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Leitmotif and Outline



The discovery of the Higgs particle WITH LOW MASS calls naturally for

a HIGGS FACTORY - a circular e⁺e⁻ collider of 240 GeV (only 15% higher than the 209 GeV at LEP2).

The new, big accelerator tunnel will be ideal to host a future pp collider.

- 1. Future Circular Collider (FCC-ee) at CERN
- 2. Circular (Chinese) Electron Positron Collider (CEPC)
- 3. Physics at future circular colliders (with selected topics, studied in Kraków)

Key Physics Explorations for Future e⁺e⁻ Colliders



- Precise measurements of the Higgs(-es) properties (mass, width, spin, couplings, CP violation...).
- ✓ Precise determination of the Top properties (studies at threshold).

✓ W and Z physics (vector boson pair production, TGCs).

- ✓ Precise studies of electroweak observables.
- ✓ Studies of two-fermion processes (Z', quark and lepton compositness, extra dimensions...) and four-fermion final states.
- \checkmark Searches for new particles.

 \checkmark





FCC - Future Circular Collider

- FCC international collaboration aiming at the study of:
- ✓ p-p collider: FCC-hh flagship
- ✓ e⁻-e⁺ collider: FCC-ee intermediate step, preceding the FCC-pp
- ✓ e-p collider: FCC-he additional option

- 80-100 km infrastructure in Geneva area
- Goal: CDR and cost review by 2018





 ε_{v} (pm)

L (10³⁴ cm⁻²s⁻¹)/IP

Statistics (4 expts)

ξγ

FCC-ee - Future Circular Collider



$\Delta M_Z = 100 \text{ keV} \qquad \Delta M_W = 500 \text{ keV} \qquad \text{(LEP: } \Delta M_Z = 2 \text{ MeV} \Delta M_W = 50 \text{ MeV}\text{)}$					
Two rings; four interaction points; flat beams; non-zero crossing angle Five working points: $\sqrt{s} = M_Z$ $\sqrt{s} = M(WW)$ $\sqrt{s} = M(ZH)$ $\sqrt{s} = M(t\bar{t})$ $\sqrt{s} = 400$ GeV					
Parameter	FCC-Z	FCC-WW	FCC-ZH	FCC-tt	LEP2
E (GeV)	45	80	120	175	104
I (mA)	1400	152	30	7	4
No. bunches	16 700	4 490	1 330	98	4
Energy loss/turn [GeV]	0.03		1.67	7.55	3.34
Synchrotron power [MW]	100	100	100	100	22
RF Voltage [GV]	0.3-2.5		3.6-5.5	11	3.5
β* _{x/y} (mm)	500 / 1	500 / 1	500 / 1	1000 / 1	1500 / 50
ε_{x} (nm)	29	3.3	1	2	30-50

7

0.06

12

10⁸ WW / 1yr

 $2.1 \times 10^{31} \text{ cm}^{-2} \text{s}^{-1}$

60

0.03

28

10¹² Z / 2yrs

New e+e- *Circular* Accelerators at Energy Frontier

2

0.09

6.0

2 10⁶ ZH/5yrs

2

0.09

1.8

 $10^6 \overline{tt}$ / 5yrs

~250

0.07

0.012





Major characteristics of CEPC











- Circular Electron-Positron Collider





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- Circular Electron-Positron Collider



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- Circular Electron-Positron Collider



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Parameter	LEP(2)	FCC-Z	FCC-WW	FCC-ZH	FCC-tt	CEPC
E (GeV)	104	45	80	120	175	120
I (mA)	4	1400	152	30	7	16.6
No. bunches	4	16'700	4'490	1'330	98	50
β* _{x/y} (mm)	1500/50	500 /1	500 / 1	500 /1	1000 / 1	800 / 1.2
ε _x (nm)	30-50	29	3.3	1	2	6.8
ε _y (pm)	250	60	7	2	2	20
P _{SR} [MW]	22	100	100	100	100	100
L (10 ³⁴ cm ⁻² s ⁻¹)/IP	0.012	28	12	6.0	1.8	1.8

Timeline: FCC-ee & CEPC



Phase	FCC	CEPC		
Pre-studies; engineering design; R&D	2014-2022	2014-2021		
Preparatory phase	2022-2027			
Construction	2027-2037	2021-2027		
Data taking	2037-2045	2028-2036		
Important milestones:				

FCC: The first annual meeting: Washington D.C. 23-27. March 2015 http://indico.cern.ch/event/340703/

> preparation of Conceptual Design Report (CDR) for 2018 (update of European Strategy of High Energy Physics).

CEPC: Accelerator pre-CDR issued in March 2015;
 Physics pre-CDR appeared in April 2015;
 R&D funding request passed to Chinese Government (5-year plan 2016-20)



Proposals of New e⁺e⁻ Colliders: Instead of Summary



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Physics at Future Circular Colliders







Three major Higgs production processes at the e^+e^- circular collider:



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Higgs Mass and Width

- A very clean Higgs mass determination in $e^+e^- \rightarrow Zh$ and using a recoil technique (unique for lepton colliders). $m_{\text{recoil}}^2 = (\sqrt{s} - E_{ll})^2 - |\vec{p}_{ll}|^2$
- Preferably with $Z \rightarrow \mu^+ \mu^-$ or $Z \rightarrow e^+ e^-$
- ZH events are tagged independently of Higgs decay mode (invisible decays included).
- Precise measurement of the g_{HZZ} : $\sigma(HZ) \propto g_{HZZ}^2$



	ILC500	FCC – ee	CEPC
	lumiUp		
ZH statistics [10 ⁶]	1	2	1
Δm_H [MeV]	15	8(?)	5.9(?)
$\Delta \Gamma_H / \Gamma_H [\%]$	3	1.0	2.8

Higgs Couplings



- Higgs couplings to WW, ZZ, bb,cc, gg, TT, YY etc can be determined through the tagging of the respective Higgs decay final states.
- Observables:

 $\sigma(e^+e^- \to ZH) \times \mathsf{BR}(H \to X)$

 $\sigma(e^+e^- \to \nu\bar{\nu}H) \times \mathsf{BR}(H \to X)$



all uncertainties	FCC – ee	CEPC
are in %	240 GeV	250 GeV
$\sigma(ZH)$	0.40	0.51
$\sigma(ZH) imes BR(H o b\overline{b})$	0.20	0.28
$\sigma(ZH) imes BR(H o c\overline{c})$	1.2	2.2
$\sigma(ZH) \times BR(H \to \tau^+ \tau^-)$	0.7	1.2
$\sigma(ZH) \times BR(H \to \mu^+ \mu^-)$	13	17.0
$\sigma(ZH) imes {\sf BR}(H o gg)$	1.4	1.6
$\sigma(ZH) imes BR(H o WW)$	0.9	1.5
$\sigma(ZH) imes BR(H o ZZ)$	3.1	4.3
$\sigma(ZH) imes {\sf BR}(H o \gamma \gamma)$	3.0	9.0









Normalized Higgs Couplings



• Higgs couplings normalized to the Standard Model predictions:



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GigaZ → TeraZ



• Run around $\sqrt{s}=M_Z$ (energy scan)

	Current	FCC – ee	CEPC
	Stat./Precision	stat (syst)	stat only
NZ	2×10^7	10 ¹²	2×10^{9}
M_Z [MeV]	91187.6 ± 2.1	$0.005~(<\pm0.1)$	0.1
Γ_Z [MeV]	2495.2 ± 2.3	$0.008~(<\pm 0.1)$	0.2
R_l	20.767 ± 0.025	$0.0001 \ ({}^{0.002}_{0.0002})$	0.001
R_b	0.21629 ± 0.00066	$0.000003 \ (< \pm 0.00004)$	0.00018
A^b_{FB}	0.923 ± 0.020		0.002
$\overline{N_{\nu}}$	2.984 ± 0.008	$0.00008(<\pm0.004)$	0.003

• Potential to reach precision of 100 keV on Z mass and width.



• Critical progress in R_b , R_l , asymmetry measurements, $sin\Theta_W$, ...





OkuW: WW Threshold Scan



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MegaTop: tt Threshold Scan

- For the 1st time the top quark to be studied using a precisely defined leptonic state.
- The beam energy is known and readily variable.
- It is possible to tune the initial spin state, giving additional options for precision threshold measurements.
- The dependence of the t quark cross-section shape on the t quark mass and interactions is computable to high precision (depends on m_t , Γ_t , a_s , g_{Htt} , ISR, luminosity spectrum).





- Photon selection common for both final states \rightarrow cancellations of systematics.
- N_v can be measured vs sqrt(s) \rightarrow sensitivity to NP at high energy scales.



Both methods are independent and complementary: data sets, systematics, theoretical input...





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Heavy Neutrino Searches (FCCee) HNL production and decay



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Studies of charged Lepton Flavour Violation (cLFV)



different chirality structures (as in the LHCb analysis).

• This approach is being integrated with the TAUOLA package (Z.Was, S Jadach).



Summary



- * The circular colliders at the energy frontiers are back on the market (contrary to the death sentence received after LEP).
- * Two ambitious projects (FCC-ee and CEPC) are being pursued.
- The circular colliders offer the potential for biggest data sets up to ttbar threshold and thus provide a vast physics program, in particular:
 - ✓ Higgs studies
 - ✓ Electroweak precise measurements (neutrino counting)
 - ✓ Top quark parameters
 - ✓ W mass

✓ Flavour physics (charged lepton flavour violation)

 \checkmark











Physics reach of linear colliders

a	rXiv:15	604.0	1726	v1 [h	nep-ph]	
\sqrt{s}/GeV :	92,160	240	350	500	1000	3000	threshold scans required
Higgs				-		-	
m _H	-	X	X	X	х	х	Х
Γ_{tot}	-	-	X	х			
$g_{c,b}$	-	X	X	х		Х	
g _{tt} H	-	-	-	х	Х		
<i>SHHH</i>	-	-	-	Х	Х	Х	
$m_{H,A}^{50,51}$	-	-	-	Х	Х	Х	Х
Тор							
m_t^{th}	_	_	X				Х
m_t^{cont}	-	-	-	х	(x)	(x)	
A_{FB}^{t}	-	-	X	х			
gz,γ	-	-	-	х			
<i>gfcnc</i>	-	-	-	Х	Х	(?)	
Electroweak Precision Observables							
$\sin^2 \theta_{\rm eff}(Z-{\rm pole})$	X					(x)	
m_W^{th}	X						х
m_W^{cont}		X	X	х	(x)	(x)	
Γ_Z	Х						Х
A_{LR}	Х						
A_{FB}	Х						

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Physics reach of linear colliders



	arXiv:1	504.0	01726	ov1 []	hep-pł	1]	
\sqrt{s}/GeV :	92,160	240	350	500	1000	3000	threshold scans required
SUSY							
indirect search	Х	X	Х				
direct search	-	_	Х	Х	Х	Х	Х
light higgsinos	_	1 - 1	х	Х			Х
parameter determination	-		х	Х	Х		х
quantum numbers	-	-	х	Х	Х		х
extrapolations	-	-	—	Х	X	Х	х
v mixing							
θ_{23}^2	-	—	Х	X			
Dark Matter							
effective-field-theory	_	_		X	Х	Х	
non-relativistic	—	_	х	X	Х	х	
Extra gauge bosons							
indirect search $m_{z'}$	X	_	_	Х	Х	Х	
v'_f, a'_f	-		—	Х	Х	(x)	
$m_{W'}$	Х	—	-	X	Х	х	
direct search	-	-	-	-	-	X	Х

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New e+e- Accelerators



FCC-hh baseline parameters

Parameter	LHC	HL-LHC	FCC-hh
√s (TeV)	1	4	100
Circumference (km)	26	100 (80)	
Dipole field (T)	8	16 (20)	
Luminosity (10 ³⁴ cm ⁻² s ⁻¹)	1	5	5 [→ 30]
Integrated Lumi (ab-1)	0.3	3	3 [→ 30]
Bunch spacing (ns)	25		25 { <mark>5</mark> }
Events / bunch crossing	35	140	170 {34} [→ 1020 {204}]
Total SR Power (MW)	0.007	0.015	<mark>5</mark> [→ <u>3</u> 0]

• Cross-sections for most interesting processes grow significantly from 14 TeV to 100 TeV

 With the luminosity of 30 ab⁻¹ @ 100 TeV most measurements will be limited by systematic uncertainties



→ equivalent to an Airbus A380 (560 t) at full speed (850 km/h).



- Task: develop Nb₃Sn-based 16 T dipole magnet technology.
- Goal: 16T short dipole models by 2018/19 (America, Asia, Europe).
- Non negligible synchrotron radiation (the first time in proton-proton).





Precision measurements and New Physics

- With the Higgs discovery the SM has nowhere to go!
- Any deviation is now 'new physics' , 5σ is discovery.
- Indirect but inclusive information on new physics with ~weak couplings.
- Precise knowledge of both m_H and m_{top} is essential.



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Top threshold scan





The cross-section around the threshold is affected by several properties of the top quark and by QCD

- Top mass, width, Yukawa coupling
- · Strong coupling constant



 Effects of some parameters are correlated; dependence on Yukawa coupling rather weak precise external α_s helps

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New e+e- Accelerators



Top Anomalous Couplings Example: $t_L t_L Z$ and $t_R t_R Z$ couplings, g_L and g_R $2\mathbf{e}F_{1V}^{Z} = \mathbf{g}_{R} + \mathbf{g}_{L}$ Couplings most sensitive to composite Higgs models $2\mathbf{e}F_{1A}^{Z} = \mathbf{g}_{R} - \mathbf{g}_{L}$ $\Delta g_R/g_R(\%)$ 20% Other NP models 4D-CHM (tested at the LHC) f < 2 TeV 10% LC (Poeschl) -10%FC -20% -30% 20% 30% eel0% $\Delta g_L/g_L(\%)$ 20% Adapted from S. de Curtis et al.

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New e+e- Circular Accelerators at Energy Frontier

arXiv:1504.05407

Top Anomalous Couplings



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Heavy Neutrino Searches (FCC-ee)



Fermions get mass via the Yukawa couplings

$$-\mathcal{L}_{\text{Yukawa}} = Y_{ij}^{d} \overline{Q_{Li}} \phi D_{Rj} + Y_{ij}^{u} \overline{Q_{Li}} \tilde{\phi} U_{Rj} + Y_{ij}^{\ell} \overline{L_{Li}} \phi E_{Rj} + \text{h.c.}$$

If we want the same coupling for neutrinos, we need right-handed (sterile) neutrinos... the most generic lagrangian is



Neutrinos : the Ne forgive the confusion b	w Physics there is between fields and particle	and a lot of it!	
SM	Dirac mass term only ≡ «Yukawa»	Majorana mass term only	Dirac AND Majorana mass terms
$\begin{array}{ccc} \nu_{L} & \bar{\nu}_{R} \\ = \frac{1}{2} & \frac{1}{2} \end{array}$	$\begin{array}{cccc} \nu_{L} & \nu_{R} & \overline{\nu}_{R} & \overline{\nu}_{L} \\ \frac{1}{2} & 0 & \frac{1}{2} & 0 \end{array}$	$\begin{array}{ccc} v_{L} & & & \bar{v}_{R} \\ \frac{1}{2} & & \frac{1}{2} \end{array}$	M ₃ M ₂ M ₁ M ₁ M ₃ M ₂ M ₁ M ₁ M ₂ M ₁ M ₂ M ₁ M ₂ M ₁ M ₂ M ₁ M ₁ M ₂ M ₂ M ₁ M ₂ M ₁ M ₂ M ₂ M ₁ M ₂ M ₂ M ₂ M ₁ M ₂ M ₂ M ₂ M ₂ M ₂ M ₂ M ₂ M ₂
X 3 Families	X 3 Families	X 3 Families	`
6 massless states	3 masses 12 states 3 active neutrinos 3 active antinu's	3 masses 6 active states No steriles 3 mixing angles	6 masses (Majorana) 12 states 6 active states 6 sterile neutrinos
wrong	 6 sterile neutrinos 3 mixing angles 1 CP violating phase 0vββ = 0 	3 CP violating phases 0v ββ ≠ 0	More mixing angles and CPV phases $0\mathbf{v}\beta\beta \neq 0$ (different than pure Majorana case if $m_N < 100 \text{ MeV}$) \rightarrow Leptogenesis and Dark matter

Mass hierarchies are all unknown except $m_1 < m_2$ Preferred scenario has both Dirac and Majorana terms ...

... many physics possibilities and experimental challenges

one family see-	Manifestations of right ha	<mark>nded neutrinos</mark>
saw : $\theta \approx (m_D/M)$ m_p^2	$\boldsymbol{v} = \boldsymbol{v} \boldsymbol{L} \cos \theta - \boldsymbol{N}^{c}_{R} \sin \theta$	v = light mass eigenstate N = heavy mass eigenstate
$m_v \approx \frac{w}{M}$ $m_N \approx M$	$N = N_R \cos\theta + v_L^{c} \sin\theta$	$\neq v_L$, active neutrino which couples to weak inter
$ U ^2 \propto \theta^2 \approx m_v / m_N$	what is produced in W, Z decays is: $v_L = v \cos \theta + N \sin \theta$	and N _R , which does'nt.

-- mixing with active neutrinos leads to various observable consequences

-- if very light (eV) , possible effect on neutrino oscillations

-- if in keV region (dark matter), monochromatic photons from galaxies with $E=m_N/2$

-- possibly measurable effects at High Energy

If N is heavy it will decay in the detector (not invisible)

→ PMNS matrix unitarity violation and deficit in Z «invisible» width

(Serguei)

→ Higgs and Z visible exotic decays H→ $v_i \overline{N}_i$ and Z→ $v_i \overline{N}_i$ also W-> $I_i \overline{N}_i$

- \clubsuit violation of unitarity and lepton universality in Z, W or $\tau\,$ decays
- -- etc... etc...

-- Couplings are small (m_v/m_N) (but who knows?) and generally out of reach of hadron colliders (but this deserves to be revisited for detached vertices @LHC, HL-LHC, FCC-hh)

Heavy Neutrino Searches (FCCee) Direct Search for HNL in Z decays



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The EFT approach



$$R_{e} = \frac{1 - \gamma_{5}}{2} \binom{0}{\psi_{e}}, \ R_{\mu} = \frac{1 - \gamma_{5}}{2} \binom{0}{\psi_{\mu}}, \ R_{\tau} = \frac{1 - \gamma_{5}}{2} \binom{0}{\psi_{\tau}}.$$
 (2.40)

Taking into account Eq. 2.9 and 2.40 and the matrix of Higgs fields from [53], one can derive the following relevant dimension six operators:

$$O_1 = (\bar{L}\gamma_\mu L)(\bar{L}\gamma^\mu L), \qquad (2.41)$$

$$O_2 = (\bar{L}\tau^a \gamma_\mu L)(\bar{L}\tau^a \gamma^\mu L), \qquad (2.42)$$

$$O_3 = (\bar{R}\gamma_\mu R)(\bar{R}\gamma^\mu R), \qquad (2.43)$$

$$O_4 = (\bar{R}\gamma_\mu R)(\bar{L}\gamma^\mu L), \qquad (2.44)$$

$$R_1 = g'(\bar{L}H\sigma_{\mu\nu}R)B^{\mu\nu}, \qquad (2.45)$$

$$R_2 = g(\bar{L}\tau^a H \sigma_{\mu\nu} R) W^{\mu\nu}, \qquad (2.46)$$

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The EFT approach

as defined above, $B_{\mu\nu}$ and $W_{\mu\nu,a}$ are the electroweak gauge fields, gand g' are the coupling constants of $SU(2)_L$ and $U(1)_Y$, H denotes the matrix of Higgs fields, L(R) are the left(right)-handed fields and $\sigma^{\mu\nu} = \frac{i}{4} [\gamma^{\mu}, \gamma^{\nu}]$. According to S. Turczyk et. al. [54], higher order operators are suppressed by small lepton Yukawa couplings, so we will not consider them in this thesis. In the effective field theory the most general Hamiltonian that describes the discussed process is formed as the sum of the operators from Eq. 2.41 - 2.46. For the studied process $\tau^- \rightarrow \mu^-\mu^+\mu^-$ the operators O_1 and O_2 are identical after projecting them on charged leptons. The O_3 corresponds to a purelly right-handed current and is completely analogous to O_1 . For radiative operators R_1 and R_2 the latter is suppressed by small Yukawa coupling of τ , so only the photonic operator R_1 is relevant.

The analysis performed in this dissertation was also interpreted in terms of the BSM operators, as described in Sect. 4.10. The respective decay widths can be presented in the form of Dalitz distributions [55], which were derived in the following five cases, corresponding to different lepton chirality structures:

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• Four left-handed leptons (O_1 operator):

$$\frac{d^2 \Gamma_V^{(LL)(LL)}}{d^2 m_{23} d^2 m_{12}} = \frac{\left| g_V^{(L_\mu L^\tau)(L_\mu L^\mu)} \right|^2 (m_\tau^2 - m_\mu^2)^2 - (2m_{12}^2 - m_\tau^2 - 3m_\mu^2)^2}{\Lambda^4} \frac{(m_\tau^2 - m_\mu^2)^2 - (2m_{12}^2 - m_\tau^2 - 3m_\mu^2)^2}{256\pi^3 m_\tau^3}.$$
(2.47)

• Two left-handed, two right-handed leptons (O_4 operator):

$$\frac{d^2 \Gamma_V^{(LL)(RR)}}{d^2 m_{23} d^2 m_{12}} = \frac{\left| \frac{g_V^{(L_\mu L^\tau)(L_\mu L^\mu)}}{\Lambda^4} \right|^2}{\left[\frac{(m_\tau^2 - m_\mu^2)^2 - 4m_\mu^2(m_\tau^2 + m_\mu^2 - m_{12}^2)}{512\pi^3 m_\tau^3} - \frac{(2m_{12}^2 - m_\tau^2 - 3m_\mu^2)^2 + (2m_{23}^2 - m_\tau^2 - 3m_\mu^2)^2}{1024\pi^3 m_\tau^3} \right].$$
(2.48)

$$\frac{d^{2}\Gamma_{rad}^{(L,R)}}{d^{2}m_{23}d^{2}m_{12}} = \alpha_{em}^{2} \frac{\left|g_{rad}^{(L_{\mu}R^{\tau})}\right|^{2}\nu^{2}}{\Lambda^{4}} \left[\frac{4m_{\mu}^{2}(m_{\tau}^{2}+m_{\mu}^{2}-m_{12}^{2})}{128\pi^{3}m_{\tau}^{3}}(\frac{1}{m_{13}^{4}}+\frac{1}{m_{23}^{4}})\right. \\ \left.+\frac{m_{\mu}(m_{\tau}^{4}(-3m_{\tau}^{2}m_{\mu}^{2}+2m_{\mu}^{2})}{128\pi^{3}m_{\tau}^{3}m_{23}^{2}m_{12}^{2}}+\frac{2m_{12}^{2}-3m_{\mu}^{2}}{128\pi^{3}m_{\tau}^{3}}\right. \\ \left.+\frac{(m_{13}^{2}+m_{23}^{2})(m_{12}^{4}+m_{13}^{4}+m_{23}^{4}-6m_{\mu}^{2}(m_{\mu}^{2}+m_{\tau}^{2}))}{256\pi^{3}m_{\tau}^{3}m_{23}^{2}m_{12}^{2}}\right].$$

$$(2.49)$$

• Interference between O_1 and R_1 :

$$\frac{d^{2}\Gamma_{mix}^{(LL)(RR)}}{d^{2}m_{23}d^{2}m_{12}} = \alpha_{cm}^{2} \frac{2\nu Re\left[g_{V}^{(L_{\mu}L^{\tau})(L_{\mu}L^{\mu})}g_{rad}^{*LR}\right]}{\Lambda^{4}} \left[\frac{m_{12}^{2} - 3m_{\mu}^{2}}{64\pi^{3}m_{\tau}^{2}} + \frac{m_{\mu}^{2}(m_{\tau}^{2} - m_{\mu})^{2}(m_{13}^{2} + m_{23}^{2})}{128\pi^{3}m_{\tau}^{3}m_{23}^{2}m_{12}^{2}}\right].$$
(2.50)

• Interference between O_4 and R_1 :

$$\frac{d^2 \Gamma_{rad}^{(LL)(RR)}}{d^2 m_{23} d^2 m_{12}} = \alpha_{em} \frac{2\nu Re \left[g_V^{(L_\mu L^\tau)(R_\mu R^\mu)} g_{rad}^{*LR} \right]}{\Lambda^4} \left[\frac{m_\tau^2 - m_{12}^2 - 3m_\mu^2}{256\pi^3 m_\tau^3} + \frac{m_\mu (m_\tau^2 - m_\mu^2)(m_{13}^2 + m_{23}^2)}{256\pi^3 m_\tau^2 m_{23}^2 m_{12}^2} \right].$$
(2.51)

New e+e- Circular Accelera

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The EFT approach

In the Eq. 2.47 - 2.51 the following dimuon masses are defined:

$$m_{--}^2 = m_{12} = (p_{\mu^-} + p'_{\mu^-})^2, \qquad m_{+-}^2 = m_{23} = (p_{\mu^-} + p_{\mu^+})^2, \quad (2.52)$$

and m_{ℓ} are the masses of corresponding leptons, g_V are the coupling constants and ν is the element from the Higgs matrix. All the above models and several others were implemented by the author in the TAUOLA library [56] of Monte Carlo programs dedicated to τ physics. The Dalitz distributions corresponding to the simulation of each of the above mentioned models can be found in Fig. 2.5.

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The EFT approach



Figure 2.5: Dalitz distributions simulated in the effective field approach for the five different BSM operators corresponding to different lepton chirality structures [53]. The distributions were implemented in the TAUOLA package and normalized to unit area.

New e+e- Circular Accelerators at Energy