

Fully differential decay rate of a SM Higgs boson into a b-pair at NNLO

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in collaboration with

V. Del Duca, C. Duhr, *G. Somogyi*, F. Tramontano



Matter to the Deepest 2015, Ustron
September 14, 2015

Higgs boson has been discovered

- m_H [GeV] = $125.09_{\pm 0.21_{\text{stat}} \pm 0.11_{\text{syst}}}$ (CMS + ATLAS Run 1: $\gamma\gamma$ + 4 lepton)
- Γ_H [MeV] = $1.7^{+7.7}_{-1.8}$ (CMS), < 23 (95%, ATLAS)
- $\sigma/\sigma_{\text{SM}} = 1.00 \pm 0.13$ (ATLAS)
- All measured properties are consistent with SM expectations within experimental uncertainties
 - spin zero
 - parity +
 - couples to masses of W and Z (with $c_v=1$ within experimental uncertainty)
- Yet it still could be the first element of an extended Higgs sector (e.g. SUSY neutral Higgs)
 - Distinction requires high-precision prediction for both production and decay

Example: $pp \rightarrow H + X \rightarrow b\bar{b} + X$ in PT

- $\Gamma_H [\text{MeV}] = 4.07 \pm 0.16_{\text{theo}}$

\Rightarrow can use the narrow width approximation

$$\frac{d\sigma}{dO_{b\bar{b}}} = \left[\sum_{n=0}^{\infty} \frac{dd^2\sigma_{pp \rightarrow H+X}^{(n)}}{dp_{\perp,H} d\eta_H} \right] \times \left[\frac{\sum_{n=0}^{\infty} d\Gamma_{H \rightarrow b\bar{b}}^{(n)} / dO_{b\bar{b}}}{\sum_{n=0}^{\infty} \Gamma_{H \rightarrow b\bar{b}}^{(n)}} \right] \times \text{Br}(H \rightarrow b\bar{b})$$

known up
to NNLO

this talk:
up to NNLO

known with
1% accuracy

$$pp \rightarrow H + X \rightarrow b \bar{b} + X \text{ in PT}$$

Including up to NNLO corrections for production and decay:

$$\begin{aligned} \frac{d\sigma}{dO_{b\bar{b}}} = & \left[\frac{d^2\sigma_{pp \rightarrow H+X}^{(0)}}{dp_{\perp,H} d\eta_H} \frac{d\Gamma_{H \rightarrow b\bar{b}}^{(0)}/dO_{b\bar{b}} + d\Gamma_{H \rightarrow b\bar{b}}^{(1)}/dO_{b\bar{b}} + d\Gamma_{H \rightarrow b\bar{b}}^{(2)}/dO_{b\bar{b}}}{\Gamma_{H \rightarrow b\bar{b}}^{(0)} + \Gamma_{H \rightarrow b\bar{b}}^{(1)} + \Gamma_{H \rightarrow b\bar{b}}^{(2)}} \right. \\ & + \frac{d^2\sigma_{pp \rightarrow H+X}^{(1)}}{dp_{\perp,H} d\eta_H} \frac{d\Gamma_{H \rightarrow b\bar{b}}^{(0)}/dO_{b\bar{b}} + d\Gamma_{H \rightarrow b\bar{b}}^{(1)}/dO_{b\bar{b}}}{\Gamma_{H \rightarrow b\bar{b}}^{(0)} + \Gamma_{H \rightarrow b\bar{b}}^{(1)}} \\ & \left. + \frac{d^2\sigma_{pp \rightarrow H+X}^{(2)}}{dp_{\perp,H} d\eta_H} \frac{d\Gamma_{H \rightarrow b\bar{b}}^{(0)}/dO_{b\bar{b}}}{\Gamma_{H \rightarrow b\bar{b}}^{(0)}} \right] \times \text{Br}(H \rightarrow b\bar{b}) \end{aligned}$$

Method

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(with jet functions defined in $d = 4$)

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- ✓ fully differential predictions
(with jet functions defined in $d = 4$)
- ✓ option to constrain subtraction near singular regions (important check)

Completely Local Subtractions for Fully Differential
Predictions@NNLO

Explicit and general: structure

of subtractions is governed by the jet functions

$$\sigma^{\text{NNLO}} = \sigma_{m+2}^{\text{RR}} + \sigma_{m+1}^{\text{RV}} + \sigma_m^{\text{VV}} = \sigma_{m+2}^{\text{NNLO}} + \sigma_{m+1}^{\text{NNLO}} + \sigma_m^{\text{NNLO}}$$

$$\sigma_{m+2}^{\text{NNLO}} = \int_{m+2} \left\{ d\sigma_{m+2}^{\text{RR}} J_{m+2} - d\sigma_{m+2}^{\text{RR},A_2} J_m - \left(d\sigma_{m+2}^{\text{RR},A_1} J_{m+1} - d\sigma_{m+2}^{\text{RR},A_{12}} J_m \right) \right\}$$

$$\sigma_{m+1}^{\text{NNLO}} = \int_{m+1} \left\{ \left(d\sigma_{m+1}^{\text{RV}} + \int_1 d\sigma_{m+2}^{\text{RR},A_1} \right) J_{m+1} - \left[d\sigma_{m+1}^{\text{RV},A_1} + \left(\int_1 d\sigma_{m+2}^{\text{RR},A_1} \right) A_1 \right] J_m \right\}$$

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RR,A₂ regularizes doubly-unresolved limits

G. Somogyi, ZT hep-ph/0609041, hep-ph/0609043

G. Somogyi, ZT, V. Del Duca hep-ph/0502226, hep-ph/0609042

Z. Nagy, G. Somogyi, ZT hep-ph/0702273

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RR,A₁₂ removes overlapping subtractions

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CoLoRFuI NNLO uses known ingredients

- Universal IR structure of QCD (squared) matrix elements
 - ϵ -poles of one- and two-loop amplitudes
 - soft and collinear factorization of QCD matrix elements

tree-level 3-parton splitting, double soft current:

J.M. Campbell, E.W.N. Glover 1997, S. Catani, M. Grazzini 1998

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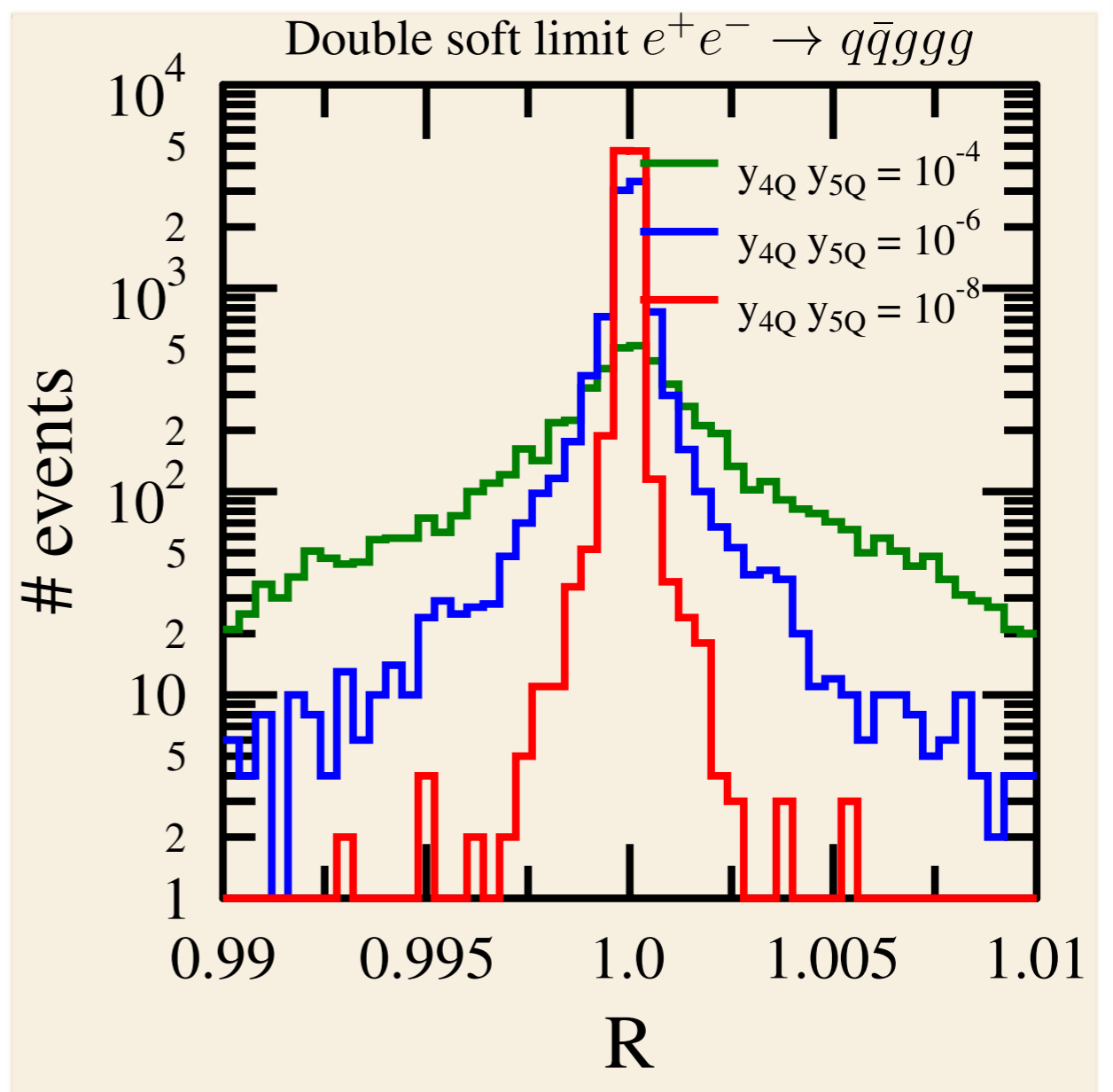
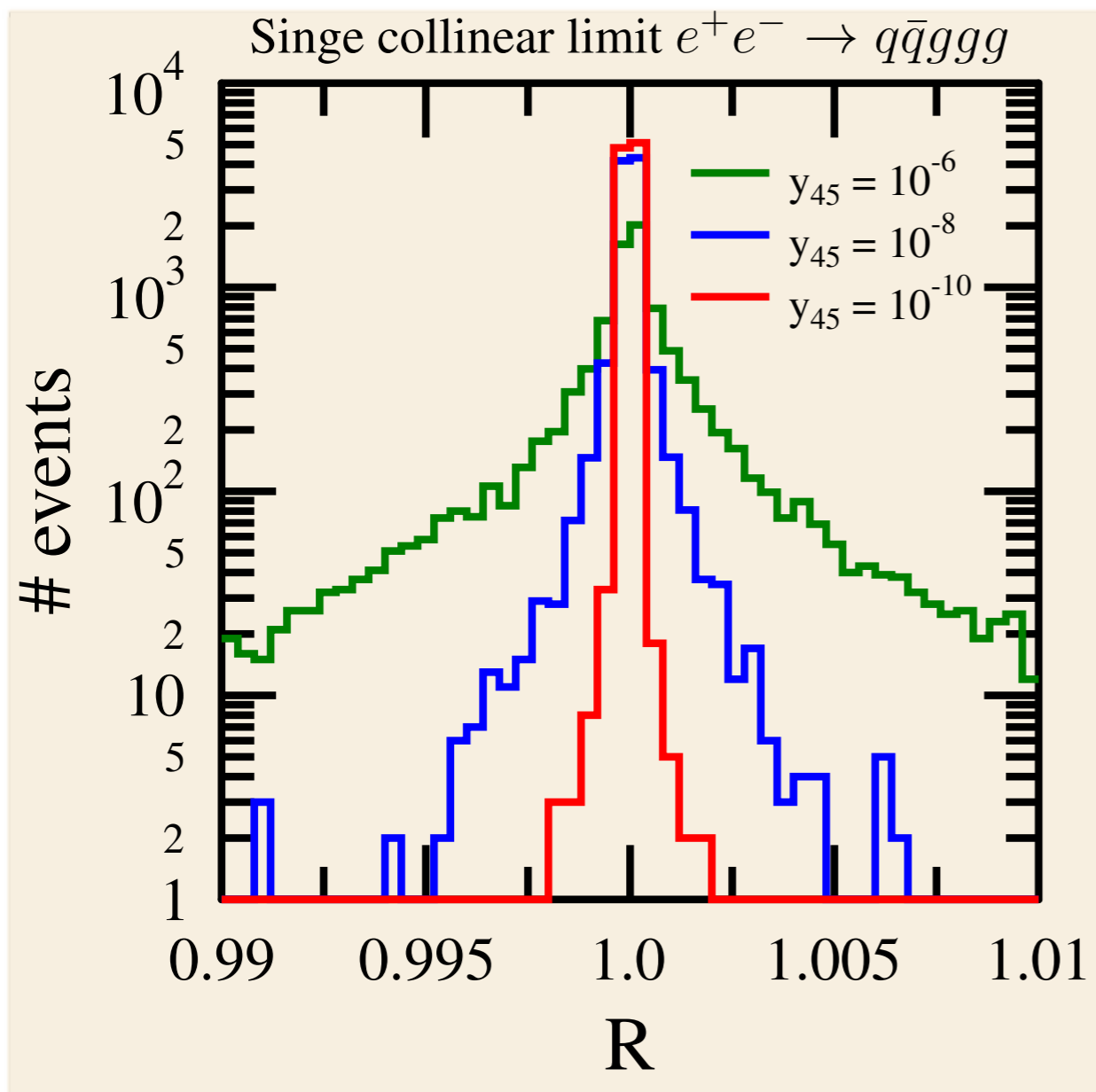
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- Extension over whole phase space using momentum mappings (not unique):

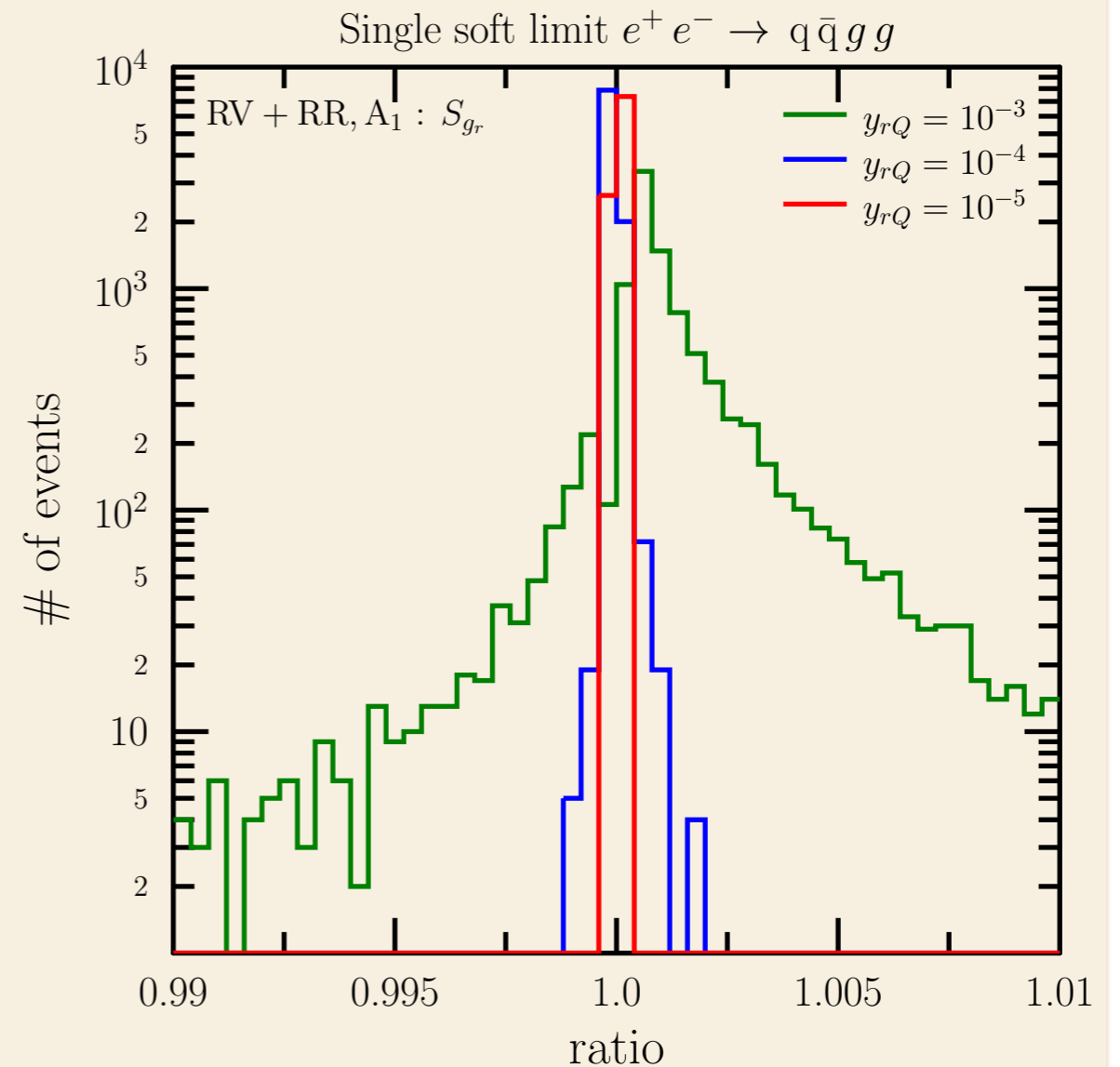
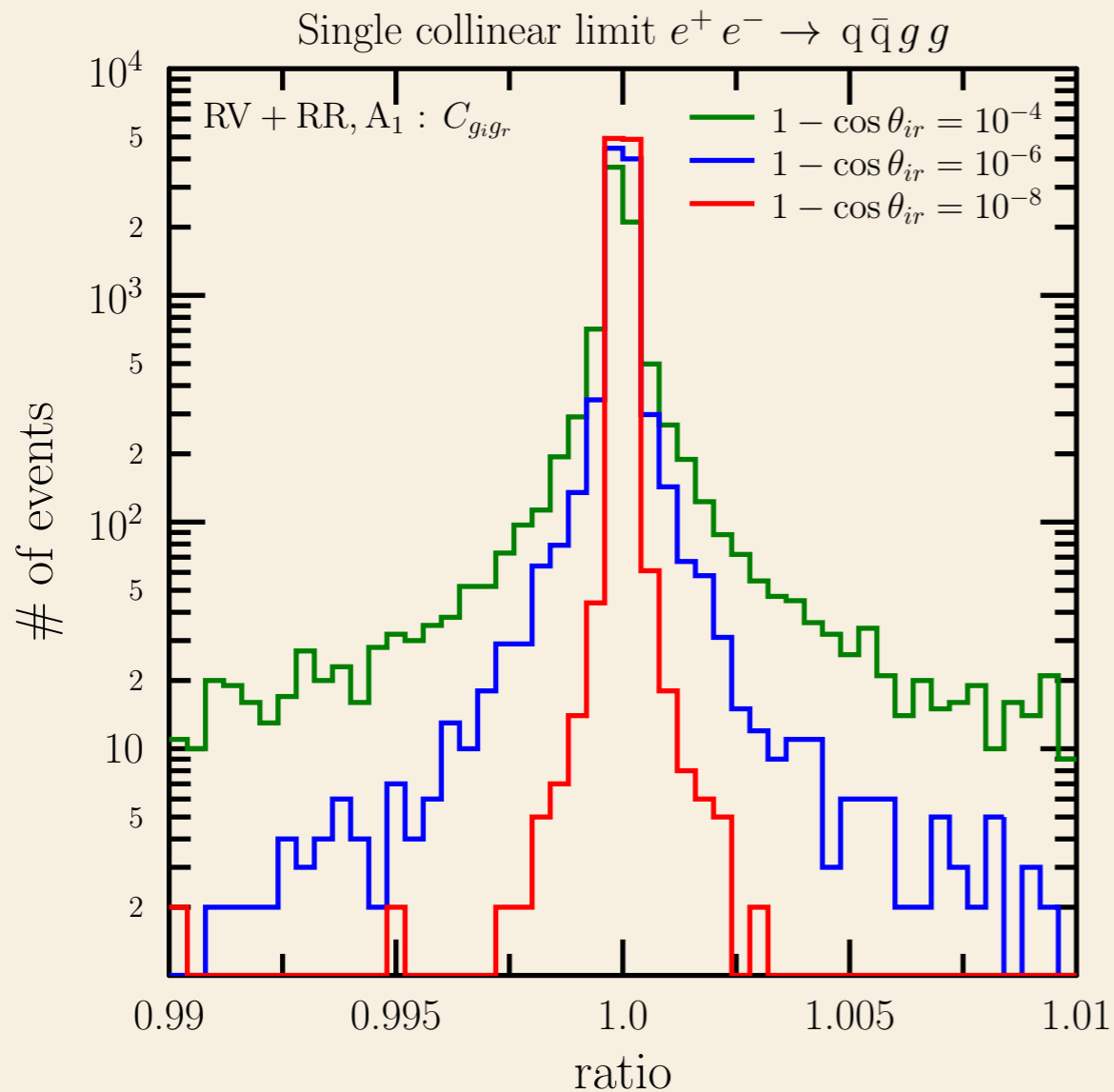
$$\{p\}_{n+s} \rightarrow \{\tilde{p}\}_n$$

Fully local: kinematic singularities cancel in RR



$R = \text{subtraction}/RR$

Fully local: kinematic singularities cancel in RV



$$R = \text{subtraction} / (RV + \int_1 RR, A_1)$$

Cancellation of poles

- ▶ we checked the cancellation of the leading and first subleading poles (defined in our subtraction scheme) for arbitrary number of m jets
- ▶ for $m=2$,
 - ▶ the insertion operators are independent of the kinematics (momenta are back-to-back, so MI's are needed at the endpoints only)
 - ▶ color algebra is trivial: $T_1 T_2 = -T_1^2 = -T_2^2 = -C_F$
- ▶ so can demonstrate the cancellation of poles

Poles cancel: $H \rightarrow b\bar{b}$ at $\mu = m_H$

$$\sigma_m^{\text{NNLO}} = \int_m \left\{ d\sigma_m^{\text{VV}} + \int_2 \left[d\sigma_{m+2}^{\text{RR},A_2} - d\sigma_{m+2}^{\text{RR},A_{12}} \right] + \int_1 \left[d\sigma_{m+1}^{\text{RV},A_1} + \left(\int_1 d\sigma_{m+2}^{\text{RR},A_1} \right)^{A_1} \right] \right\} J_m$$

$$\begin{aligned} d\sigma_{H \rightarrow b\bar{b}}^{\text{VV}} = & \left(\frac{\alpha_s(\mu^2)}{2\pi} \right)^2 d\sigma_{H \rightarrow b\bar{b}}^{\text{B}} \left\{ + \frac{2C_F^2}{\epsilon^4} + \left(\frac{11C_A C_F}{4} + 6C_F^2 - \frac{C_F n_f}{2} \right) \frac{1}{\epsilon^3} \right. \\ & + \left[\left(\frac{8}{9} + \frac{\pi^2}{12} \right) C_A C_F + \left(\frac{17}{2} - 2\pi^2 \right) C_F^2 - \frac{2C_F n_f}{9} \right] \frac{1}{\epsilon^2} \\ & \left. + \left[\left(-\frac{961}{216} + \frac{13\zeta_3}{2} \right) C_A C_F + \left(\frac{109}{8} - 2\pi^2 - 14\zeta_3 \right) C_F^2 + \frac{65C_F n_f}{108} \right] \frac{1}{\epsilon} \right\} \end{aligned}$$

C. Anastasiou, F. Herzog, A. Lazopoulos, arXiv:0111.2368

$$\begin{aligned} \sum \int d\sigma^{\text{A}} = & \left(\frac{\alpha_s(\mu^2)}{2\pi} \right)^2 d\sigma_{H \rightarrow b\bar{b}}^{\text{B}} \left\{ - \frac{2C_F^2}{\epsilon^4} - \left(\frac{11C_A C_F}{4} + 6C_F^2 + \frac{C_F n_f}{2} \right) \frac{1}{\epsilon^3} \right. \\ & - \left[\left(\frac{8}{9} + \frac{\pi^2}{12} \right) C_A C_F + \left(\frac{17}{2} - 2\pi^2 \right) C_F^2 - \frac{2C_F n_f}{9} \right] \frac{1}{\epsilon^2} \\ & \left. - \left[\left(-\frac{961}{216} + \frac{13\zeta_3}{2} \right) C_A C_F + \left(\frac{109}{8} - 2\pi^2 - 14\zeta_3 \right) C_F^2 + \frac{65C_F n_f}{108} \right] \frac{1}{\epsilon} \right\} \end{aligned}$$

V. Del Duca, C. Duhr, G. Somogyi, F. Tramontano, Z. Trócsányi, arXiv:1501.07226

Example: $e^+e^- \rightarrow m(=3)$ jets at $\mu^2 = s$

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$$d\sigma_3^{\text{VV}} = \mathcal{Poles}(A_3^{(2 \times 0)} + A_3^{(1 \times 1)}) + \mathcal{Finite}(A_3^{(2 \times 0)} + A_3^{(1 \times 1)})$$

$$\mathcal{Poles}(A_3^{(2 \times 0)} + A_3^{(1 \times 1)}) + \mathcal{Poles} \sum \int d\sigma^A = 200k \text{ Mathematica lines}$$

= zero numerically in any phase space point:

```

      0.      2      0. nf
      0. + --- + 0. Nc + ----- + 0. Nc nf
          2          Nc

Out[1]= ----- +
          2
          e

      0.      2      0. nf
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= zero analytically according to C. Duhr

Message:

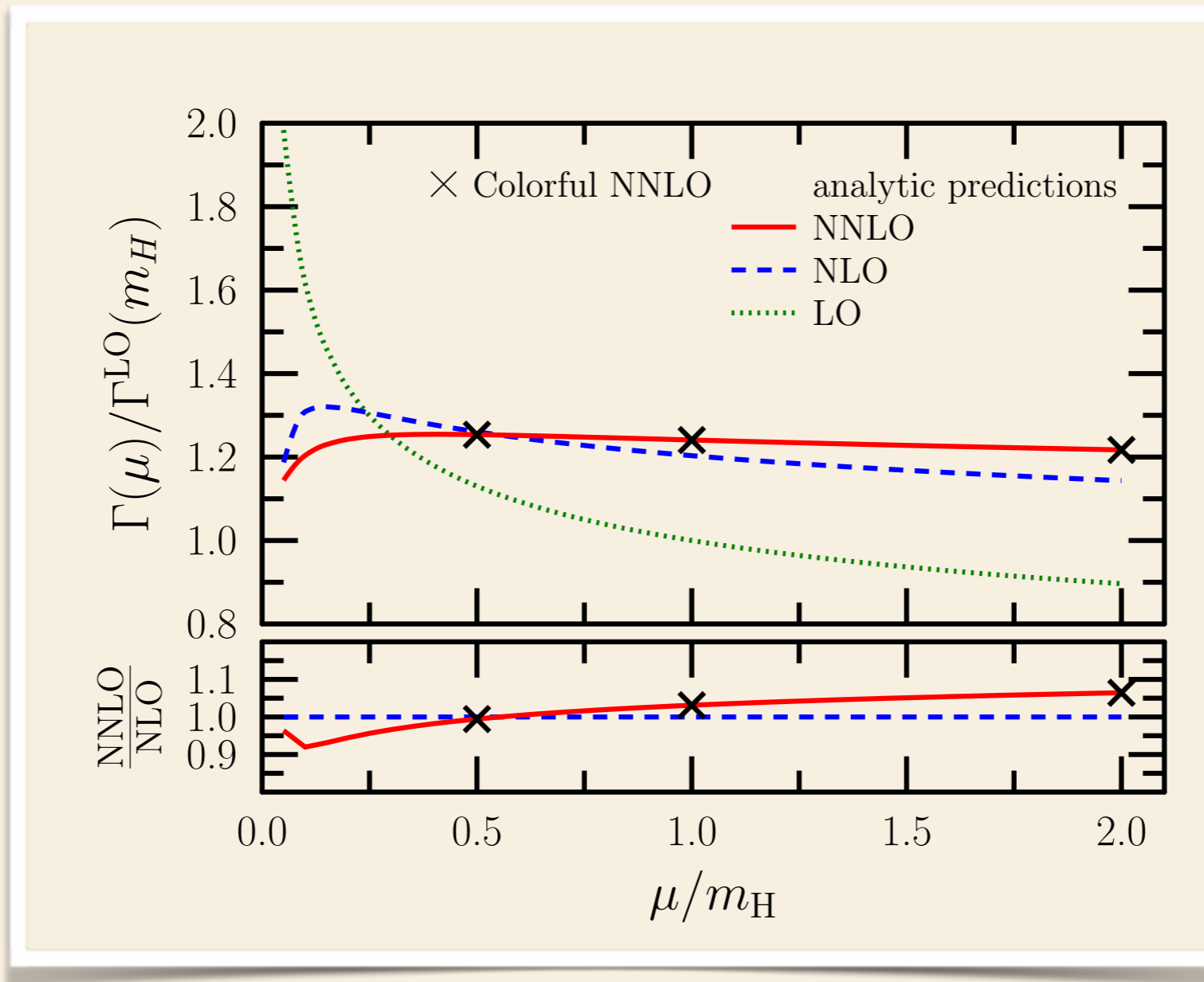
$$\sigma_3^{\text{NNLO}} = \int_3 \left\{ d\sigma_3^{\text{VV}} + \sum \int d\sigma^A \right\}_{\epsilon=0} J_3$$

indeed finite in $d=4$ dimensions

Application

Example: $H \rightarrow b\bar{b}$

$$\Gamma_{H \rightarrow b\bar{b}}^{\text{NNLO}}(\mu = m_H) = \Gamma_{H \rightarrow b\bar{b}}^{\text{LO}}(\mu = m_H) \left[1 - \left(\frac{\alpha_s}{\pi}\right) 5.666667 - \left(\frac{\alpha_s}{\pi}\right)^2 29.149 + \mathcal{O}(\alpha_s^3) \right]$$



Scale dependence of the inclusive decay rate $\Gamma(H \rightarrow b\bar{b})$

analytic: K.G. Chetyrkin hep-ph/9608318

Can constrain subtractions

We can constrain subtractions near singular regions ($\alpha_0 < 1$)

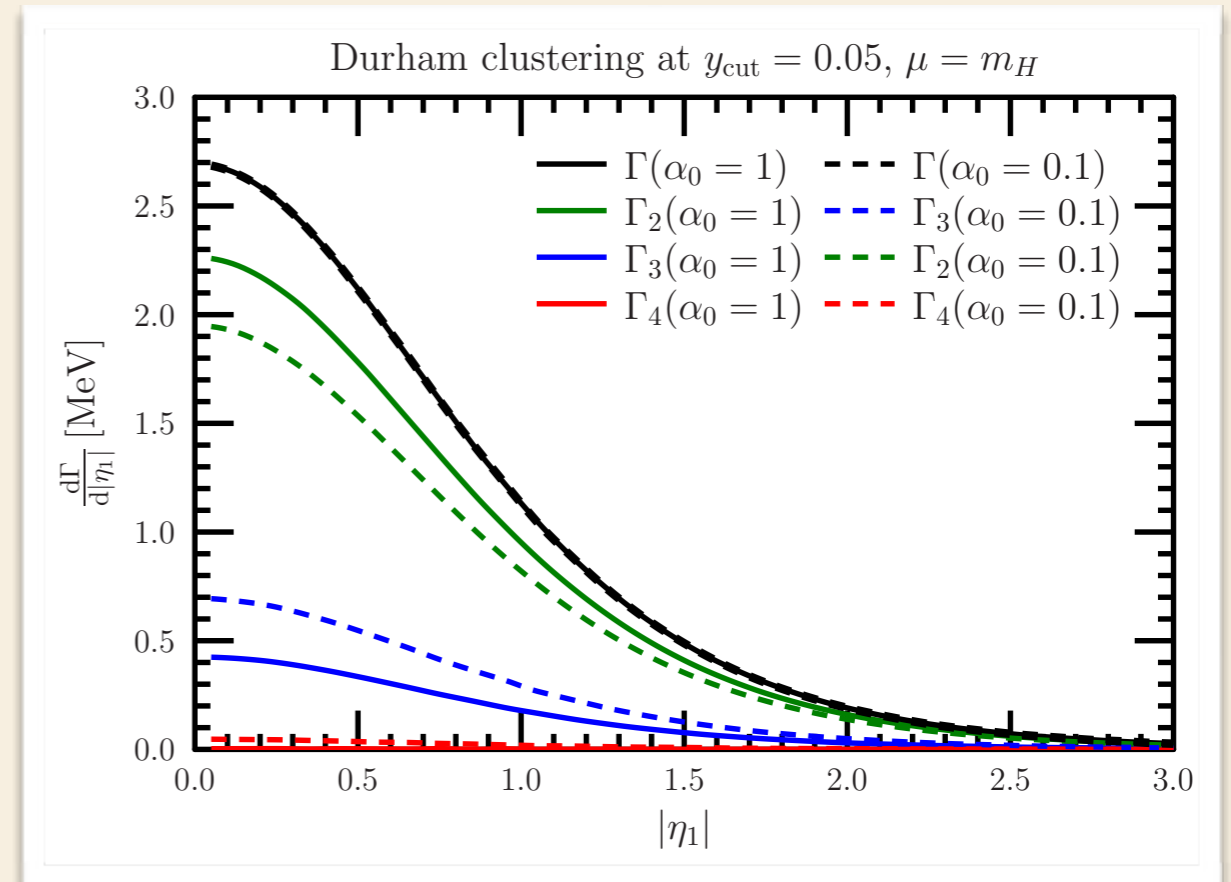
Poles cancel numerically ($\alpha_0 = 0.1$)

$$d\sigma_{H \rightarrow b\bar{b}}^{VV} + \sum \int d\sigma^A = \frac{5.4 \times 10^{-8}}{\epsilon^4} + \frac{3.9 \times 10^{-5}}{\epsilon^3} + \frac{3.3 \times 10^{-3}}{\epsilon^2} + \frac{6.7 \times 10^{-3}}{\epsilon} + \mathcal{O}(1)$$

$$Err\left(\sum \int d\sigma^A\right) = \frac{3.1 \times 10^{-5}}{\epsilon^4} + \frac{5.0 \times 10^{-4}}{\epsilon^3} + \frac{8.1 \times 10^{-3}}{\epsilon^2} + \frac{7.7 \times 10^{-2}}{\epsilon} + \mathcal{O}(1)$$

Predictions remain the same:

rapidity distribution of the leading jet in the rest frame of the Higgs boson. jets are clustered using the Durham algorithm (flavour blind) with $y_{\text{cut}} = 0.05$



Subtractions may help efficiency

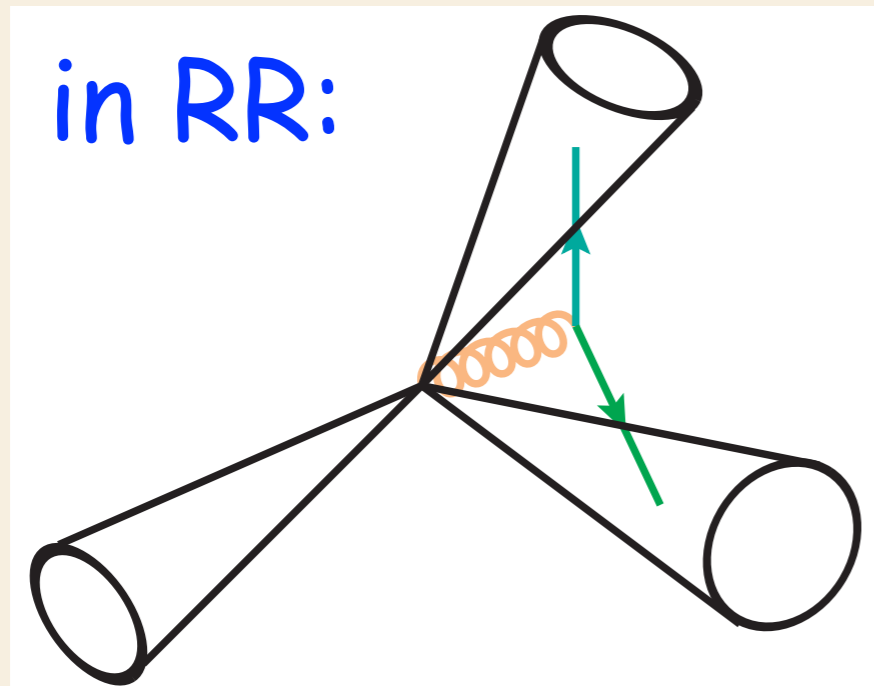
We can constrain subtractions near singular regions ($\alpha_0 < 1$), leading to fewer calls of subtractions:

α_0	1	0.1
timing (rel.)	1	0.40
$\langle N_{\text{sub}} \rangle$	52	14.5

$\langle N_{\text{sub}} \rangle$ is the average number of subtraction calls

IR safe predictions w flavour- k_{\perp}

At NNLO accuracy the Durham algorithm is not infrared safe if the jet is tagged because **soft gluon splitting can spoil the flavor of jets**

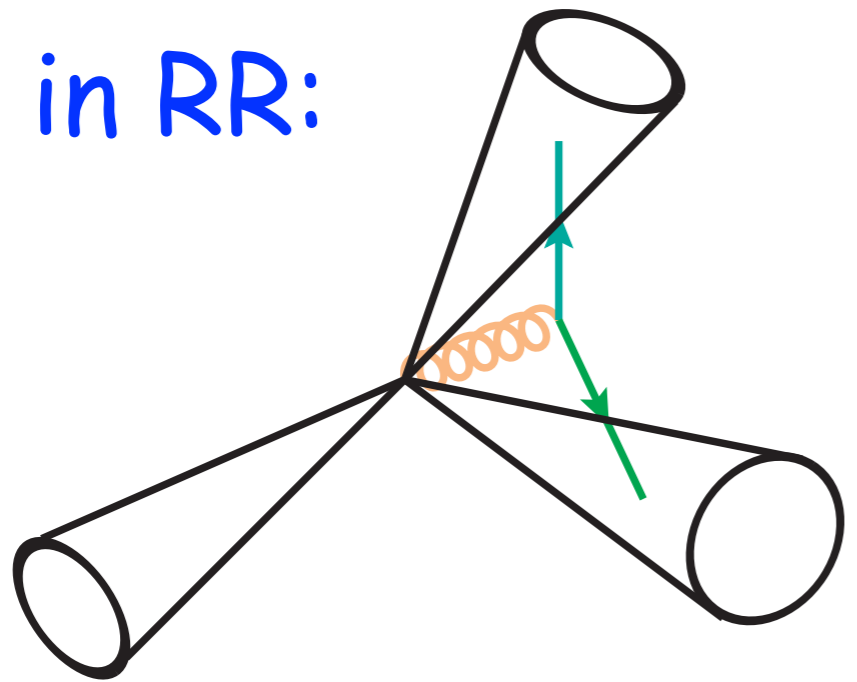


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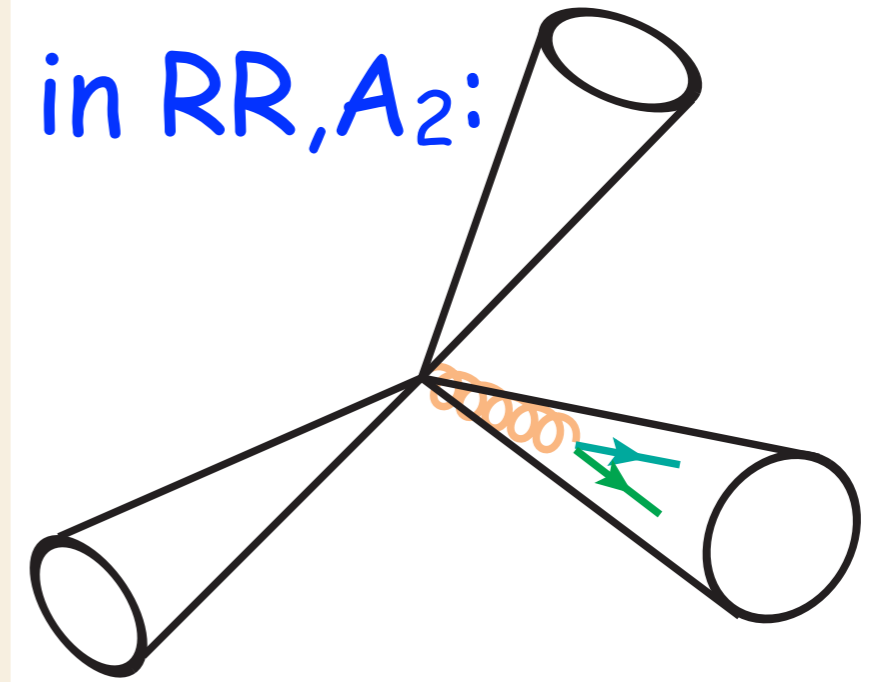
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of jets

in RR:



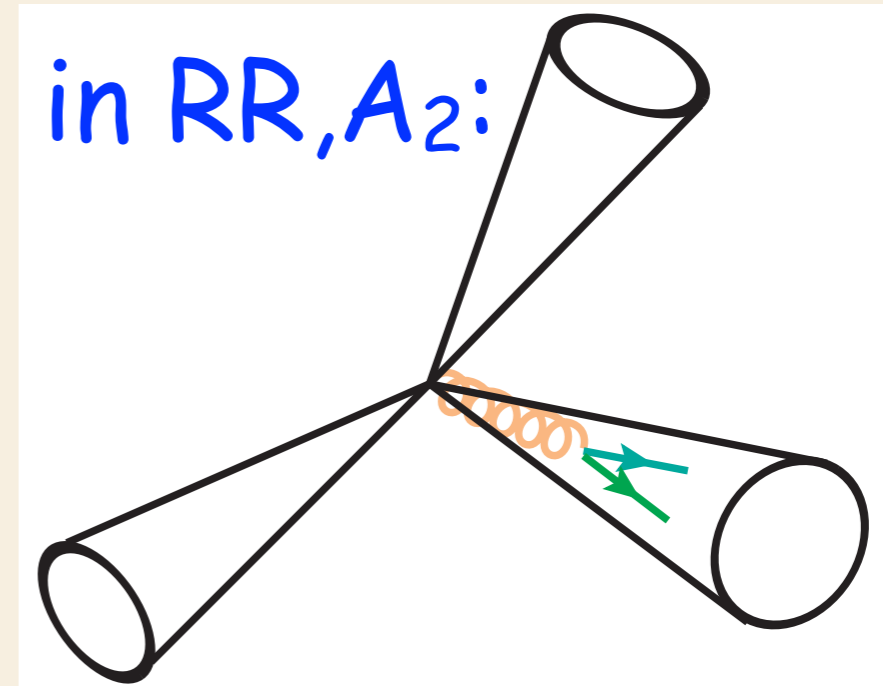
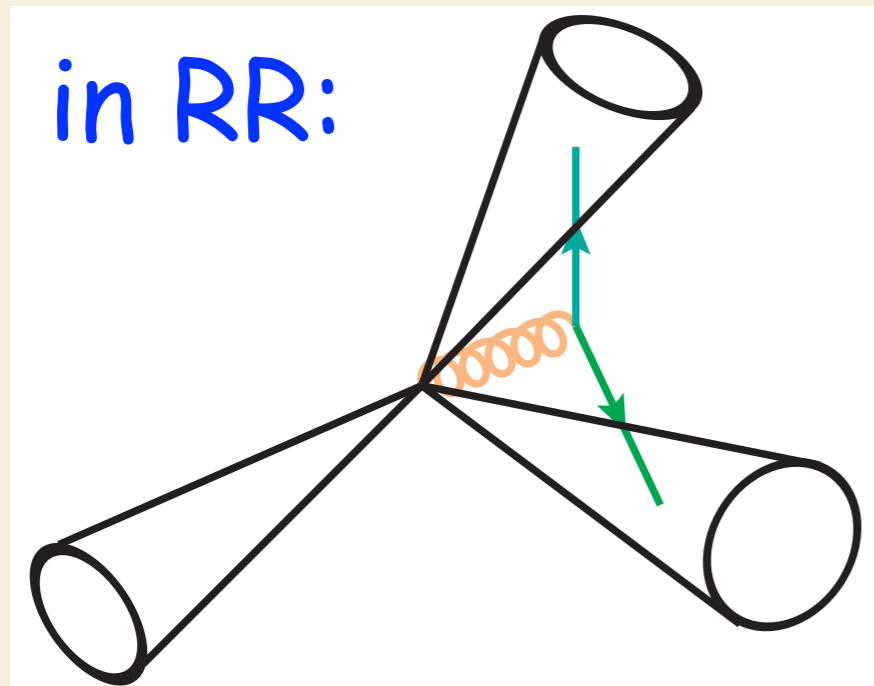
in RR, A_2 :



IR safe predictions w flavour- k_{\perp}

At NNLO accuracy the Durham algorithm is not infrared safe if the jet is tagged because **soft gluon splitting can spoil the flavor**

of jets

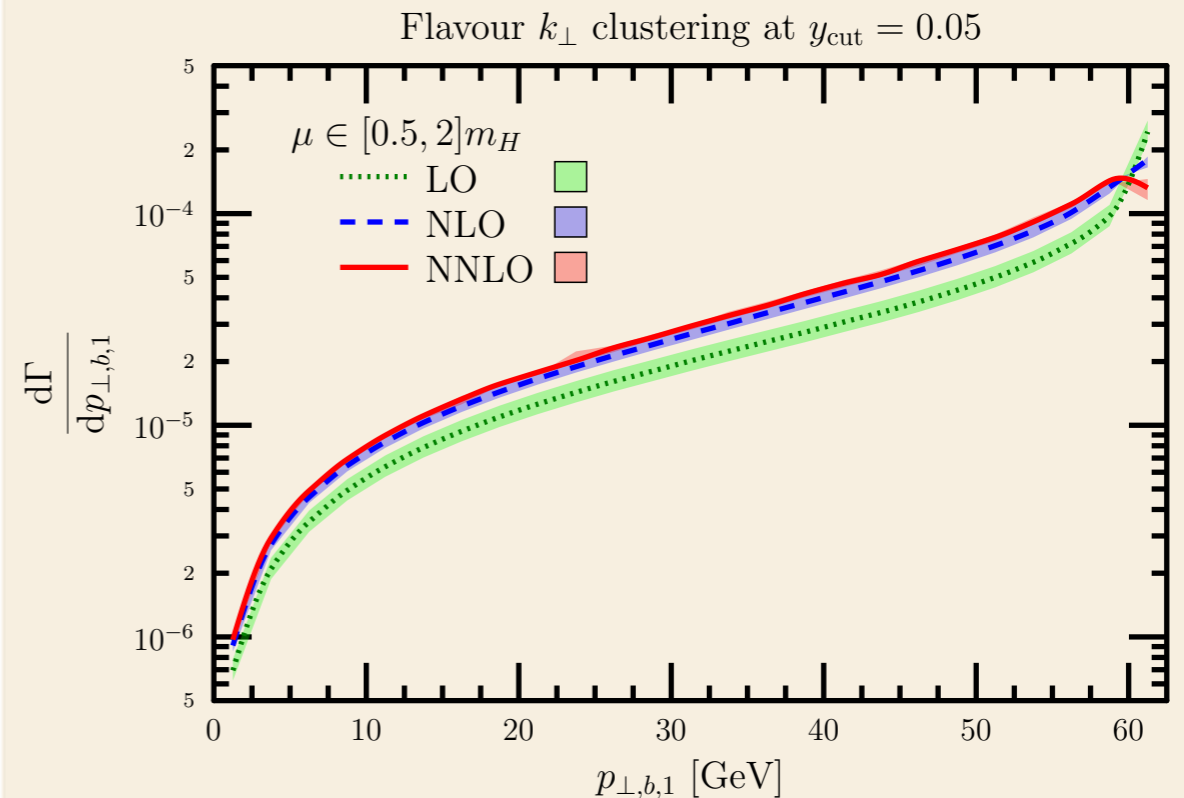
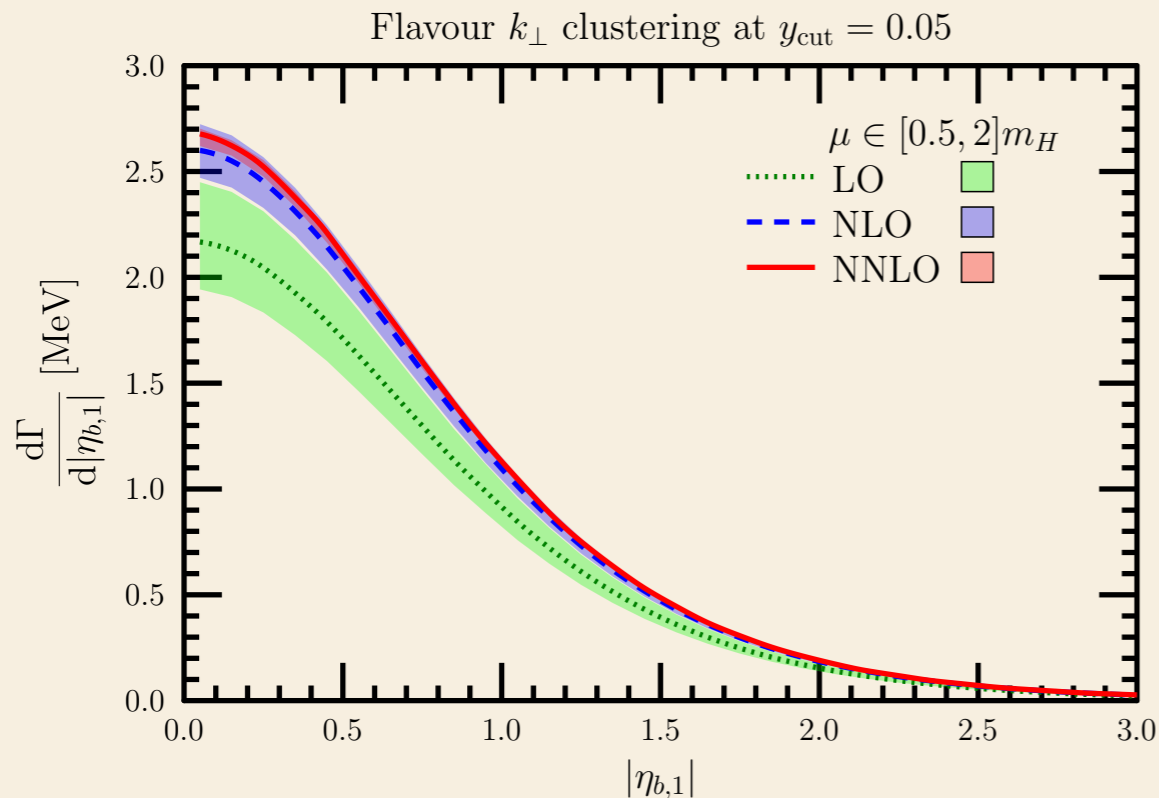


Possible solutions

- treat the b-quarks massive only in the parts of the Feynman graphs that contain the gluon splitting into a b-quark pair, while keeping $m_b = 0$ in the Hbb vertex
- Use flavour- k_{\perp} algorithm

A. Banfi et al hep-ph/0601139

IR safe predictions w flavour- k_{\perp}



rapidity distribution

of the leading b-jet in the rest frame of the Higgs boson.

jets are clustered using the flavour- k_{\perp} algorithm with $y_{\text{cut}} = 0.05$

p_T spectrum

Conclusions

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Conclusions

- ✓ Defined a general subtraction scheme for computing NNLO fully differential jet cross sections (presently only for processes with no colored particles in the initial state)
- ✓ Subtractions are
 - ✓ fully local
 - ✓ exact and explicit in color (using color state formalism)
- ✓ Demonstrated the cancellation of ϵ -poles
 - ✓ analytically (numerically for constrained subtractions)
- ✓ First application: Higgs-boson decay into a b-quark pair (combining with production at NNLO in progress)