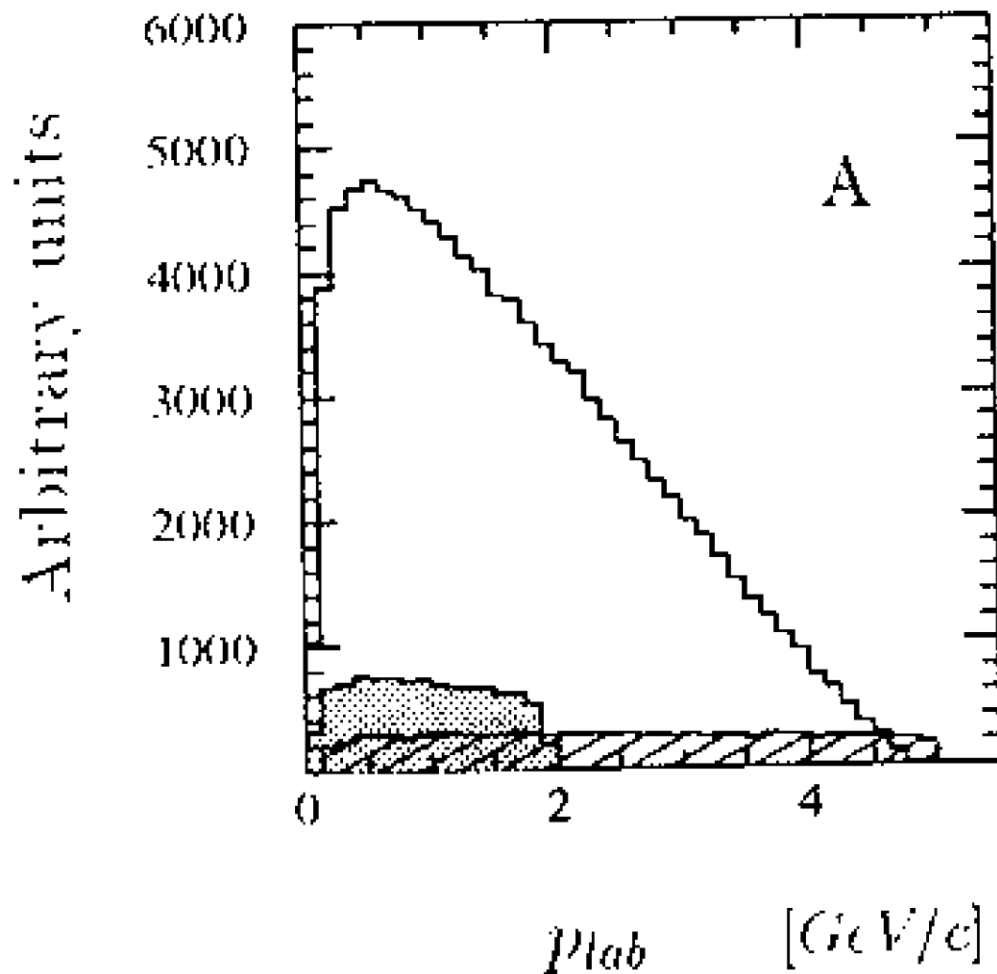
PHENOMENOLOGY

I restrict here to the decaying particle rest frame (not B-Factory environment)

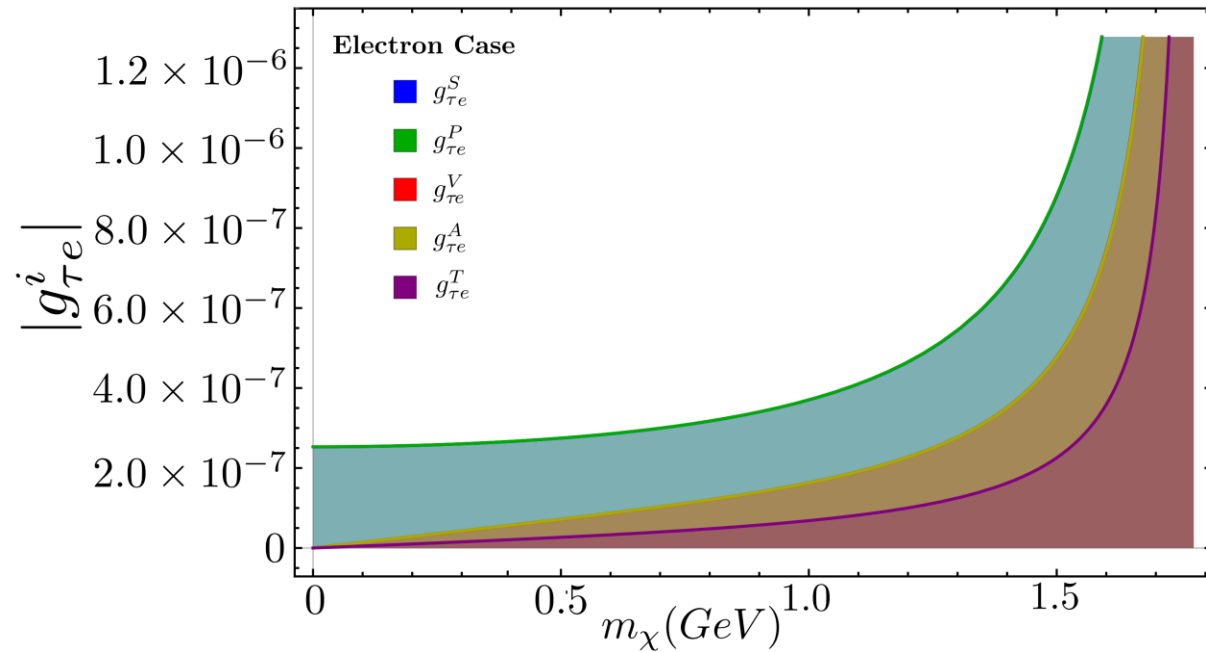
PHENOMENOLOGY

Work in progress

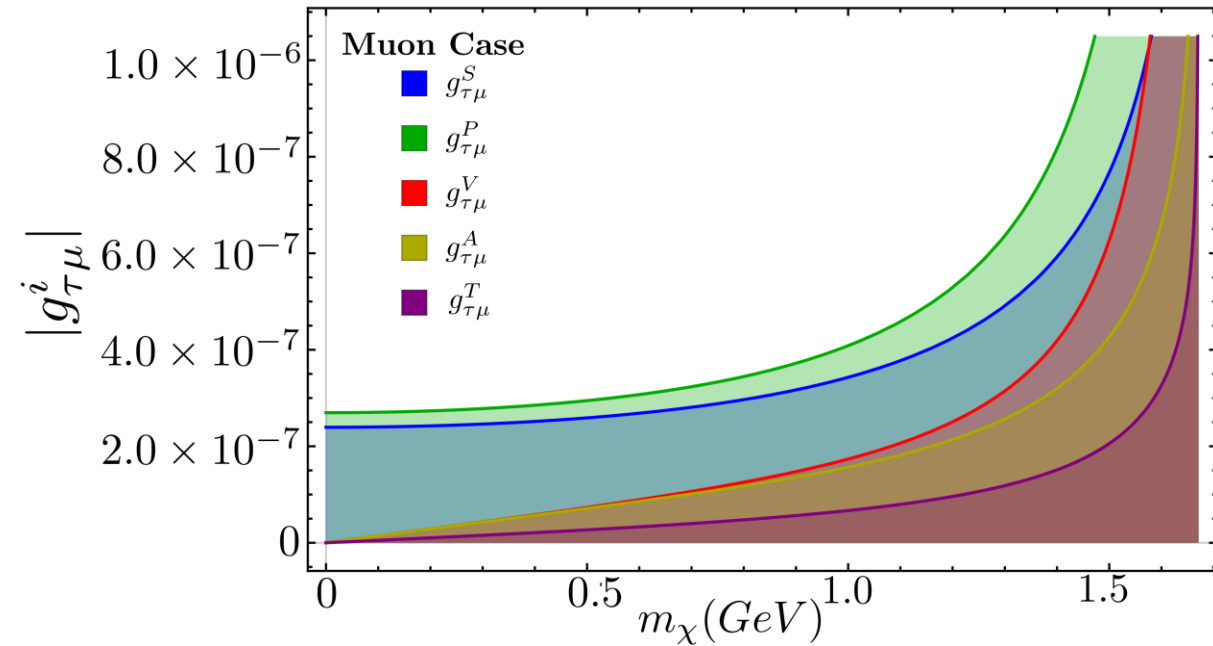
I restrict here to the decaying particle rest frame (not B-Factory environment)



PHENOMENOLOGY: $\tau \rightarrow l \chi$



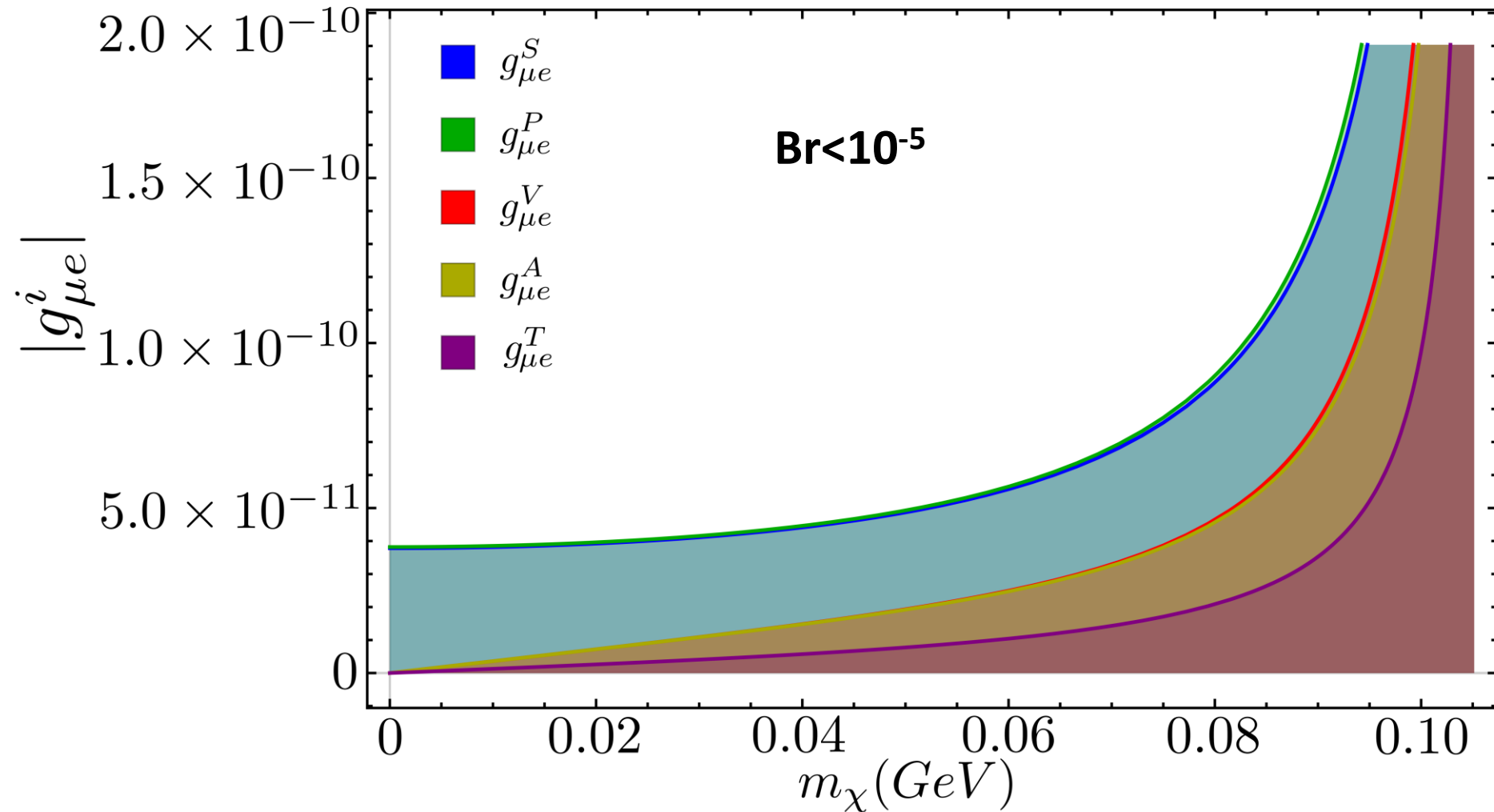
(a) $|g_{\tau e}^i|$ constraints for $\mathcal{B}r \sim 10^{-3}$ as a function of m_χ .



(b) $|g_{\tau \mu}^i|$ constraints for $\mathcal{B}r \sim 10^{-3}$ as a function of m_χ .

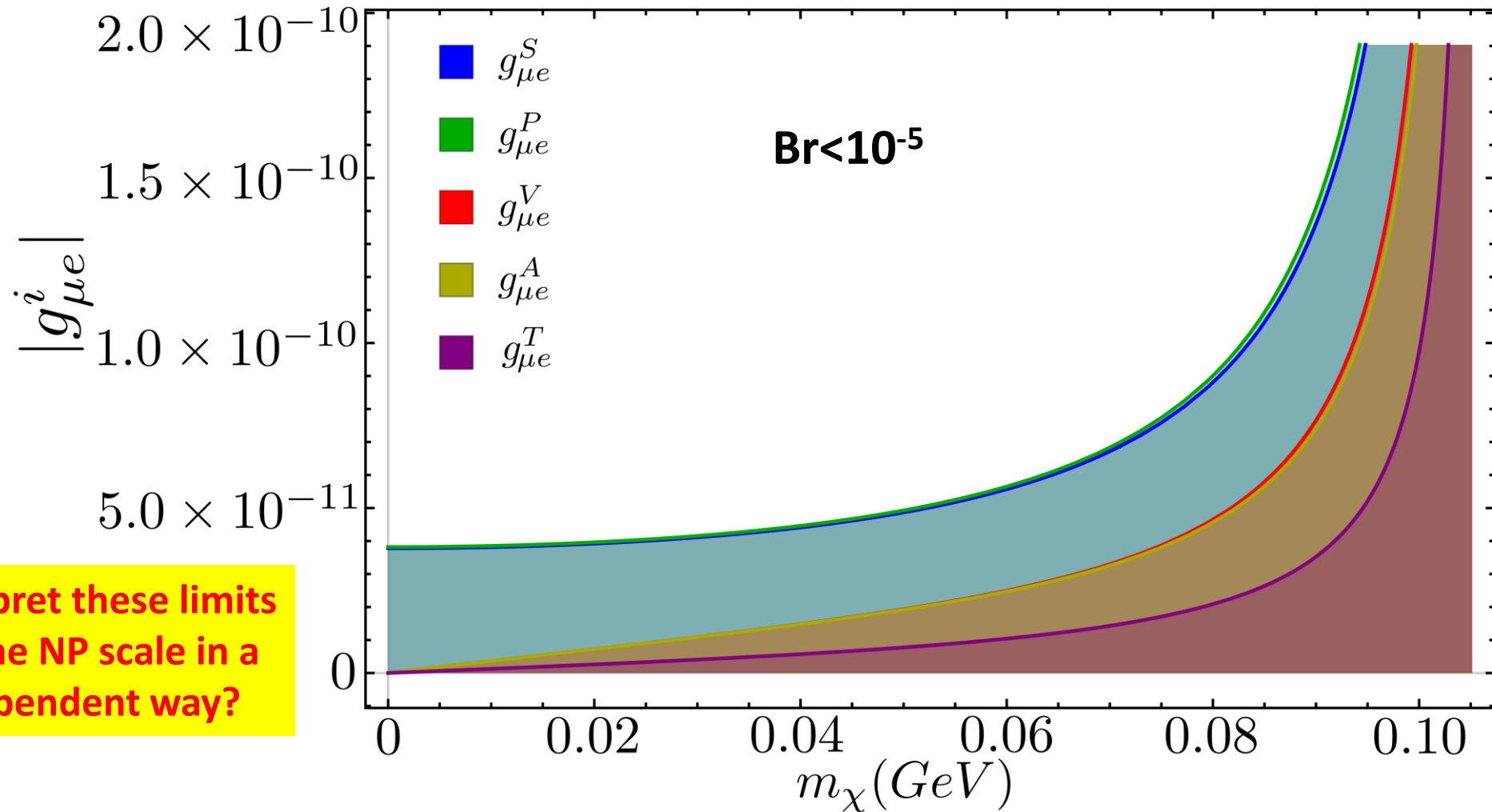
For $\mathcal{B}r < 10^{-9}$ (Belle-II reach) UL on coupling is three orders of magnitude smaller than shown

PHENOMENOLOGY: $\mu \rightarrow e \chi$



For $Br < 10^{-13}$ (MEG reach) UL on coupling is four orders of magnitude smaller than shown

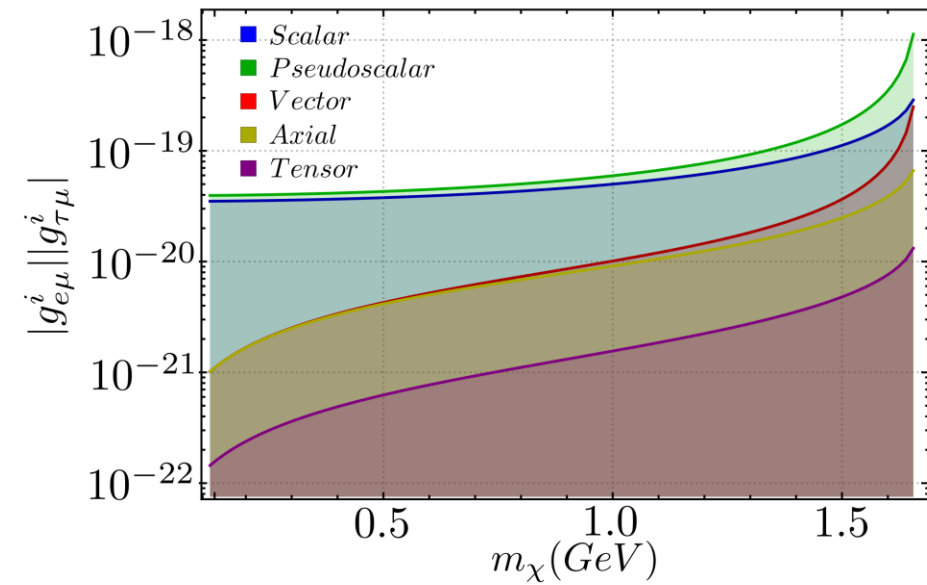
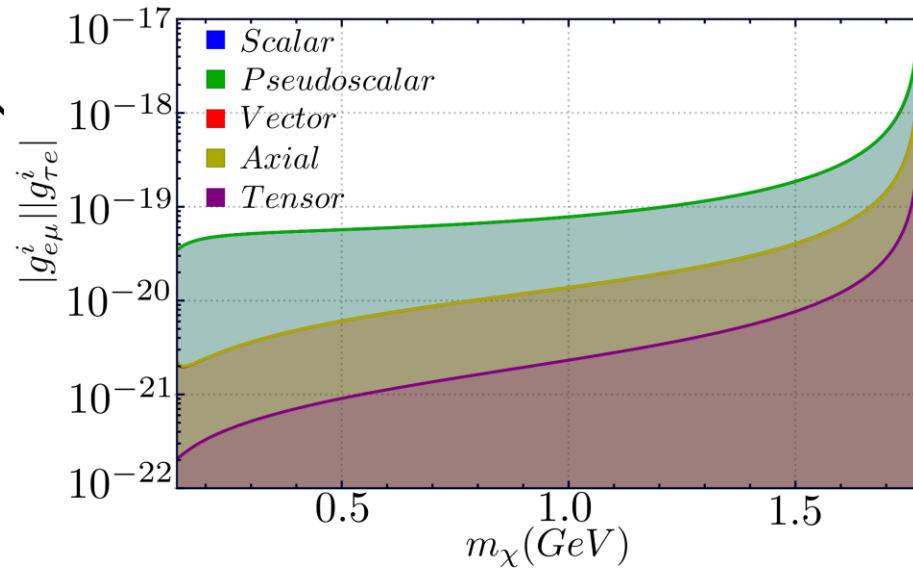
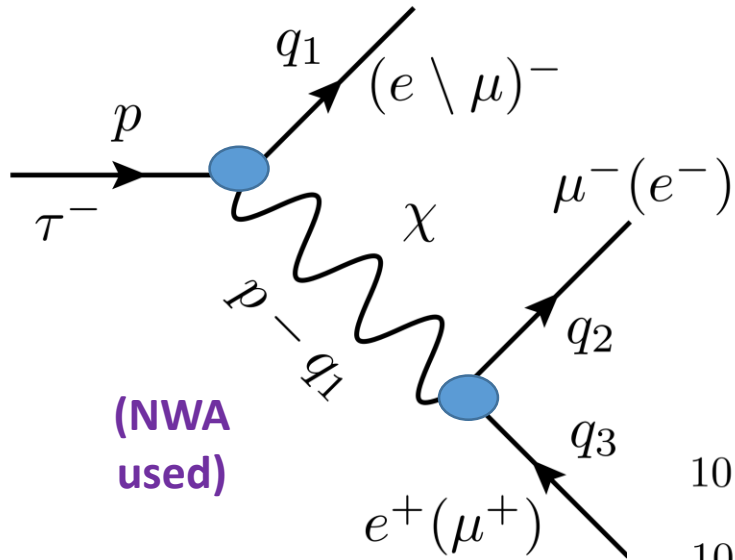
PHENOMENOLOGY: $\mu \rightarrow e \chi$



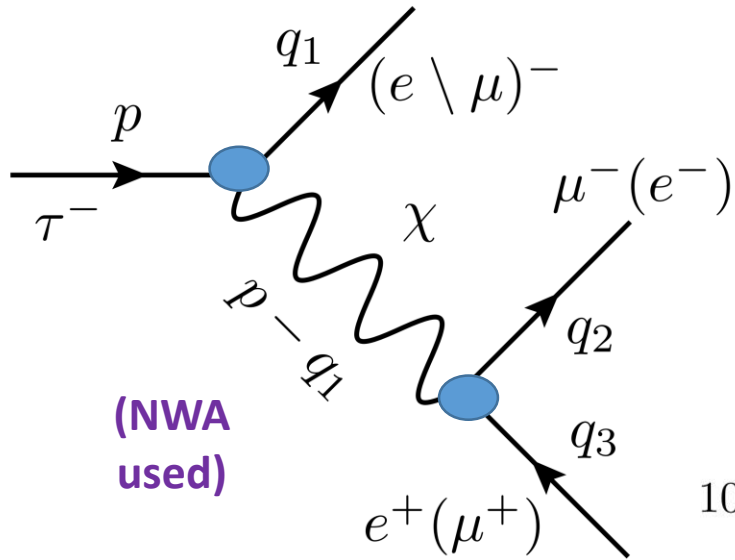
Can one interpret these limits
in terms of the NP scale in a
model-independent way?

For $Br < 10^{-13}$ (MEG reach) UL on coupling is four orders of magnitude smaller than shown

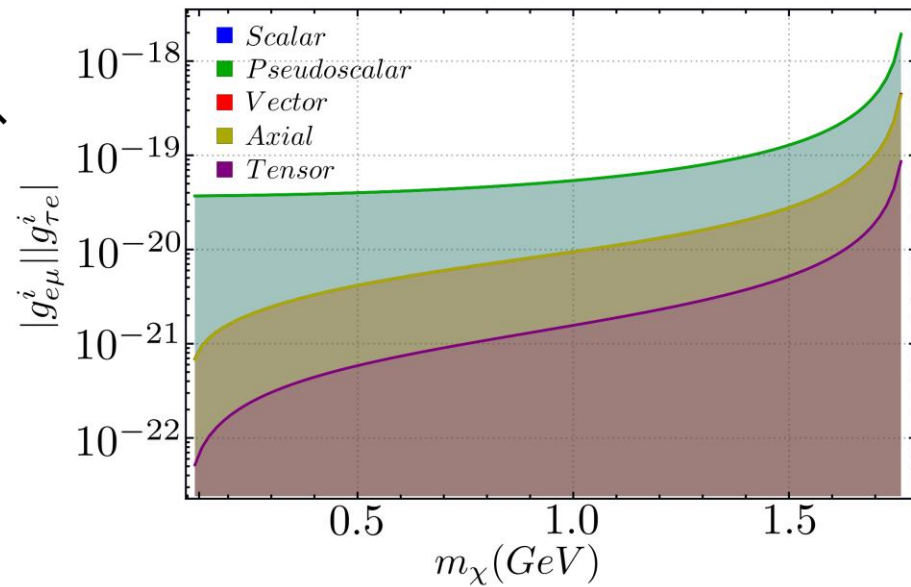
PHENOMENOLOGY: $\tau \rightarrow 3l$



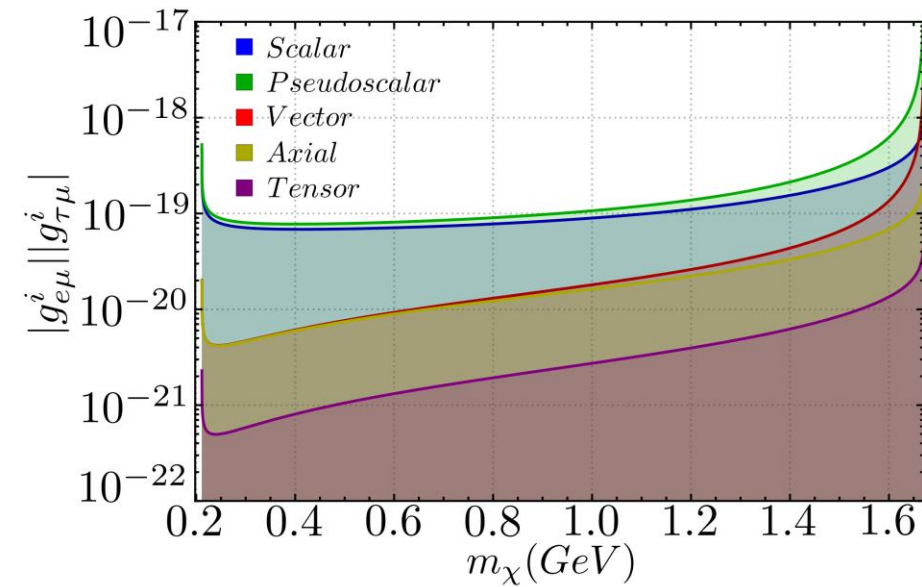
PHENOMENOLOGY: $\tau \rightarrow 3l$



These limits imply $\text{BR}(\tau \rightarrow l \chi) < 10^{-7}$, which supersedes the ARGUS bound:
BaBar & Belle(-II) should not only improve that bound
but reach similar ULs to other LFV decays



(c) $\tau^- \rightarrow e^- e^- \mu^+$



(d) $\tau^- \rightarrow \mu^- e^- \mu^+$

Effective LFV interactions involving a boson (χ)

Pablo Roig (Cinvestav)

PHENOMENOLOGY: What if $SU(2)_L \times U(1)_Y$?

Then we have LFV processes involving H (with $\chi=S,P,B_{\mu\nu}$) & ν s (with $\chi=V,A$)

PHENOMENOLOGY: What if $SU(2)_L \times U(1)_Y$?

Then we have LFV processes involving H (with $\chi=S,P,B_{\mu\nu}$) & ν s (with $\chi=V,A$)

S or P

$$\mathcal{Br}(H \rightarrow \tau^+ \mu^- \chi) \lesssim 1 \times 10^{-18}, \mathcal{Br}(H \rightarrow \tau^+ e^- \chi) \lesssim 2 \times 10^{-18}, \mathcal{Br}(H \rightarrow \mu^+ e^- \chi) \lesssim 3 \times 10^{-22}$$

$B_{\mu\nu}$

$$\mathcal{Br}(H \rightarrow \tau^+ \ell^- \chi) \lesssim 2.5 \times 10^{-14}, \mathcal{Br}(H \rightarrow \mu^+ e^- \chi) \lesssim 5 \times 10^{-18}$$

$\chi \rightarrow \nu_L N_L$ are unmeasurably small

PHENOMENOLOGY: What if $SU(2)_L \times U(1)_Y$?

Then we have LFV processes involving H (with $\chi=S,P,B_{\mu\nu}$) & ν s (with $\chi=V,A$)

S or P

$$\mathcal{Br}(H \rightarrow \tau^+ \mu^- \chi) \lesssim 1 \times 10^{-18}, \mathcal{Br}(H \rightarrow \tau^+ e^- \chi) \lesssim 2 \times 10^{-18}, \mathcal{Br}(H \rightarrow \mu^+ e^- \chi) \lesssim 3 \times 10^{-22}$$

$B_{\mu\nu}$

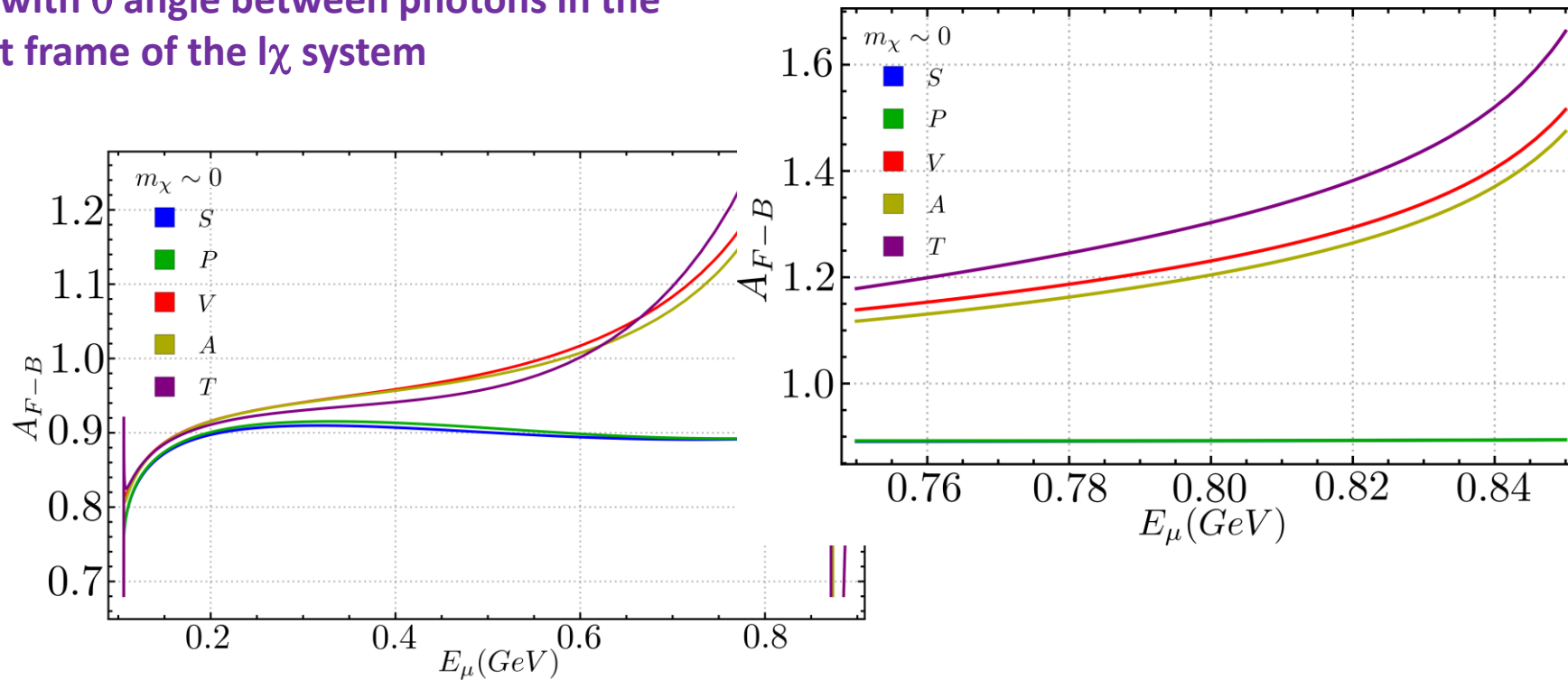
$$\mathcal{Br}(H \rightarrow \tau^+ \ell^- \chi) \lesssim 2.5 \times 10^{-14}, \mathcal{Br}(H \rightarrow \mu^+ e^- \chi) \lesssim 5 \times 10^{-18}$$

$\chi \rightarrow \nu_L N_L$ are unmeasurably small

But, what if we have a heavy χ instead?

PHENOMENOLOGY: Lessons from $L \rightarrow l \chi \gamma$

'FB' asymmetry with θ angle between photons in the rest frame of the $l\chi$ system

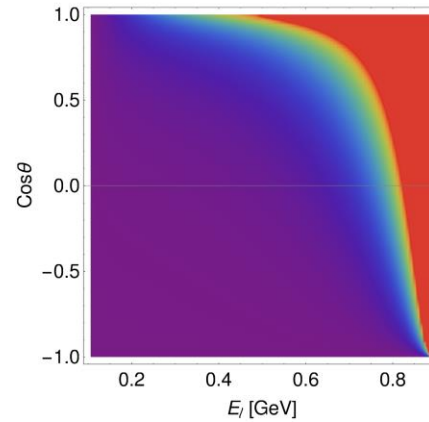


Spin 0 (S, P) & Spin 1 cases (V, A, T) could be disentangled easily.

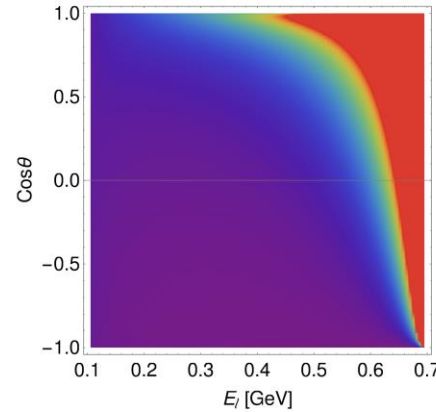
PHENOMENOLOGY: Lessons from $L \rightarrow l \chi \gamma$

Dalitz plot distributions

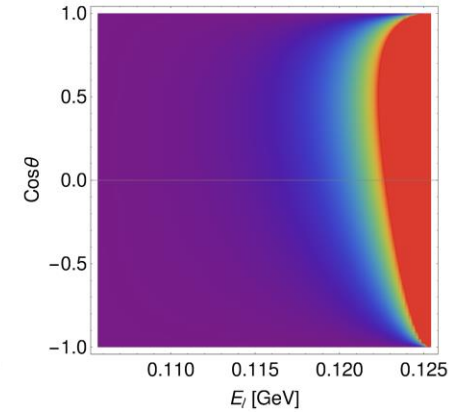
Spin 0 cases (S,P)
are pretty similar.



(a) SC, $m_\chi \sim 0$

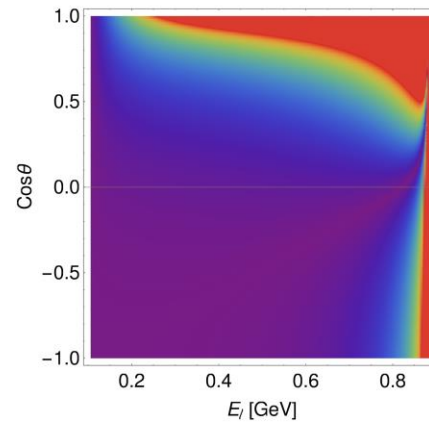


(b) SC, $m_\chi = \frac{M_\tau - m_\mu}{2}$

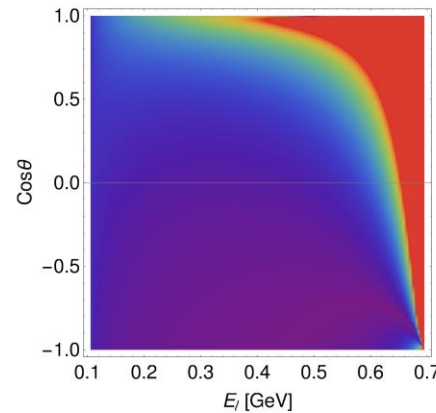


(c) SC, $m_\chi \sim M_\tau - m_\mu$

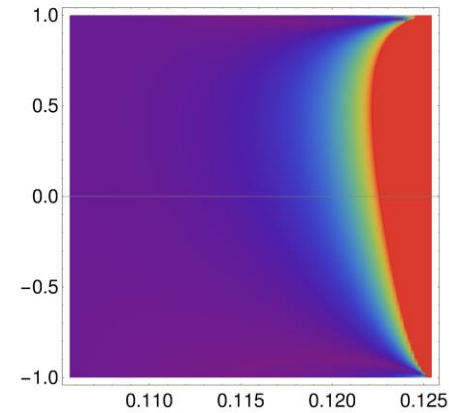
Spin 1 cases (V,A,B)
look very alike.



(d) VC, $m_\chi \sim 0$



(e) VC, $m_\chi = \frac{M_\tau - m_\mu}{2}$



(f) VC, $m_\chi \sim M_\tau - m_\mu$

Effective LFV interactions involving a boson (χ)

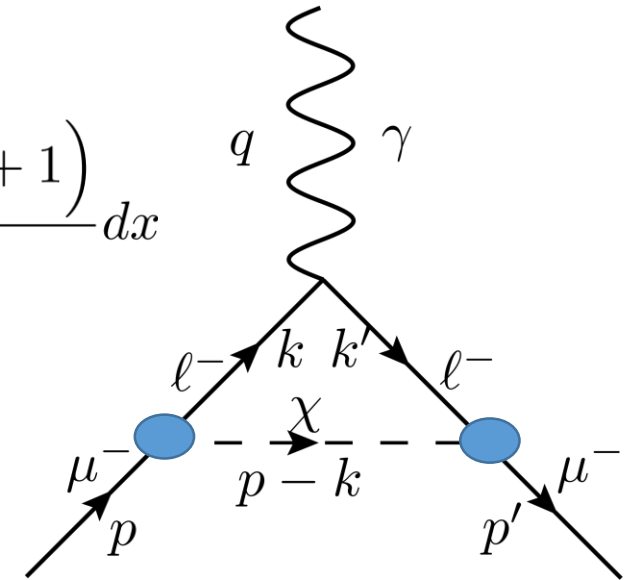
Pablo Roig (Cinvestav)

PHENOMENOLOGY: Effects on a_l are too small

$$\Delta a_\mu = a_\mu^{Exp} - a_\mu^{SM} = 268(63)_{exp}(43)_{theo} \times 10^{-11}, \quad \Delta a_e = a_e^{Exp} - a_e^{SM} = -87(36)_{exp} \times 10^{-14}$$

$$\Delta a_\mu^B = (g_{\mu\ell}^T)^2 \frac{2m_\mu^2}{\pi^2 m_\chi^2} \int_0^1 \frac{2\frac{m_\ell}{m_\mu}(x-1)(3x+1) + \frac{m_\mu^2}{m_\chi^2}(x-1)^3 \left(x - \frac{m_\ell}{m_\mu}\right) \left(x - 2\frac{m_\ell}{m_\mu} + 1\right)}{(1-x) \left(\frac{m_\ell^2}{m_\chi^2} - \frac{m_\mu^2}{m_\chi^2}x\right) + x} dx$$

(Apparently this type of contribution was not computed before)



The largest contribution to a_μ (a_e) that we get is $\lesssim 10^{-13}$ ($\lesssim 10^{-16}$) for small m_χ and the spin-zero cases, so it is clear that it is impossible that the LFV interactions considered in this work provide any solutions for such large discrepancies as currently reported in a_ℓ .

Effective LFV interactions involving a boson (χ)

Pablo Roig (Cinvestav)

CONCLUSIONS

It is interesting to consider LFV+boson with effective Lagrangians: experimentally & theoretically (B- & τ -c factories)

CONCLUSIONS

It is interesting to consider LFV+boson with effective Lagrangians: experimentally & theoretically (B- & τ -c factories)

If discovered, it would be easy to find out χ spin, but not parity

CONCLUSIONS

It is interesting to consider LFV+boson with effective Lagrangians: experimentally & theoretically (B- & τ -c factories)

If discovered, it would be easy to find out χ spin, but not parity

In case there is an underlying EW symmetry χ interactions with H & ν s would be out of reach

CONCLUSIONS

It is interesting to consider LFV+boson with effective Lagrangians: experimentally & theoretically (B- & τ -c factories)

If discovered, it would be easy to find out χ spin, but not parity

In case there is an underlying EW symmetry χ interactions with H & ν s would be out of reach

Irrelevant contributions to a_μ

CONCLUSIONS

It is interesting to consider LFV+boson with effective Lagrangians: experimentally & theoretically (B- & τ -c factories)

If discovered, it would be easy to find out χ spin, but not parity

In case there is an underlying EW symmetry χ interactions with H & ν s would be out of reach

Irrelevant contributions to a_μ

Can we interpret our impressive bounds on the χ couplings in terms of a LARGE NP scale model-independently?