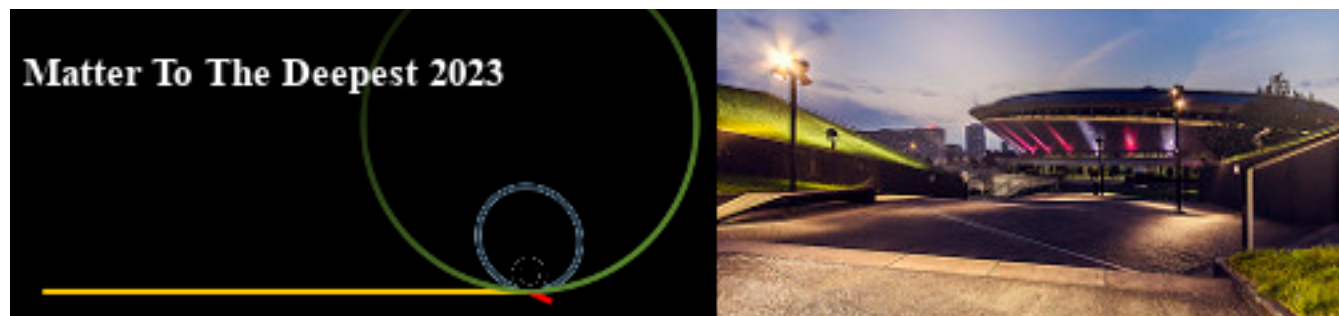


# STATUS OF THE SUPERWEAK EXTENSION OF THE STANDARD MODEL AND MUON $g - 2$

based on

arXiv:1812.11189 (*Symmetry*), 1911.07082 (*PRD*), 2104.11248 (*JCAP*), 2104.14571 (*PRD*), 2105.13360 (*J.Phys.G*), 2204.07100 (*PRD*), 2301.07961 (*JHEP*), 2301.06621 (*PRD*), 2305.11931 (*PRDL*) and correspondence with BMW collaboration  
with S. Iwamoto, T.J. Kärkkäinen, I. Nándori, Z. Péli, K. Seller, Zs. Szép

Ustron, 18 September, 2023



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# OUTLINE

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1. **Motivation**: status of particle physics
  - Colliders
  - Cosmology
  - **Muon anomalous magnetic moment** (on request by Janusz)
2. Superweak  $U(1)_Z$  extension of SM (**SWSM**)
3. Neutrino masses and dark matter candidate
4. Vacuum stability and scalar sector constraints
5. Contribution to  $M_W$  (**see talk by Zoltán Péli**)
6. Constraints from non-standard interactions
7. Conclusions



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# MOTTO

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*Rough estimates of BSM effects  
can easily be deceptive*

example: discovery of the Higgs particle came much faster than expected at the time of construction of the LHC because the

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- detector performance was
- theoretical prediction for Higgs production was significantly

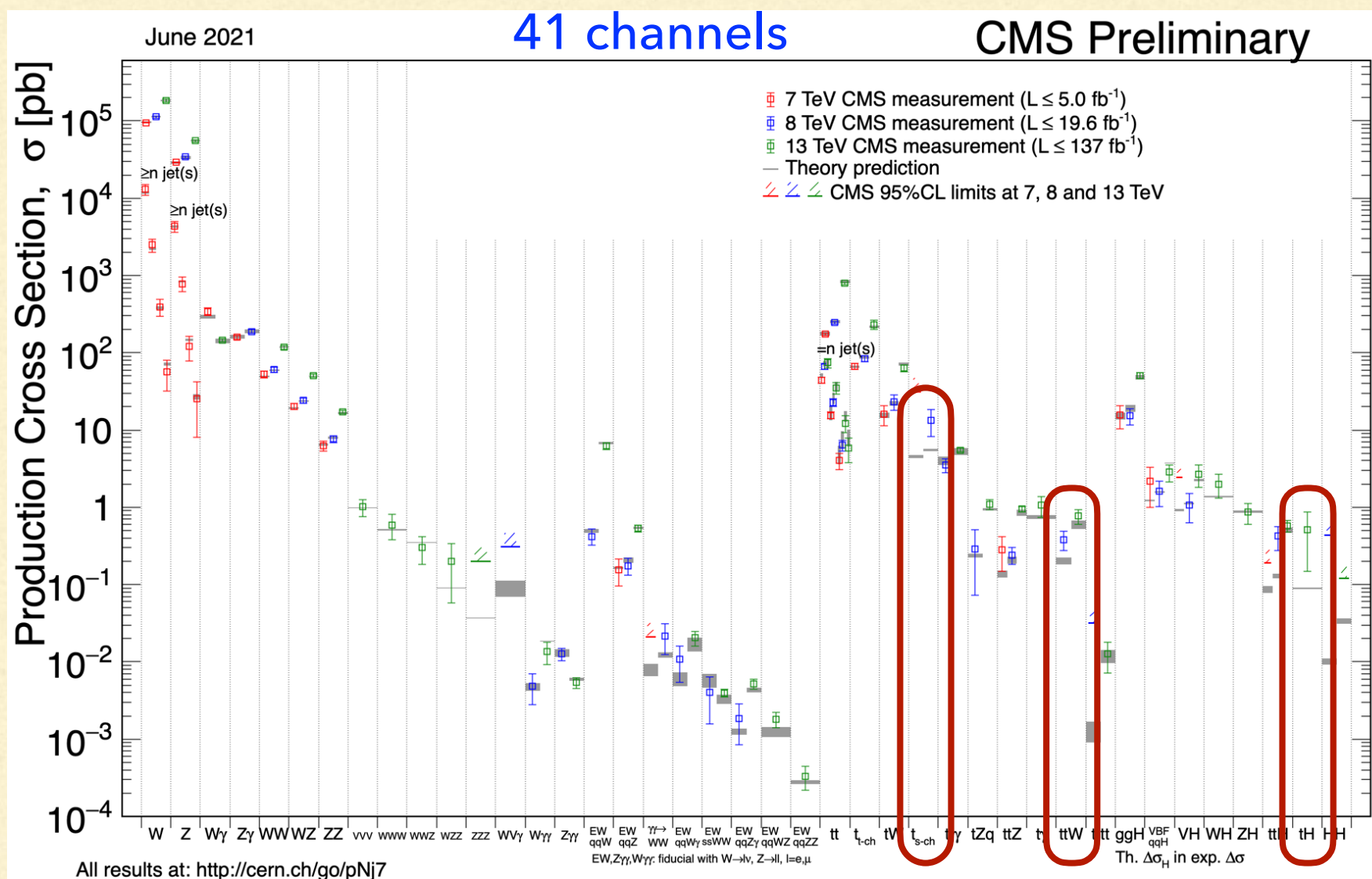
underestimated



# Status of particle physics: energy frontier

- Colliders: SM describes final states of particle collisions precisely [CM]

[CMS public]



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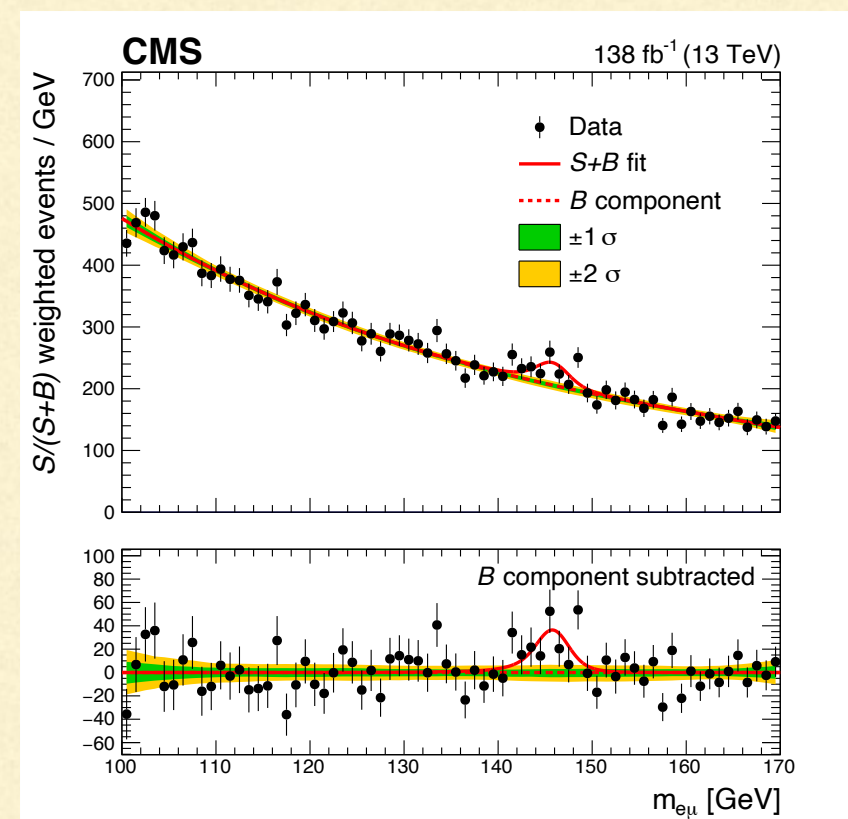


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$$pp \rightarrow X(= \text{new Higgs boson}) \rightarrow e^\pm \mu^\mp$$

[CMS preprint]



\*Exciting news keep popping up, **all below discovery significance yet**

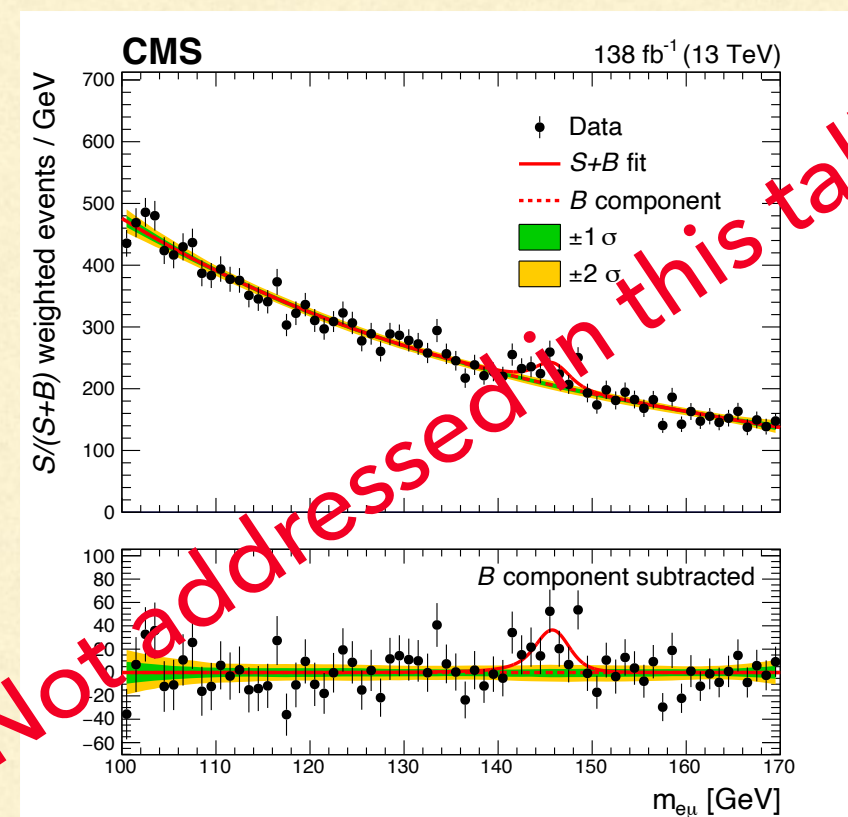


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# Status of particle physics: energy frontier

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- Colliders: SM describes final states of particle collisions precisely
- No proven sign of new physics beyond SM at colliders
- SM vacuum is metastable  
[Bezrukov et al, arXiv:1205.2893; Degrassi et al, arXiv:1205.6497]



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# Status of particle physics: cosmic and intensity frontiers

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- Universe at large scale described precisely by cosmological SM:  
 $\Lambda$ CDM ( $\Omega_m = 0.3$ )
- Neutrino flavours oscillate
- Existing baryon asymmetry cannot be explained by CP asymmetry in SM
- Inflation of the early, accelerated expansion of the present Universe

[<https://pdg.lbl.gov>]

Established observations require physics beyond SM,  
but do not suggest rich BSM physics



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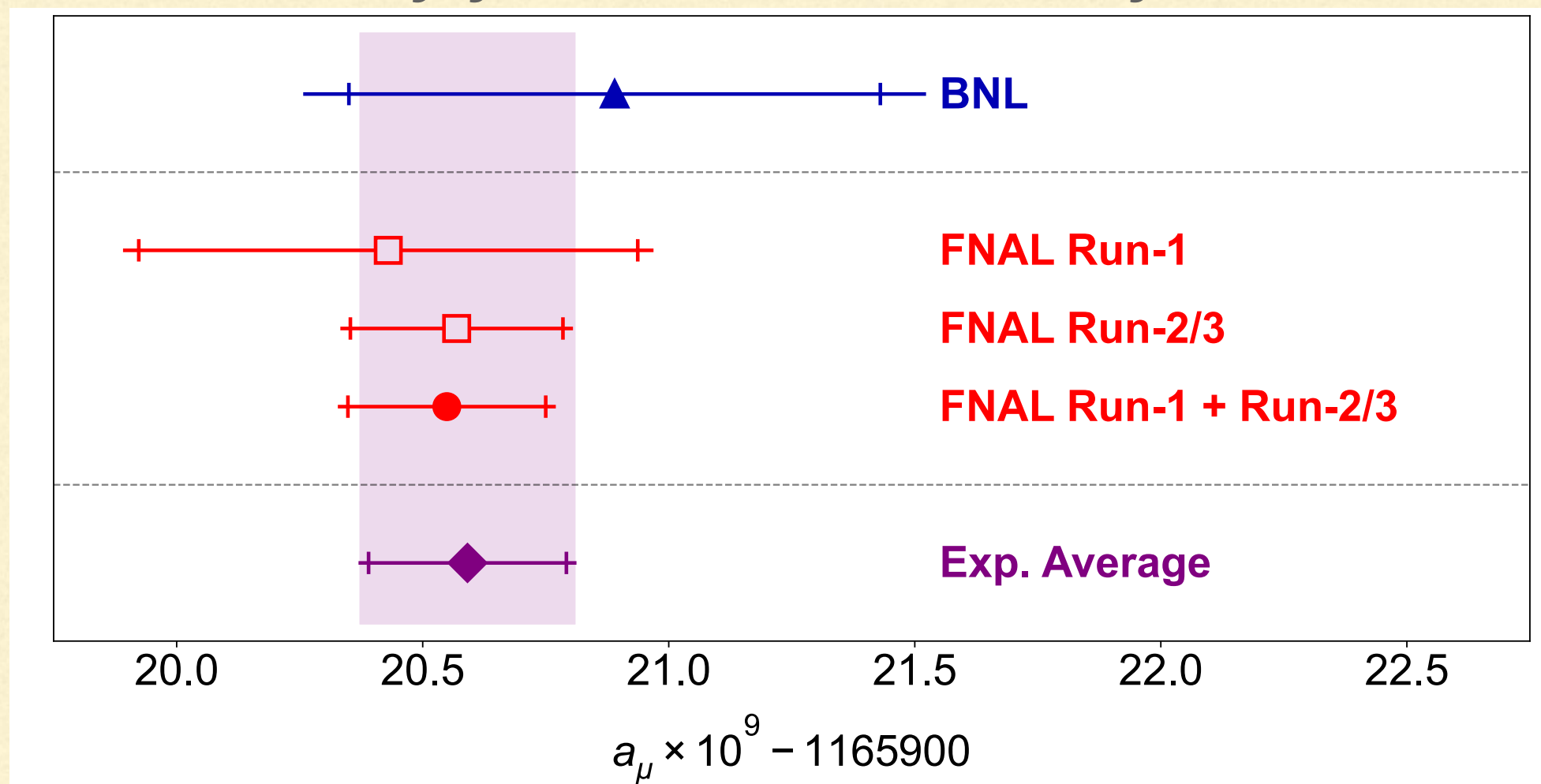
# Phenomenological approach to new physics

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Can we explain these observations,  
but not more,  
by the same model?

# Status of the muon anomalous magnetic moment: experiment

- The muon g-2 has been a smoking gun for new physics for many years, more recently:



[<https://muon-g-2.fnal.gov/result2023.pdf>]

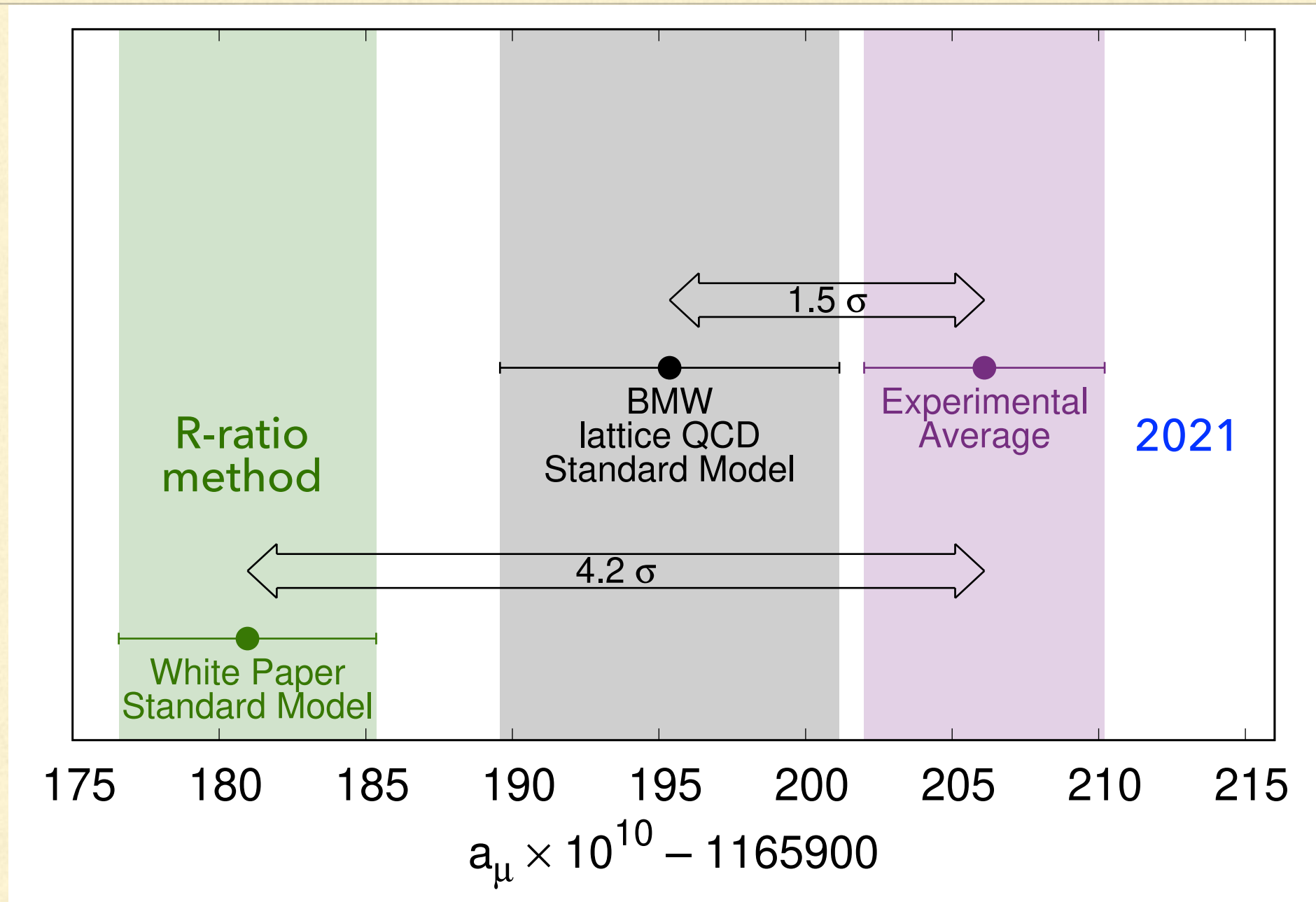


# Status of the muon anomalous magnetic moment: experiment

- The muon g-2 has been a smoking gun for new physics for many years
- The most precise experimental value is from FNAL (2023) :
$$a_{\mu} = \frac{g - 2}{2} = 116\,592\,055(24) \cdot 10^{-11} \quad (0.20 \text{ ppm})$$
- ...equivalent to a bathroom scale sensitive to a single eyelash:



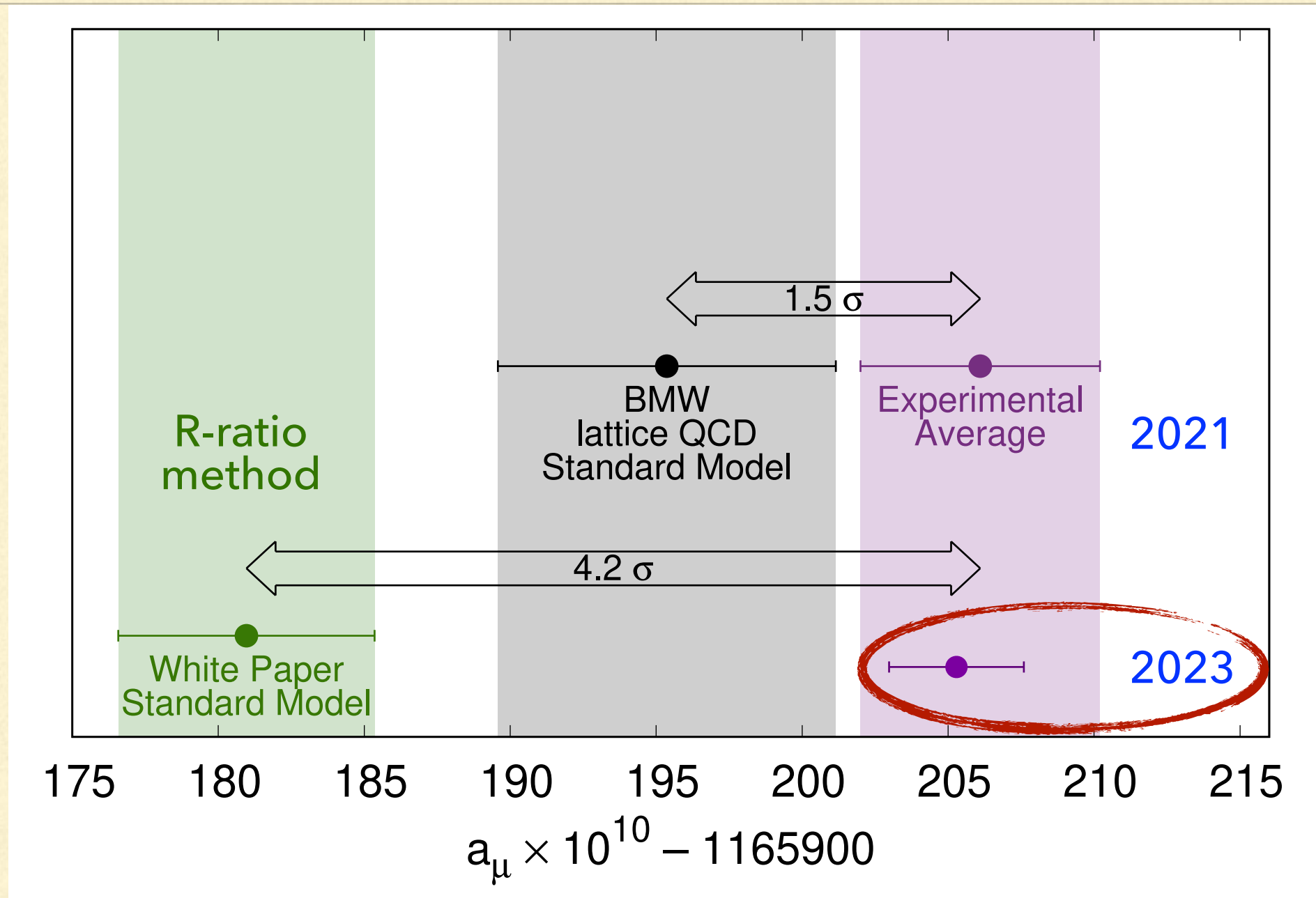
# Status of the muon anomalous magnetic moment: experiment vs. theory



[BMW compilation]



# Status of the muon anomalous magnetic moment: experiment vs. theory

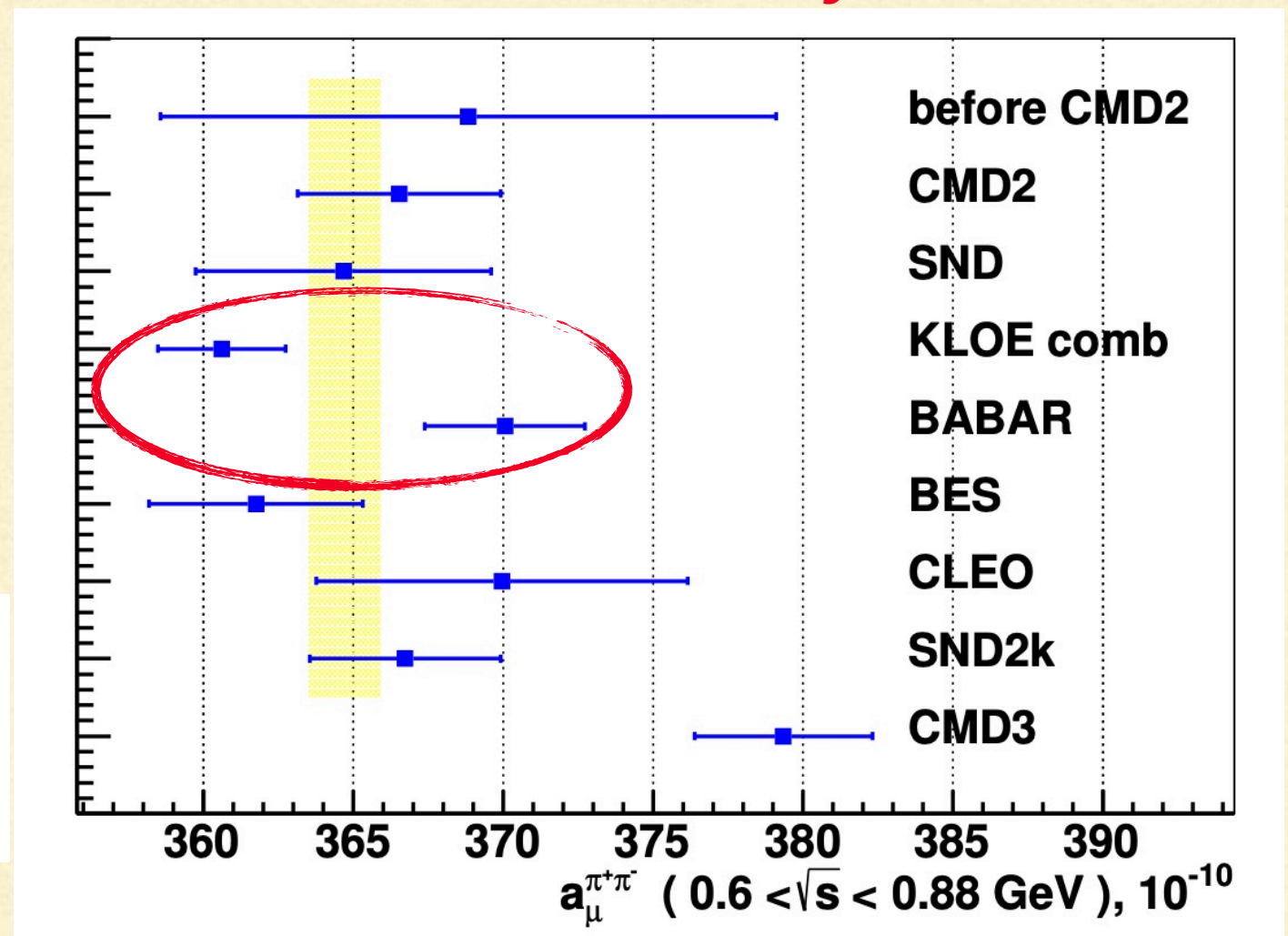
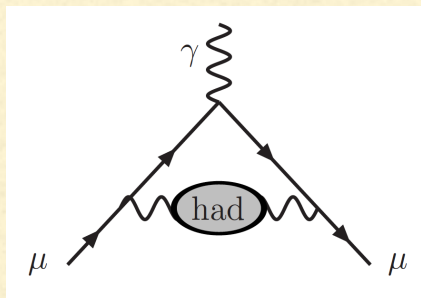


[BMW compilation]

# Status of the muon anomalous magnetic moment: theory with R-ratio

- The muon g-2 has been a smoking gun for new physics for many years, **but tension already in earlier data used for theory prediction:**

$\sigma(e^+e^- \rightarrow \pi^+\pi^-)$  cross section in this energy range gives **more than 50%** to total **HVP** contribution to  $a_\mu$



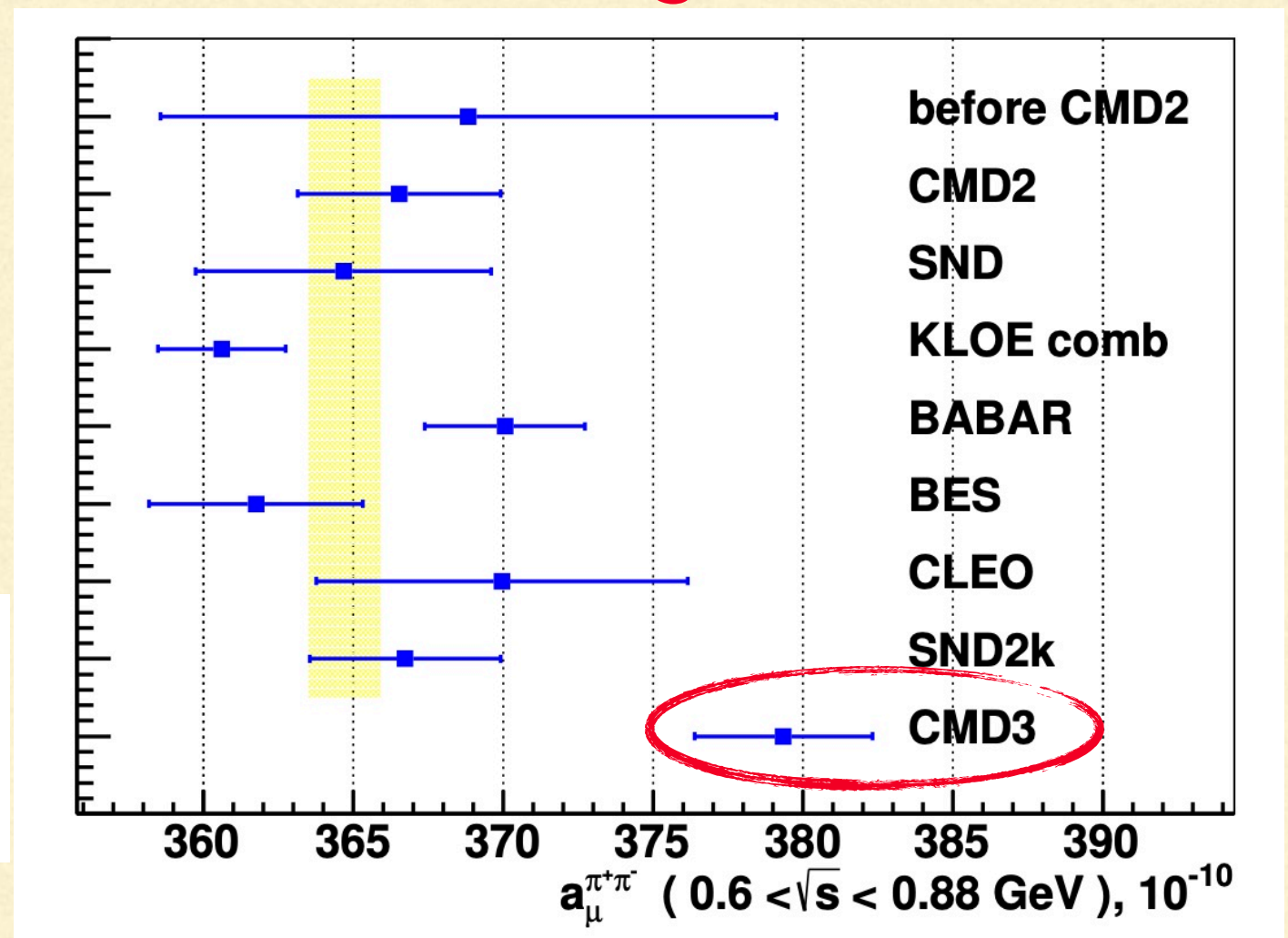
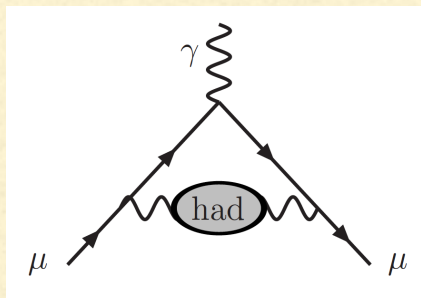
[BMW compilation]<sub>17</sub>



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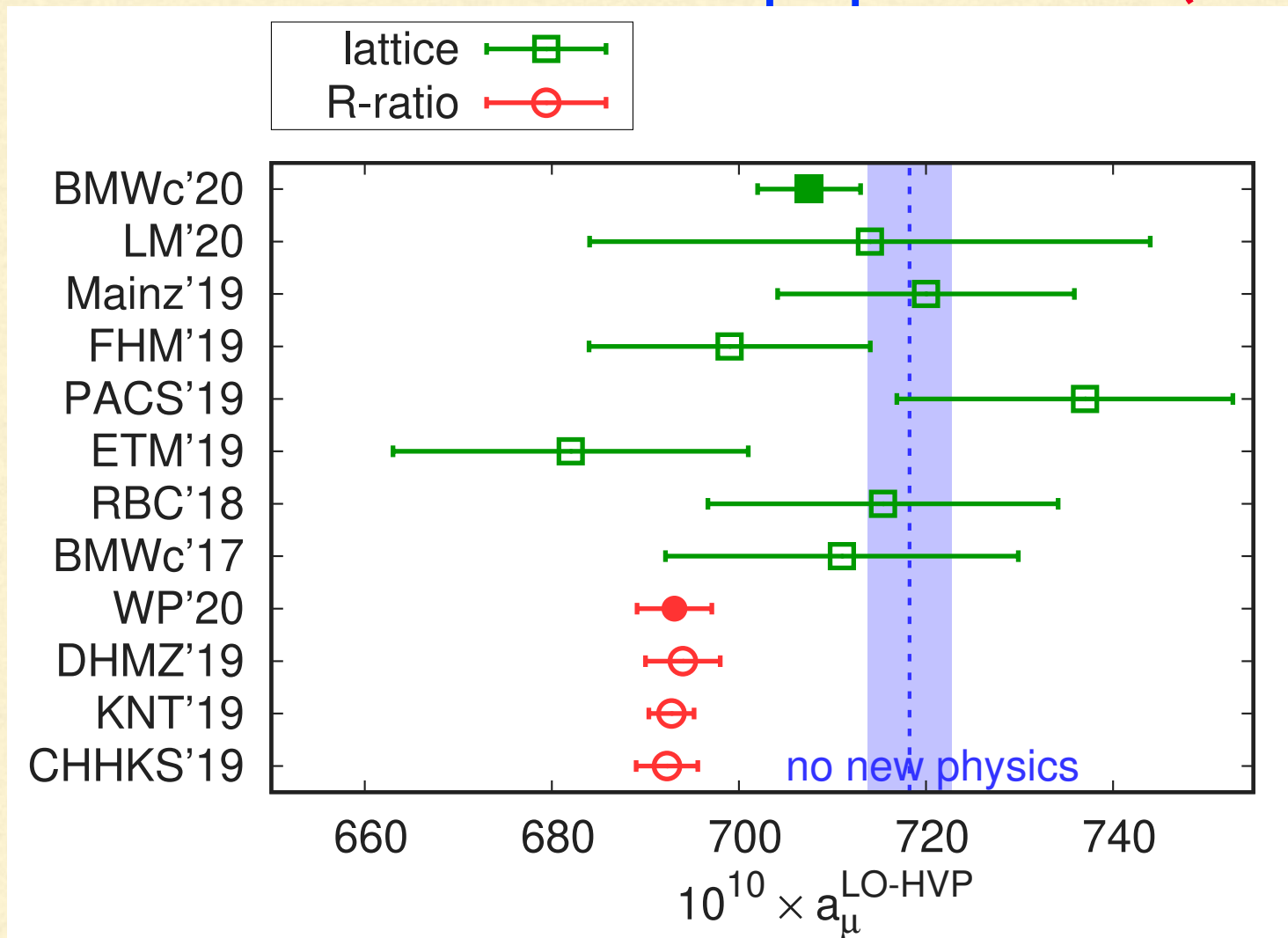
- New CMD3 data show a **~15 unit increase** in central value and **4.4 $\sigma$  tension** with old average:

$\sigma(e^+e^- \rightarrow \pi^+\pi^-)$  cross section  
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# Status of the muon anomalous magnetic moment: lattice vs. R-ratio

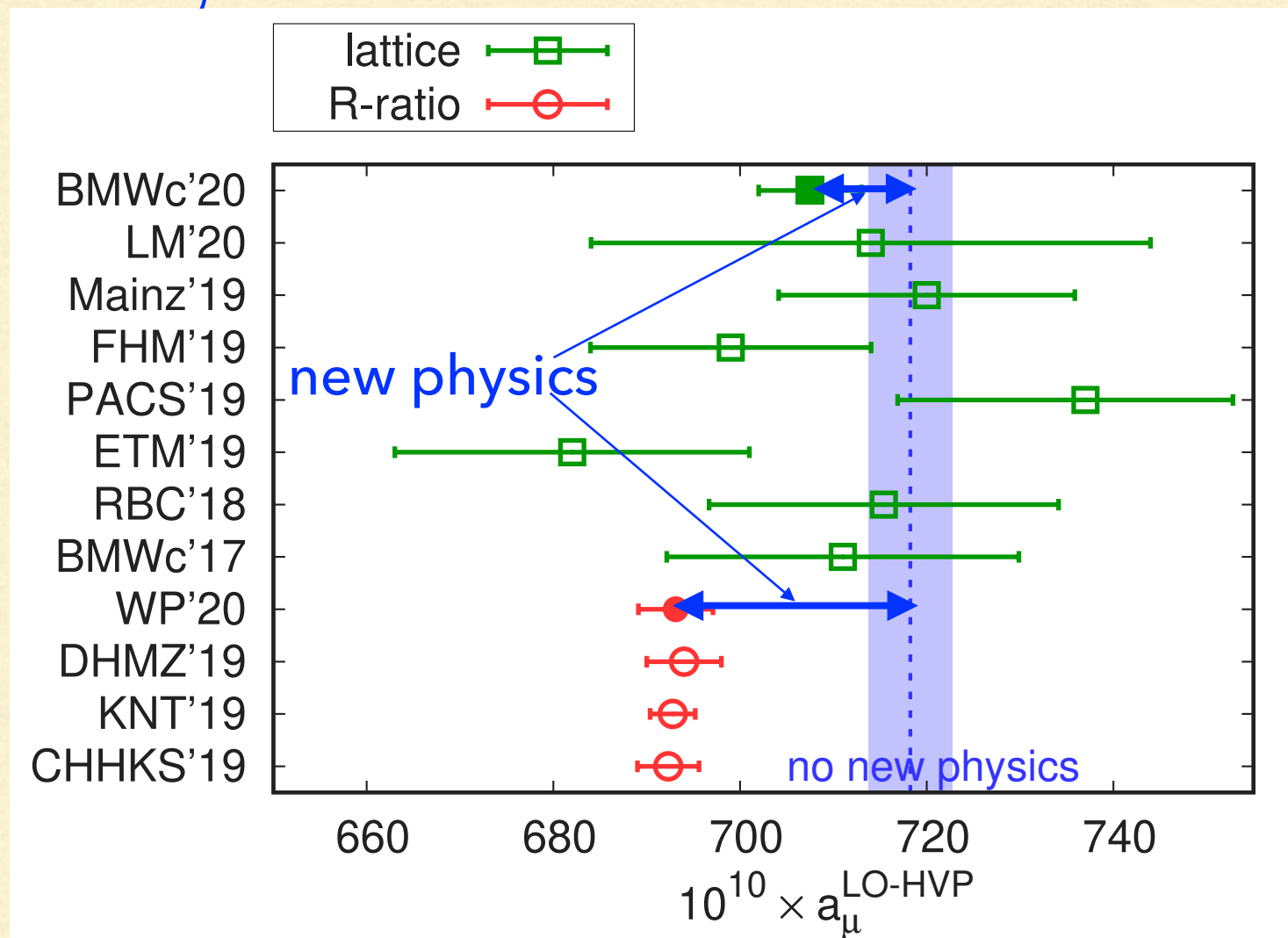
- Lattice:  $a_\mu^{\text{HVP}@LO} = 707.5(2.3)_{\text{stat}}(5.0)_{\text{sys}}[5.5]_{\text{tot}}$
- ~15 units above the R-ratio white paper value (a  $2.1\sigma$  tension)





# Message of the muon anomalous magnetic moment

- We are certain that there is new physics beyond the SM
- “Final word” on  $a_\mu$  will tell how BSM should affect the muon g-2



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# Status of the muon anomalous magnetic moment

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- The experimental result appears robust, only its uncertainty will reduce further
- Main task:
  - Resolve discrepancy between theory predictions
- Until then
  - everything else is speculation



# Muon anomalous magnetic moment: speculations with R-ratio result

- Generally **large**

$$\Delta a_{\mu}^{\text{BSM}} = C_{\text{BSM}} \frac{m_{\mu}^2}{M_{\text{BSM}}^2} \lesssim \text{O}(1) \frac{m_{\mu}^2}{M_{\text{BSM}}^2} \implies M_{\text{BSM}} \lesssim 2 \text{ TeV}$$

[Czarnecki, Marciano [hep-ph/0102122](#)]

can only be explained by rather **small masses** and/or **large couplings** and **enhanced chirality flips**

(the QFT operator corresponding to  $a_{\mu}$  connects left and right chirality muons),  
which can lead to

**conflicts with limits from LHC and dark matter experiments**

- Exhaustive study of single-, two- and three-field extensions shows that most of these are excluded

[Athron et al., [arXiv:2104.03691](#)]



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# Least constrained models

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- Some specific incomplete **three-field models** (2F1S, 2S1F) with large couplings [Athron et al., arXiv:[2104.03691](#)]



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  - **Bino-like LSP** and either slepton or chargino coannihilation
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- Muon chirality flip enhancements are related to the mass generation mechanism for the muon, so the **measurement of the Higgs-muon coupling at LHC or FCC can (will) provide further tests**
- **Planned JPARC g – 2 experiment and progress on theory prediction using results from the MUonE initiative should be decisive**



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# Muon anomalous magnetic moment: complying with lattice result

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- New physics should have a small (smaller than EW) contribution to  $a_\mu$
- May constrain the available parameter space, but unlikely to exclude a model compatible with ElectroWeak Precision Observables (EWPOs)



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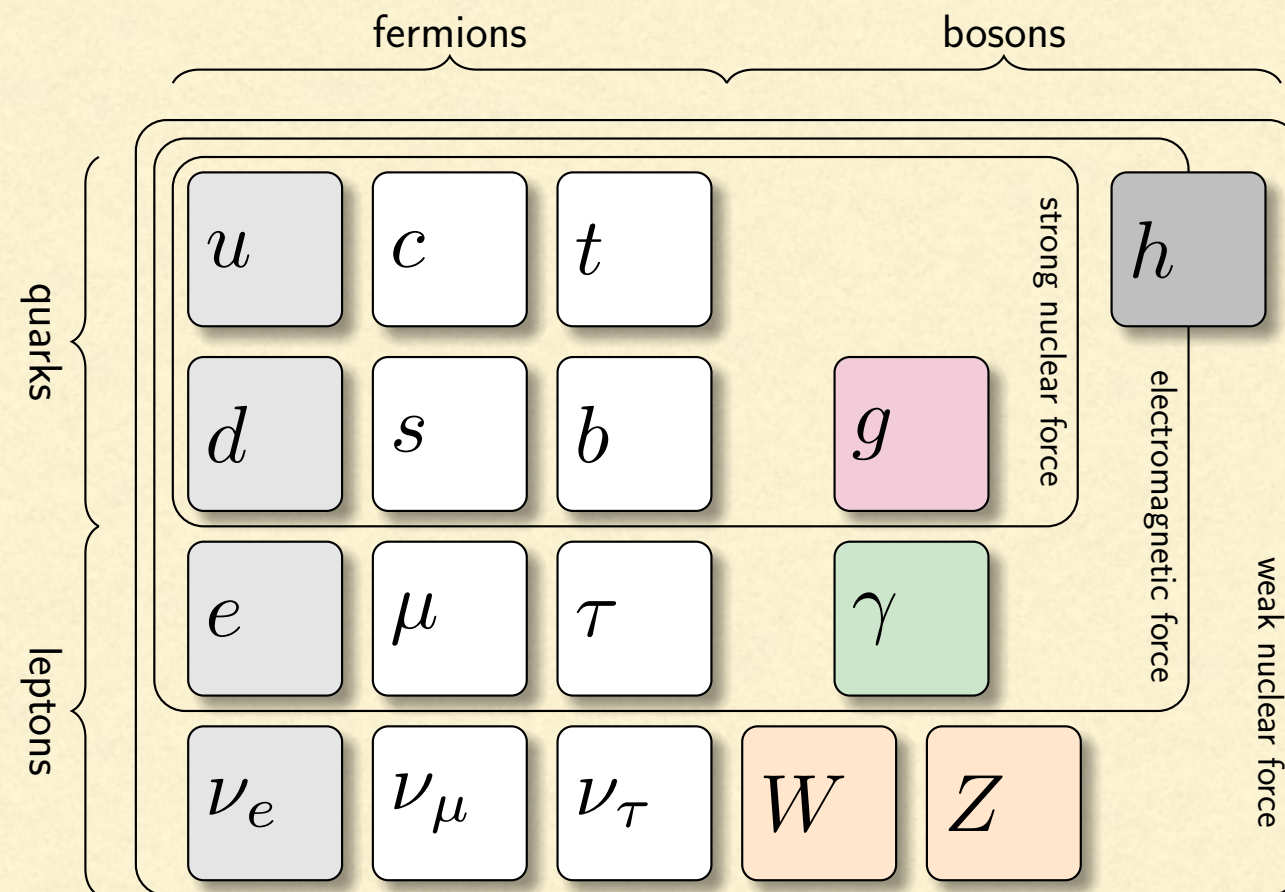
## Extension of SM: three alternatives with different **strength** and **weaknesses**

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- Effective field theory, such as **SMEFT**: **general** but **highly complex** (**2499** dim 6 operators), **focuses on new physics at high scales**
- Simplified models, such as **dark photon**, **extended scalar sector** or **right-handed neutrinos**: “**easily accessible**” **phenomenology**, but focus on specific aspect of new physics, so **cannot explain all BSM phenomena**
- UV complete extension with **potential of explaining BSM phenomena within a single model** such as **Superweak** extension of the **Standard Model**: **SWSM**

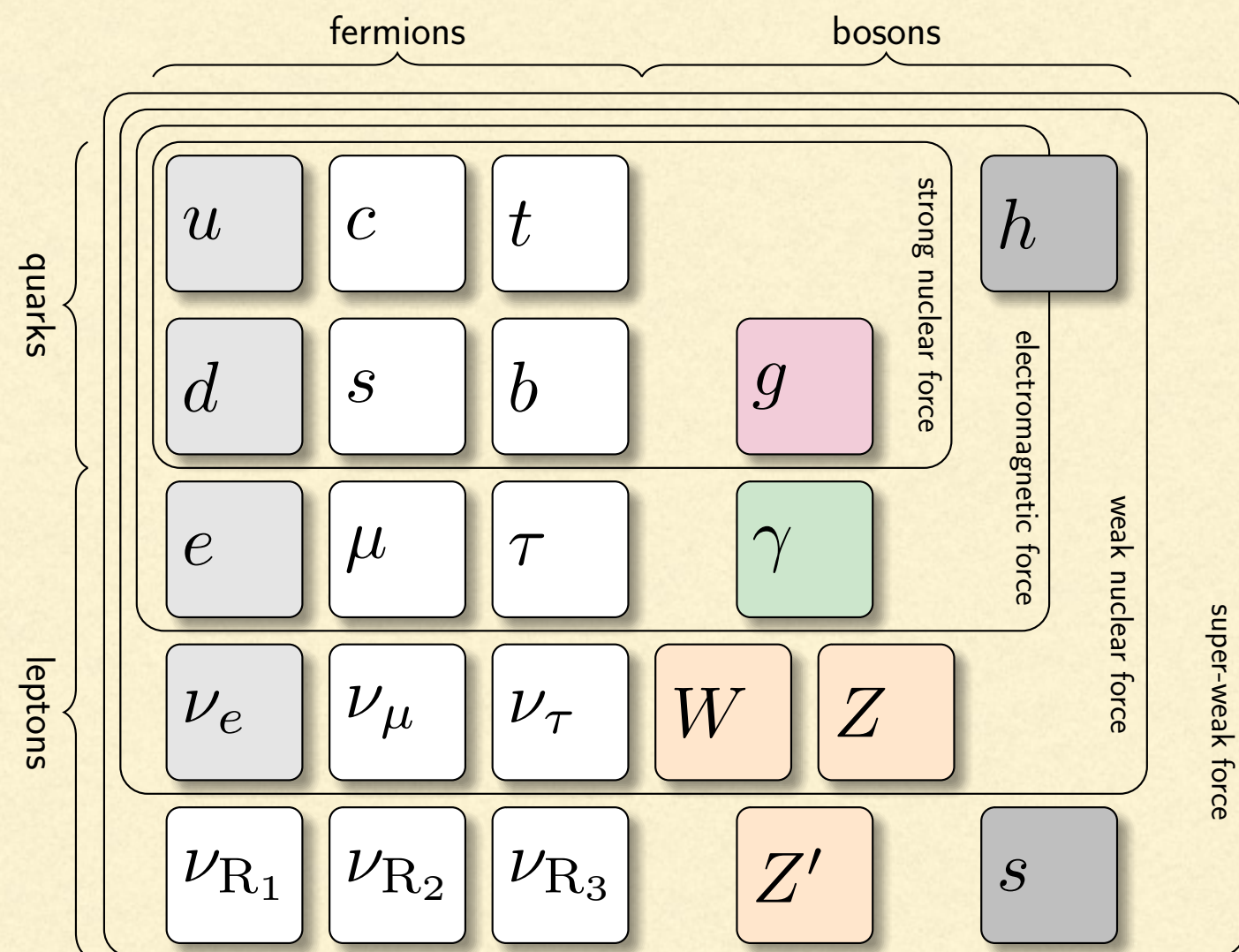


# Particle content of SM





# Particle content of SWSM (take-home picture)





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# Superweak extension of SM (SWSM)

---

- Symmetry of the Lagrangian: local  
 $G = G_{\text{SM}} \times U(1)_Z$  with  $G_{\text{SM}} = SU(3)_c \times SU(2)_L \times U(1)_Y$   
renormalizable gauge theory, including all dim 4  
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renormalizable gauge theory, including all dim 4 operators allowed by  $G$
- z-charges fixed by requirement of
  - gauge and gravity **anomaly cancellation** and
  - **gauge invariant Yukawa terms for neutrino mass generation**



# Mixing in the neutral gauge sector

$$\begin{pmatrix} B_\mu \\ W_\mu^3 \\ B'_\mu \end{pmatrix} = \begin{pmatrix} c_W & -s_W & 0 \\ s_W & c_W & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_Z & -s_Z \\ 0 & s_Z & c_Z \end{pmatrix} \begin{pmatrix} A_\mu \\ Z_\mu \\ Z'_\mu \end{pmatrix} \quad \begin{aligned} c_X &= \cos \theta_X \\ s_X &= \sin \theta_X \end{aligned}$$

where  $\theta_W$  is the weak mixing angle &  $\theta_Z$  is the  $Z - Z'$  mixing, implicitly:

$\tan(2\theta_Z) = -2\kappa / (1 - \kappa^2 - \tau^2)$ , with  $\kappa$  and  $\tau$  effective couplings,  
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The expressions for the neutral gauge boson masses are somewhat cumbersome, but exists a nice, **compact generalization** of the **SM**

mass-relation formula:  $\frac{M_W^2}{c_W^2} = c_Z^2 M_Z^2 + s_Z^2 M_{Z'}^2$



## Scalars in the SWSM

- Standard  $\phi$  complex  $SU(2)_L$  doublet and new  $\chi$  complex singlet:

$$\mathcal{L}_{\phi,\chi} = [D_{\mu}^{(\phi)} \phi]^* D^{(\phi)\mu} \phi + [D_{\mu}^{(\chi)} \chi]^* D^{(\chi)\mu} \chi - V(\phi, \chi)$$

- with scalar potential

$$V(\phi, \chi) = V_0 - \mu_{\phi}^2 |\phi|^2 - \mu_{\chi}^2 |\chi|^2 + (|\phi|^2, |\chi|^2) \begin{pmatrix} \lambda_{\phi} & \frac{\lambda}{2} \\ \frac{\lambda}{2} & \lambda_{\chi} \end{pmatrix} \begin{pmatrix} |\phi|^2 \\ |\chi|^2 \end{pmatrix}$$



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- After SSB,  $G \rightarrow SU(3)_c \times U(1)_{QED}$  in  $R_{\xi}$  gauge

$$\phi = \frac{1}{\sqrt{2}} \begin{pmatrix} -i\sqrt{2}\sigma^+ \\ v + h' + i\sigma_{\phi} \end{pmatrix} \quad \& \quad \chi = \frac{1}{\sqrt{2}} (w + s' + i\sigma_{\chi})$$



---

## Mixing in the scalar sector

---

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**5 (+1 less important) new parameters:**

- in **gauge** sector:  $\{\kappa \text{ and } \tau\}$  or  $\{\theta_Z \text{ and } M_{Z'}\}$   
(+a mixing coupling)
- in **scalar** sector:  $\{w, \lambda_\chi \text{ and } \lambda\}$  or  $\{M_S, \theta_S \text{ and } \lambda\}$



## After SSB neutrino mass terms appear

$$-\mathcal{L}_Y^\ell = \frac{w + s' + i\sigma_\chi}{2\sqrt{2}} \bar{\nu}_R^c \mathbf{Y}_N \nu_R + \frac{v + h' - i\sigma_\phi}{\sqrt{2}} \bar{\nu}_L \mathbf{Y}_\nu \nu_R + \text{h.c.}$$

$$\mathbf{M}_N = \frac{w}{\sqrt{2}} \mathbf{Y}_N$$

$$\mathbf{M}_D = \frac{v}{\sqrt{2}} \mathbf{Y}_\nu$$

- In flavour basis the full **6×6 mass matrix** reads  $\mathbf{M}' = \begin{pmatrix} \mathbf{0}_3 & \mathbf{M}_D^T \\ \mathbf{M}_D & \mathbf{M}_N \end{pmatrix}$



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- Dirac and Majorana mass terms appear already at tree level by SSB (not generated radiatively)
- Quantum corrections to active neutrinos are not dangerous  
[Iwamoto et al, [arXiv:2104.14571](https://arxiv.org/abs/2104.14571)]



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# Expected consequences (take-home messages)

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- Dirac and Majorana neutrino mass terms are generated by the SSB of the scalar fields, providing the origin of neutrino masses and oscillations  
[Iwamoto, Kärkäinen, Péli, ZT, arXiv:[2104.14571](#); Kärkkäinen and ZT, arXiv:[2105.13360](#)]
- The lightest new particle is a natural and viable candidate for WIMP dark matter if it is sufficiently stable [Seller, Iwamoto and ZT, arXiv:[2104.11248](#)]
- Diagonalization of neutrino mass terms leads to the PMNS matrix, which in turn can be the source of leptogenesis  
[Seller, Szép, ZT, arXiv:[2301.07961](#) talk by Károly Seller on Sunday and under investigation]
- The second scalar together with the established BEH field can stabilize the vacuum and be related to the accelerated expansion now and inflation in the early universe  
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# Dark matter candidate

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- **Assume that the DM has particle origin**



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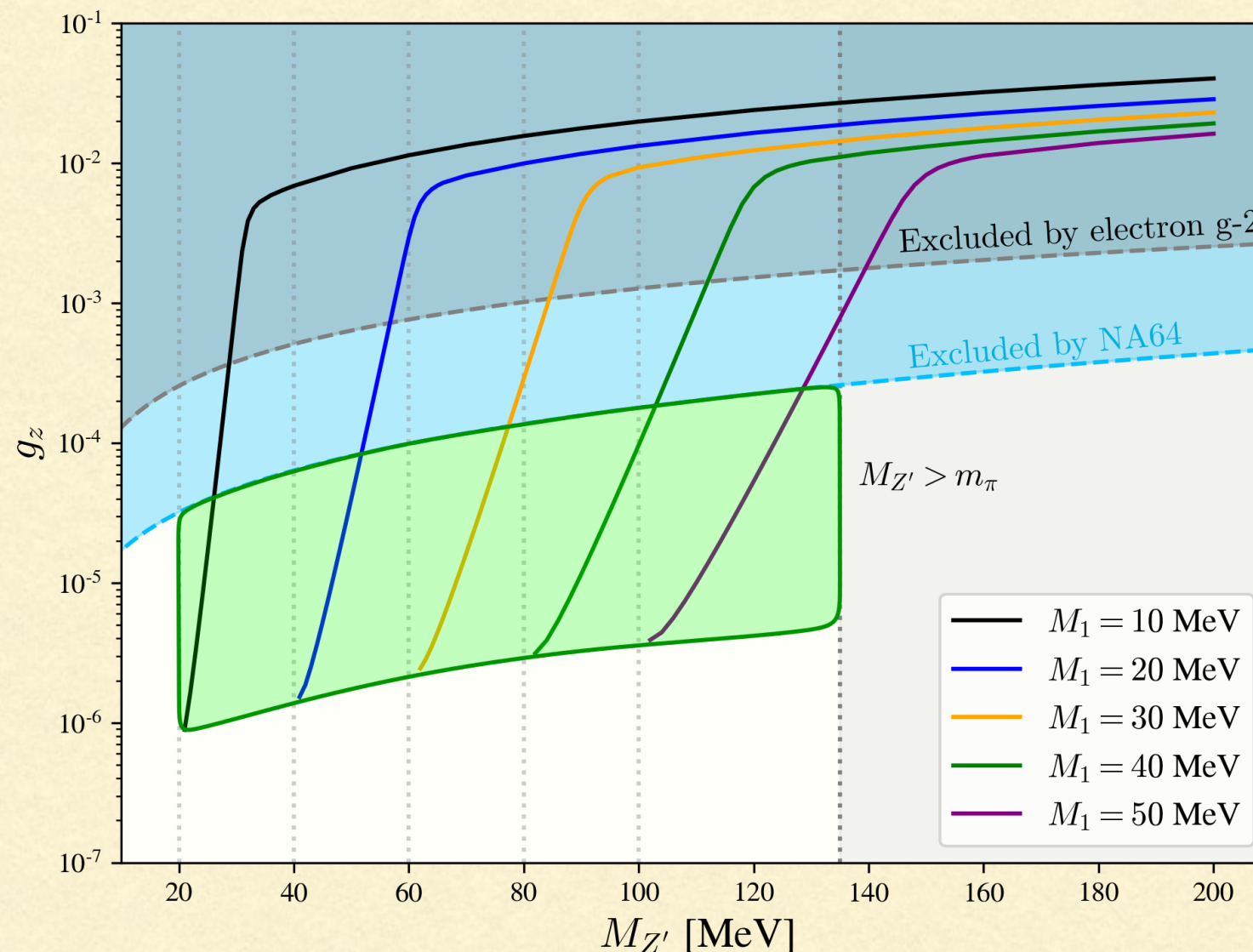
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- Assume that the DM has particle origin
- Only chance to observe such a particle if it **interacts with the SM particles, which needs a portal**  
In the superweak model the vector boson portal  $Z'$  with the lightest sterile neutrino  $\nu_4$  as dark matter candidate is a natural scenario (Higgs portal exists, but negligible)



# Parameter space for the freeze-out scenario of dark matter production in the SWSM



It is essential for the SWSM DM candidate that the resonance in  $\text{SM}+\text{SM} \rightarrow Z' \rightarrow \text{DM}+\text{DM}$  can dominate the integral in the rate



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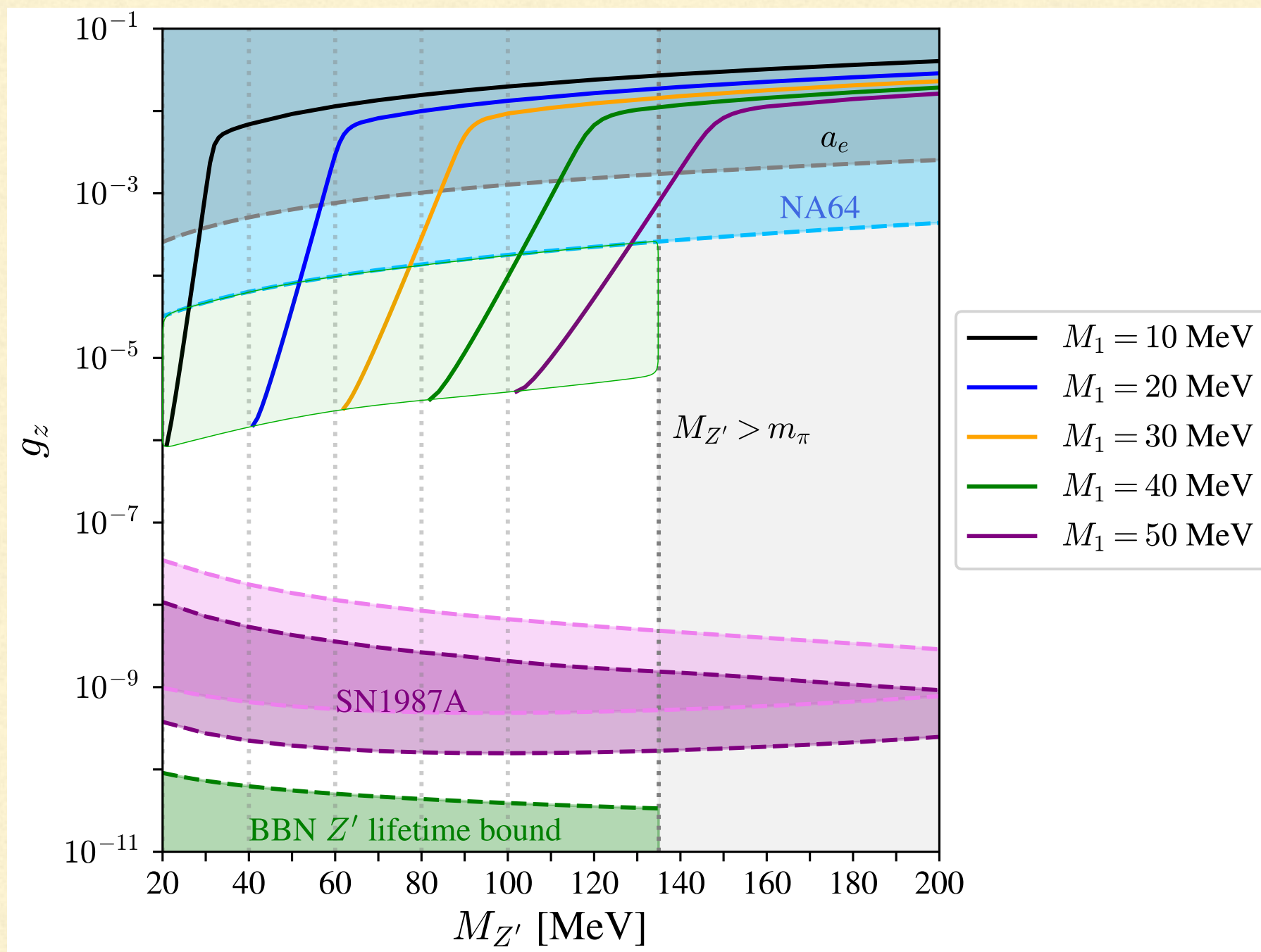
# Experimental constraints

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- **Anomalous magnetic moment** of electron and muon
  - $Z'$  couples to leptons modifying the magnetic moment
  - Constraints on  $(g - 2)$  translate to upper bounds on the coupling  $g_z(M_{Z'})$
- **NA64 search for missing energy events**
  - **Strict upper bounds** on  $g_z(M_{Z'})$  for any U(1) extension (dark photons)
- **Supernova constraints** based on SN1987A
  - Constraints are based on comparing observed and calculated neutrino fluxes
- **Big Bang Nucleosynthesis** provides **constraints on new particles**
  - New particles should have negligible effects during BBN
  - Meson production can be dangerous close to BBN
- Further constraints are due to **CMB, solar cooling, beam dump experiments** etc.



# Cosmological constraints on the freeze-out scenario of dark matter production in the SWSM





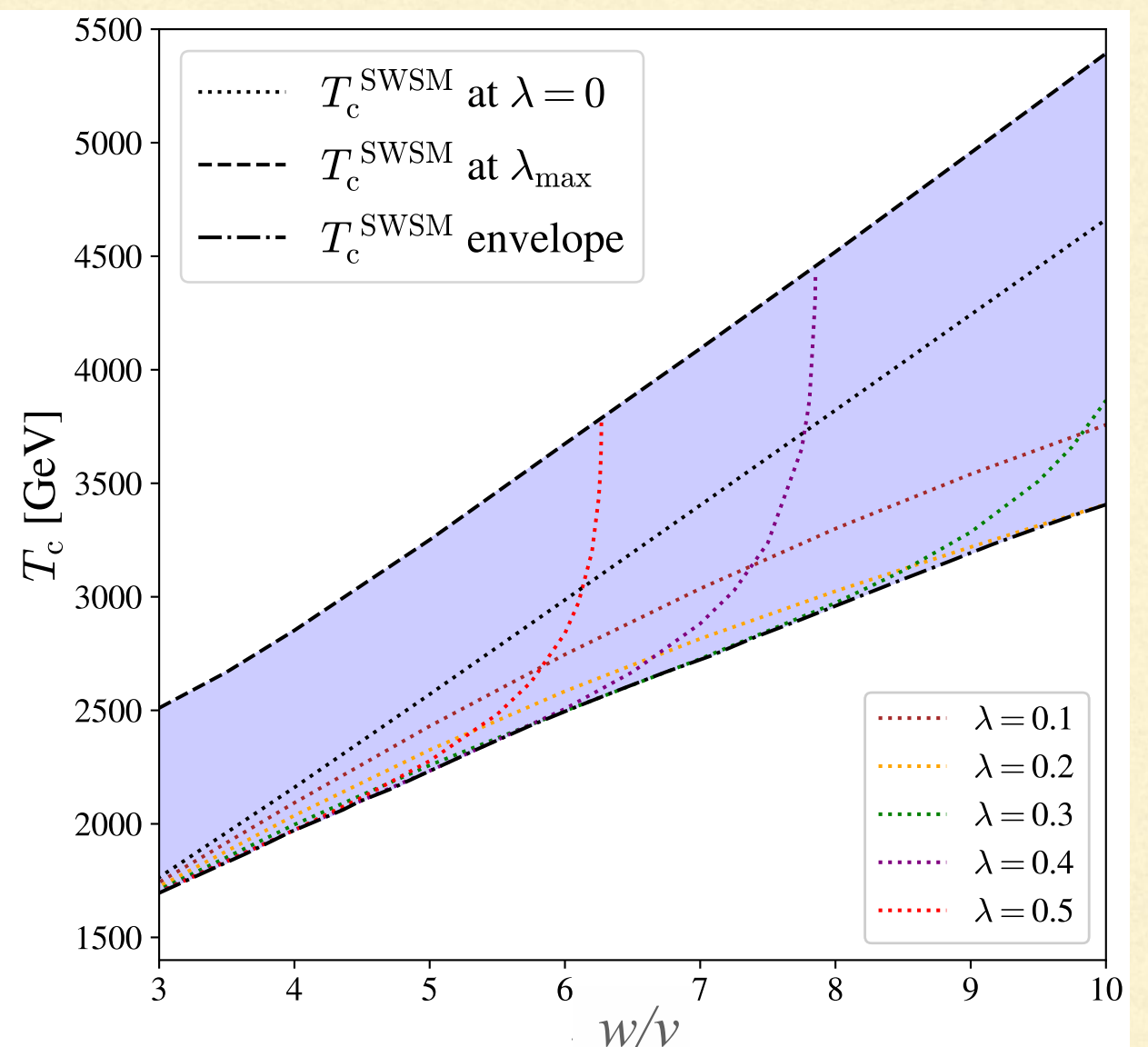
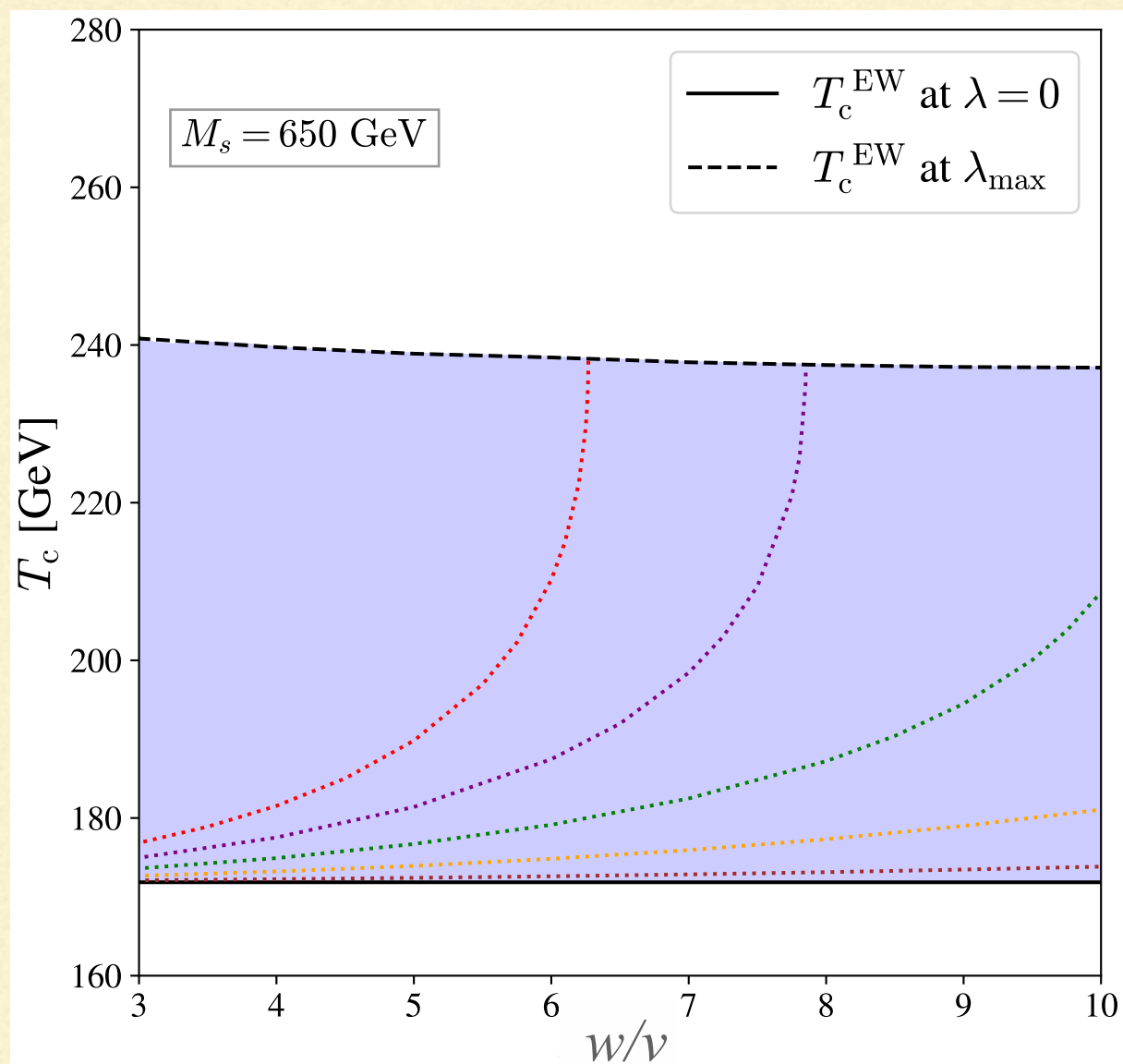
# Expected consequences (take-home messages)

- Dirac and Majorana neutrino mass terms are generated by the SSB of the scalar fields, providing the origin of neutrino masses and oscillations  
[Iwamoto, Kärkäinen, Péli, ZT, arXiv:[2104.14571](#); Kärkkäinen and ZT, arXiv:[2105.13360](#)]
- The lightest new particle is a natural and viable candidate for WIMP dark matter if it is sufficiently stable  
[Seller, Iwamoto and ZT, arXiv:[2104.11248](#)]
- Diagonalization of neutrino mass terms leads to the PMNS matrix, which in turn can be the source of leptogenesis  
[Seller, Szép, ZT, arXiv:[2301.07961](#), talk by Károly Seller on Friday and under investigation]
- The second scalar together with the established BEH field can stabilize the vacuum and be related to the accelerated expansion now and inflation in the early universe  
[Péli, Nándori and ZT, arXiv:[1911.07082](#); Péli and ZT, arXiv:[2204.07100](#)]



# Prerequisite: phase-transition temperatures in the SWSM (see Károly Seller's talk on Friday)

$U(1)_Z$  is broken earlier than  $SU(2)_L \times U(1)_Y$





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# Expected consequences (take-home messages)

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SWSM has the potential of explaining all known results beyond the SM



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# Main questions

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Is there a non-empty region of the parameter space where all these promises are fulfilled?



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Present focus:

Is there a non-empty region of the parameter space where all these promises are fulfilled?

Can we predict any new phenomenon observable by present or future experiments?



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# Important test

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Once the allowed region of the parameter space for fulfilling the expectations is understood

the observation of the  $Z'$  or  $S$  in the allowed region

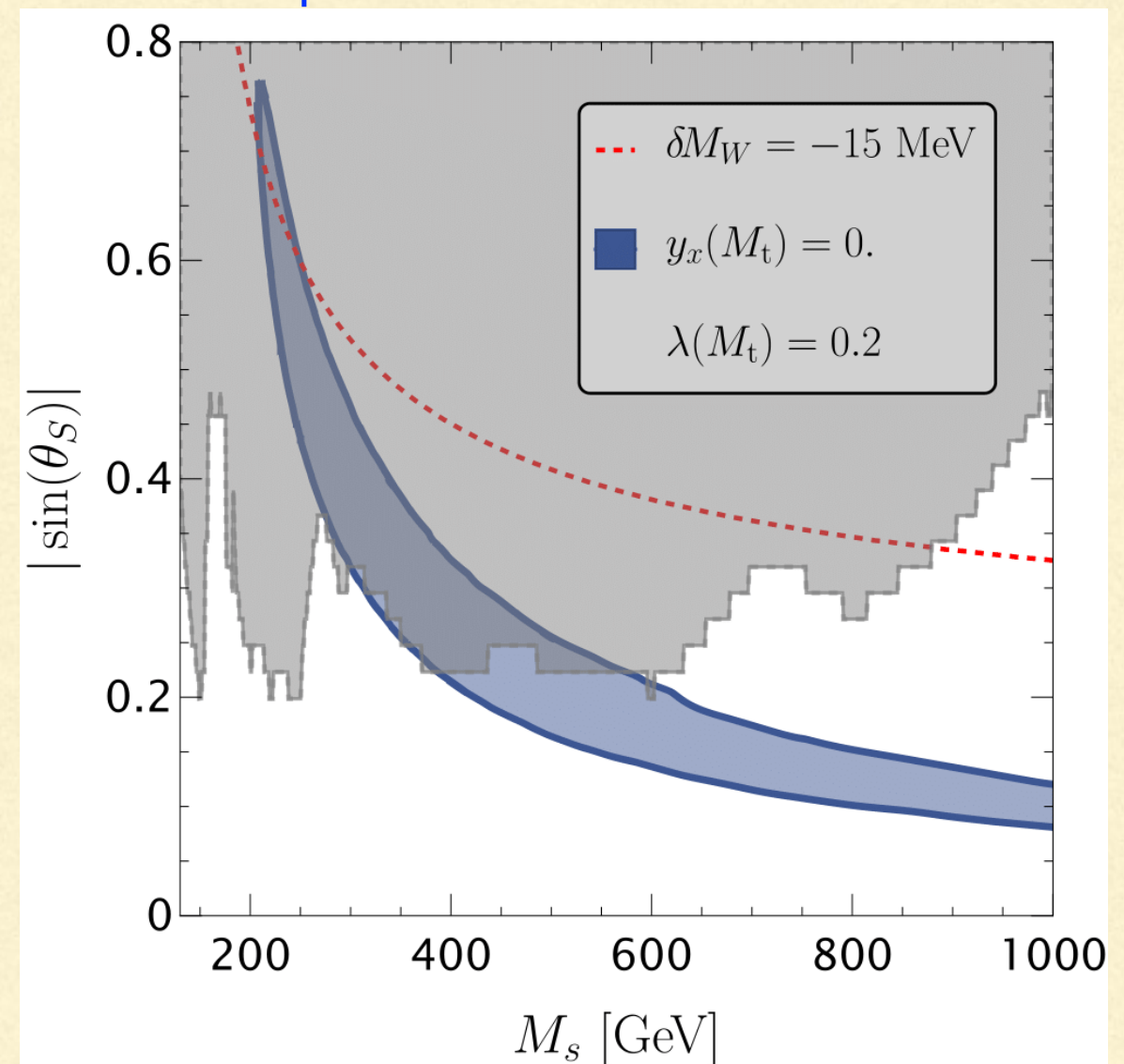
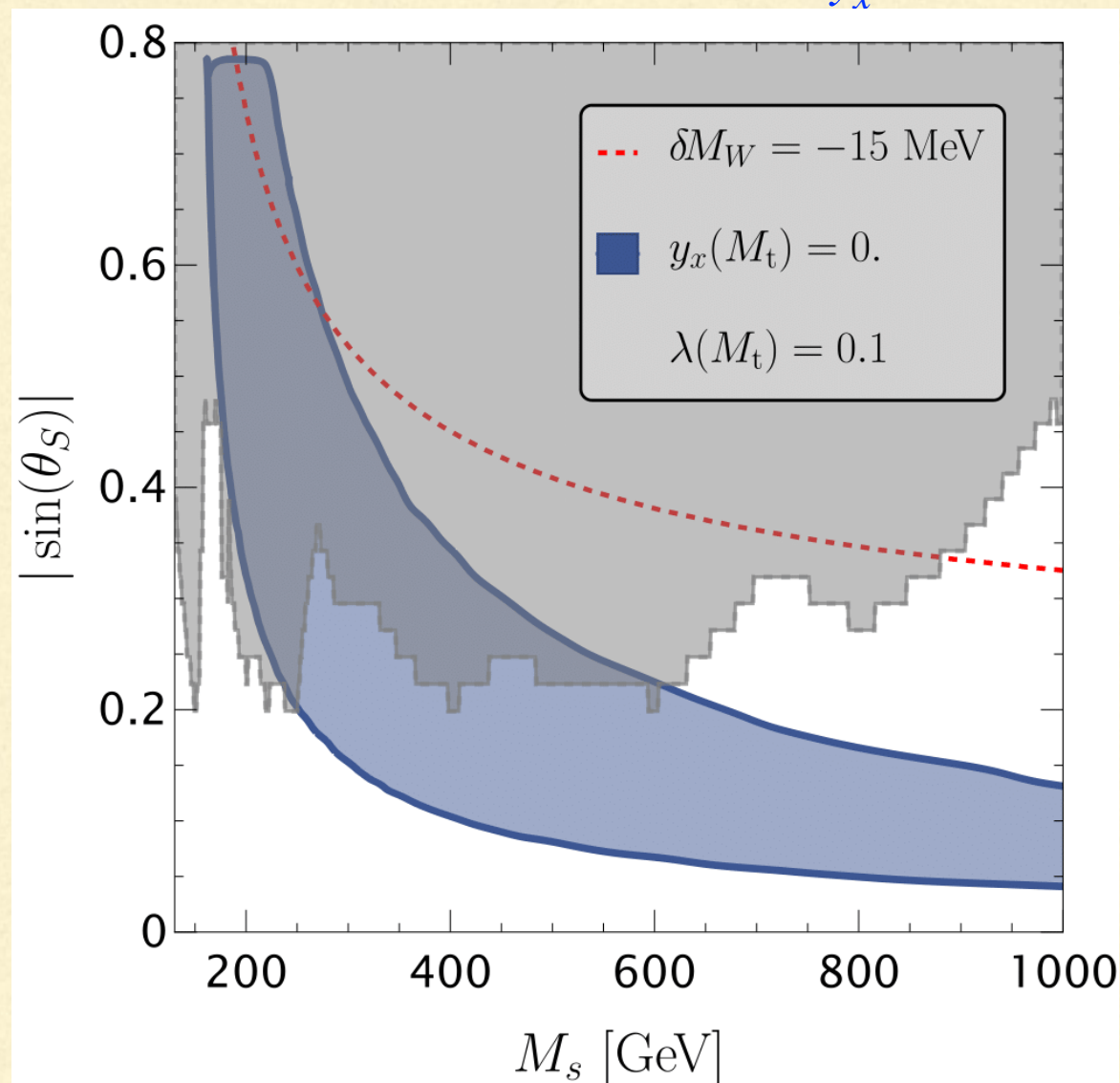


# Experimental constraints in the scalar sector from direct searches and $M_W$

■  $M_s > M_h$ :

[Zoltán Péli and ZT, arXiv: [2204.07100](#)]

$y_x = 0$ : scalar sector decouples

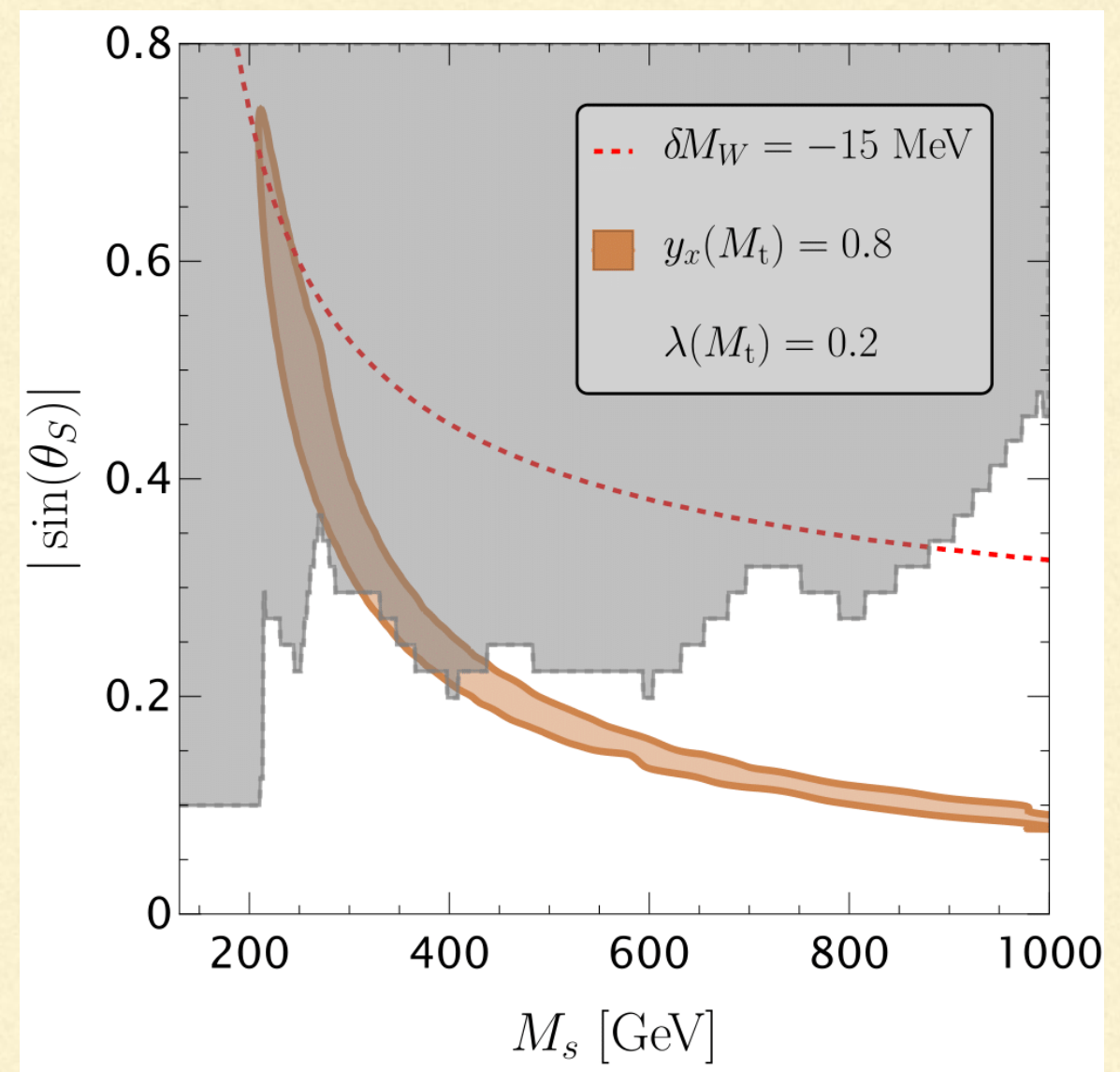
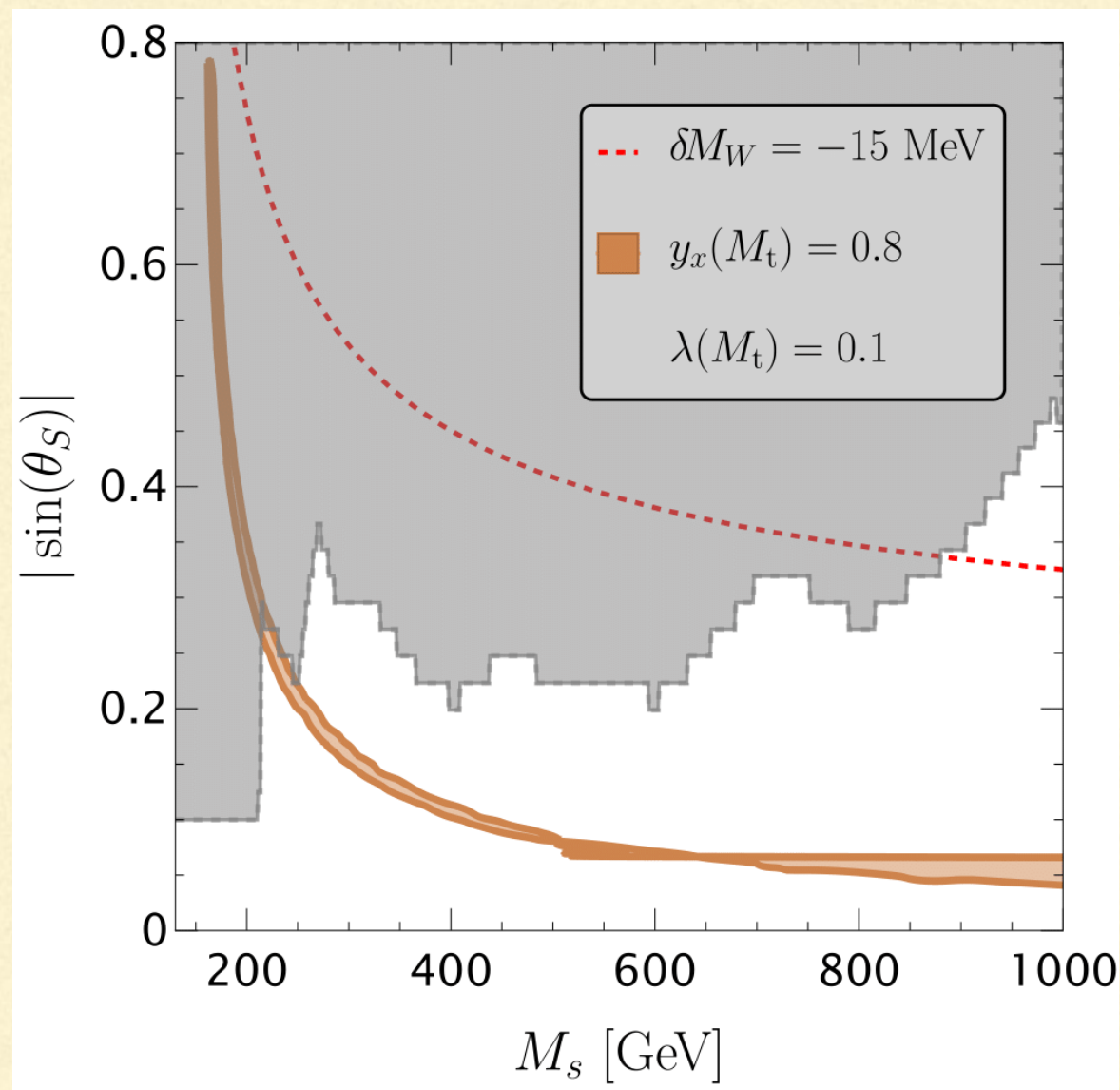




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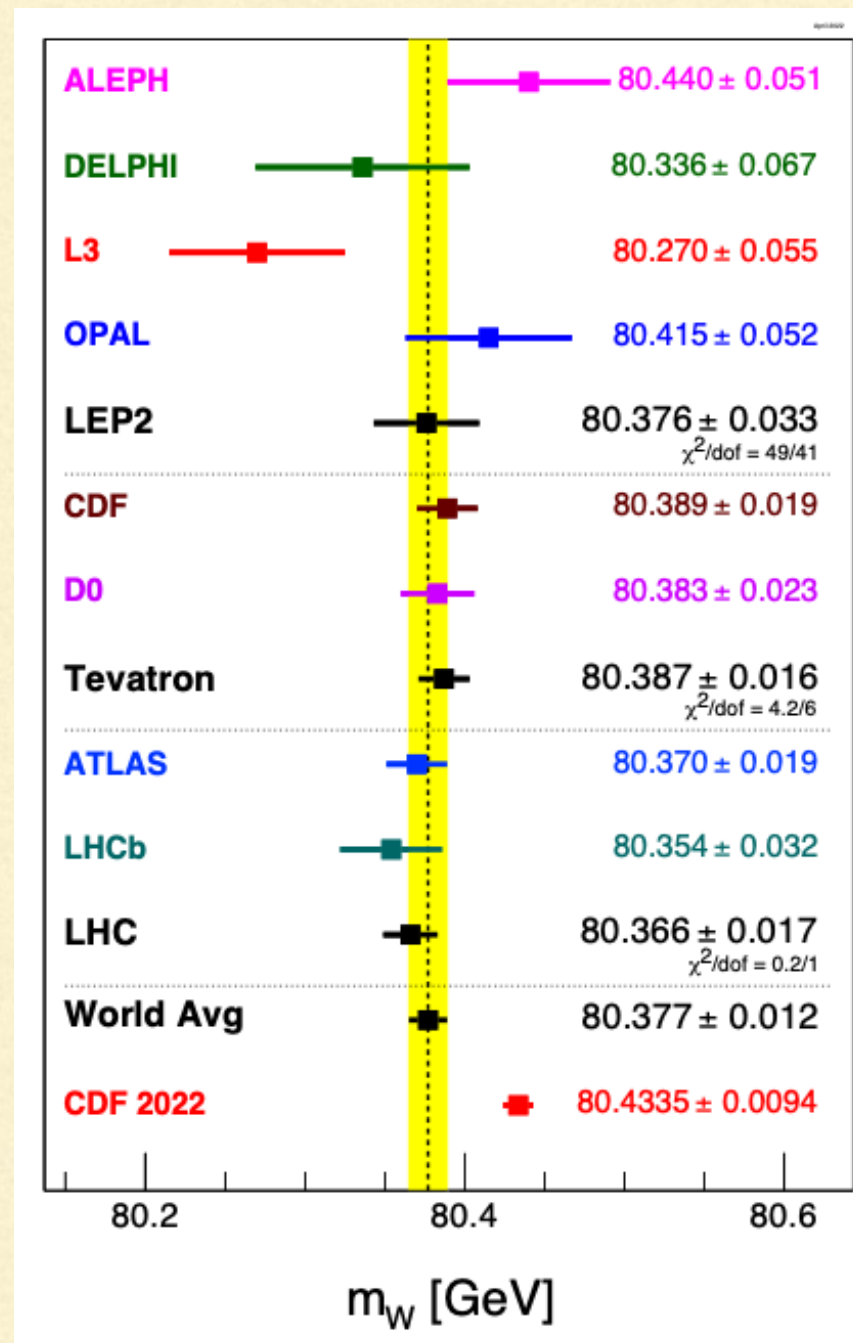
■  $M_s > M_h$ :

[Zoltán Péli and ZT, arXiv: [2204.07100](#)]





$M_W$  is measured and computed precisely  
(with per myriad precision)



[PDG 2023]



# Prediction of $M_W$ in the SWSM

(see Zoltán Péli's talk, [Zoltán Péli and ZT, arXiv: [2305.11931](#)])

- Can be determined from the decay width of the muon:

$$M_W^2 = \frac{\cos^2 \theta_Z M_Z^2 + \sin^2 \theta_Z M_{Z'}^2}{2} \left( 1 + \sqrt{1 - \frac{4\pi\alpha / (\sqrt{2}G_F)}{\cos^2 \theta_Z M_Z^2 + \sin^2 \theta_Z M_{Z'}^2} \frac{1}{1 - \Delta r_{SM} - (\Delta r_{BSM}^{(1)} + \Delta r_{BSM}^{(2)})}} \right)$$

- Valid in  $\overline{\text{MS}}$
- $\theta_Z$  is the  $Z - Z'$  mixing angle
- $\Delta r_{SM}$  collects the SM quantum corrections (known completely at two loops and partially at three loops)
- $\Delta r_{BSM}^{(1)}$  collects the formally SM quantum corrections but with BSM loops
- $\Delta r_{BSM}^{(2)}$  collects the BSM corrections to  $M_{Z'}$  and  $\theta_Z$



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# Conclusions

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- Established observations require physics beyond SM, but do not suggest rich BSM physics
- $U(1)_Z$  superweak extension has the potential of explaining all known results beyond the SM
- Neutrino masses are generated by SSB at tree level
- One-loop corrections to the tree-level neutrino mass matrix computed and found to be small (below 1‰) in the parameter space relevant in the SWSM
- Lightest sterile neutrino is a candidate DM particle in the [10,50] MeV mass range for freeze-out mechanism with resonant enhancement → predicts an approximate mass relation between vector boson and lightest sterile neutrino
- In the scalar sector we find non-empty parameter space for  $M_s > M_h$
- Contributions to EWPOs (e.g.  $M_W$ , lepton g-2) are negligible in the superweak region and a systematic exploration of the parameter space is ongoing



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the end

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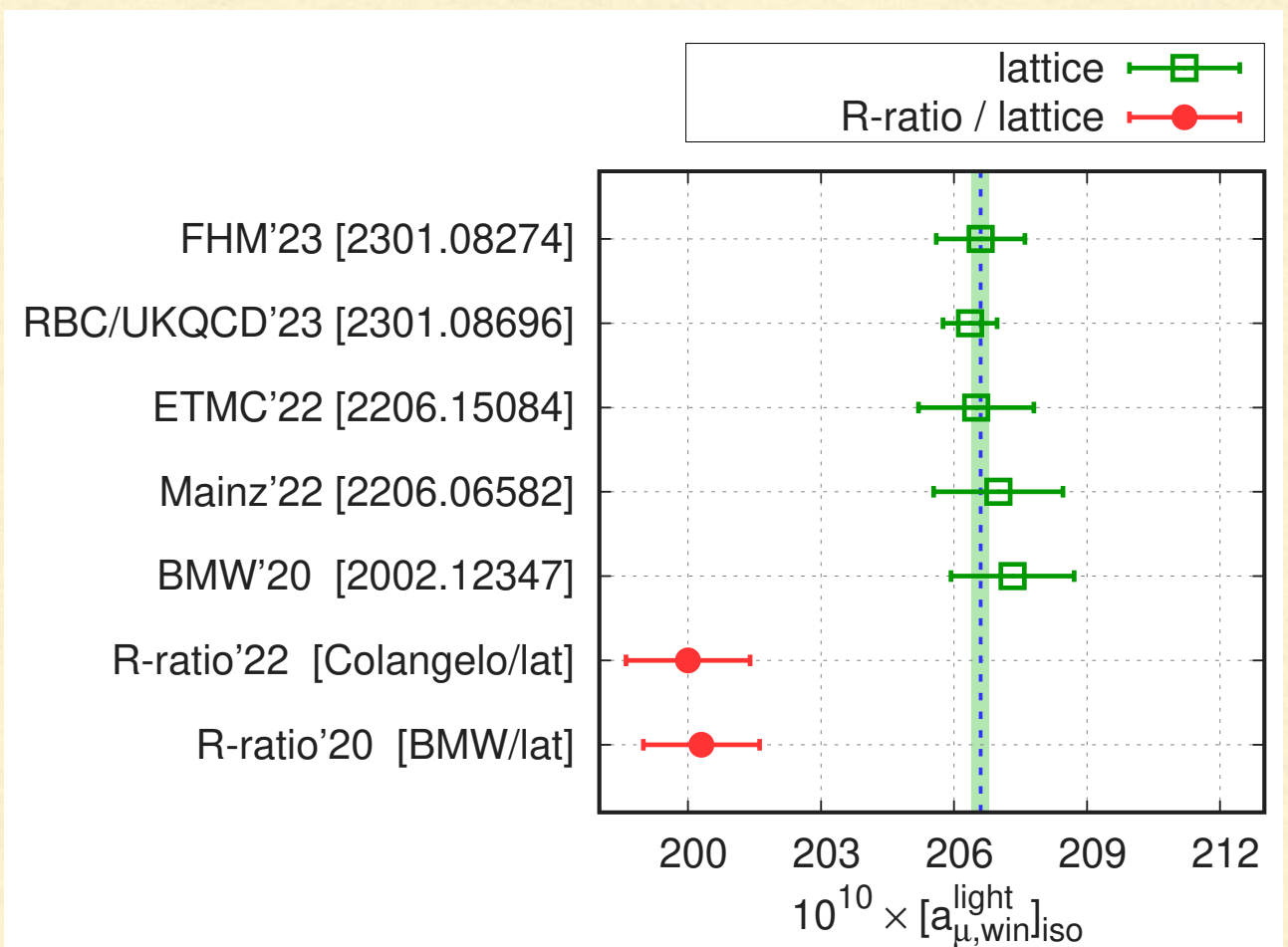
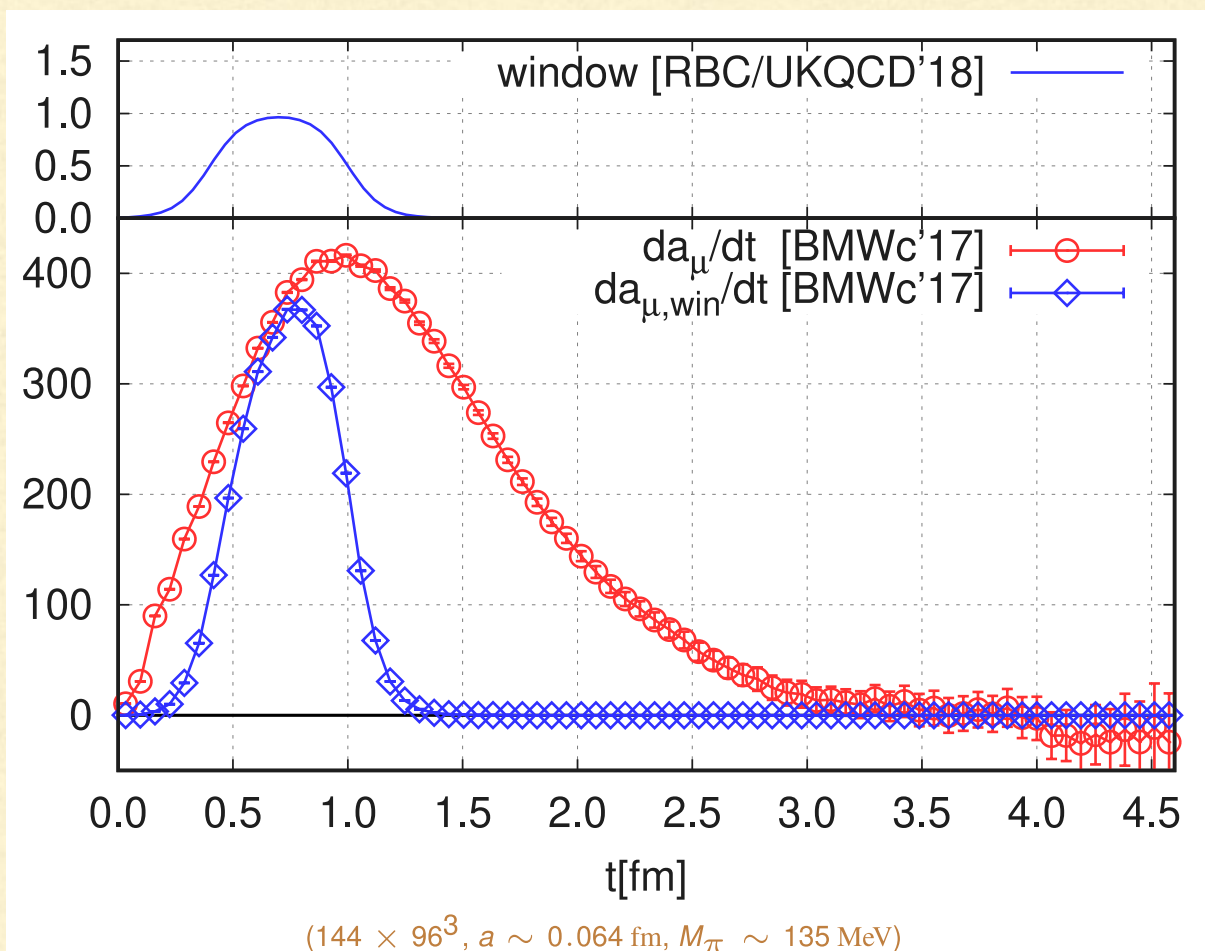
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# Appendix



# Status of the muon anomalous magnetic moment: window observable

- restrict correlation window to  $[0.4, 1.0]$  fm:
  - two orders of magnitude easier (less CPU, less manpower needed)
- lattice vs. R-ratio:  $4.9\sigma$  tension:





# Charge assignment from gauge invariant neutrino interactions

| field           | $SU(3)_c$ | $SU(2)_L$ | $y_j$          | $z_j^{(a)}$   | $z_j^{(b)}$    | $r_j = z_j/z_\phi - y_j^{(c)}$ |
|-----------------|-----------|-----------|----------------|---------------|----------------|--------------------------------|
| $U_L, D_L$      | 3         | 2         | $\frac{1}{6}$  | $Z_1$         | $\frac{1}{6}$  | 0                              |
| $U_R$           | 3         | 1         | $\frac{2}{3}$  | $Z_2$         | $\frac{7}{6}$  | $\frac{1}{2}$                  |
| $D_R$           | 3         | 1         | $-\frac{1}{3}$ | $2Z_1 - Z_2$  | $-\frac{5}{6}$ | $-\frac{1}{2}$                 |
| $\nu_L, \ell_L$ | 1         | 2         | $-\frac{1}{2}$ | $-3Z_1$       | $-\frac{1}{2}$ | 0                              |
| $\nu_R$         | 1         | 1         | 0              | $Z_2 - 4Z_1$  | $\frac{1}{2}$  | $\frac{1}{2}$                  |
| $\ell_R$        | 1         | 1         | -1             | $-2Z_1 - Z_2$ | $-\frac{3}{2}$ | $-\frac{1}{2}$                 |
| $\phi$          | 1         | 2         | $\frac{1}{2}$  | $z_\phi$      | 1              | $\frac{1}{2}$                  |
| $\chi$          | 1         | 1         | 0              | $z_\chi$      | -1             | -1                             |



# Non-standard interactions and the SWSM

[Timo J. Kärkäinen and ZT, arXiv: [2301.06621](https://arxiv.org/abs/2301.06621)]

$$\mathcal{O}_{6a} = \frac{C_{6a}}{\Lambda^2} (\bar{L} \gamma^\mu P_L L) (\bar{f} \gamma_\mu P_X f)$$

where  $\Lambda$  is the scale of new physics, can be as low as few MeV,  
which can be probed in

Coherent Elastic Neutrino-Nucleus Scattering (CEvNS)

Standard parametrization of NSI:

$$\mathcal{L}_{\text{NSI}} = -2\sqrt{2}G_F \sum_{f,X=\pm,\ell,\ell'} \varepsilon_{\ell,\ell'}^{f,X} (\bar{\nu}_\ell \gamma^\mu P_L \nu_{\ell'}) (\bar{f} \gamma_\mu P_X f)$$

where  $\varepsilon_{\ell,\ell'}^{f,X} \propto +\frac{1}{q^2}$  if  $q^2 \gg M^2$ , "light NSI" for a mediator  
 $\varepsilon_{\ell,\ell'}^{f,X} \propto -\frac{1}{M^2}$  if  $q^2 \ll M^2$ , "heavy NSI", of mass  $M$



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# Non-standard interactions and the SWSM

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assume  $M = 50 \text{ MeV}$ , which is

- light in CHARM or NuTEV  $q^2 = O((20 \text{ GeV})^2)$
- heavy in neutrino oscillation experiments  $q^2 \approx 0$
- but  $q^2 \approx M^2$  in CE $\nu$ NS

We can still apply the NSI formalism using the full propagator with  $q^2$  being the characteristic momentum transfer squared



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- Can be used to [Timo J. Kärkäinen and ZT, arXiv: [2301.06621](#)]
  - Constrain the parameter space of SWSM
  - Predict relations between NSI couplings assuming SWSM



# Non-standard interactions and the SWSM

- High-energy theory enforces texture for NSI matrix:

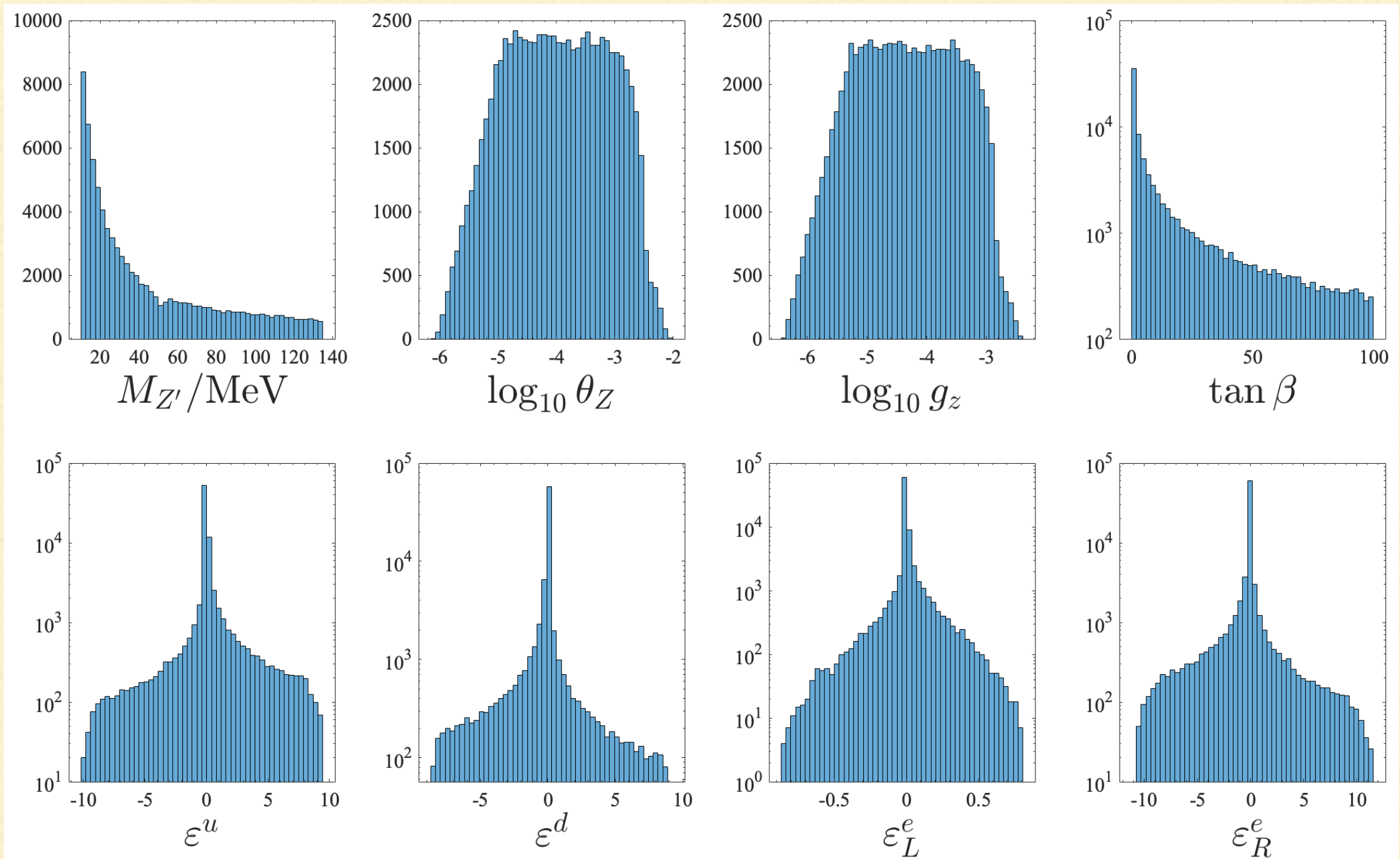
**SWSM**

|  |   |  |   |
|--|---|--|---|
| $\varepsilon_{\ell\ell}^m = \underbrace{\varepsilon_{\ell\ell}^e + 2\varepsilon_{\ell\ell}^u + \varepsilon_{\ell\ell}^d}_{=0} + \frac{N_n}{N_e}(\varepsilon_{\ell\ell}^u + 2\varepsilon_{\ell\ell}^d)$ | $\begin{pmatrix} \varepsilon_{ee}^m & \varepsilon_{e\mu}^m & \varepsilon_{e\tau}^m \\ \varepsilon_{e\mu}^{m*} & \varepsilon_{\mu\mu}^m & \varepsilon_{\mu\tau}^m \\ \varepsilon_{e\tau}^{m*} & \varepsilon_{\mu\tau}^{m*} & \varepsilon_{\tau\tau}^m \end{pmatrix}$ | $\begin{pmatrix} \varepsilon_e & 0 & 0 \\ 0 & \varepsilon_\mu & 0 \\ 0 & 0 & \varepsilon_\tau \end{pmatrix}$ | $\begin{pmatrix} \varepsilon & 0 & 0 \\ 0 & \varepsilon & 0 \\ 0 & 0 & \varepsilon \end{pmatrix}$ |
|  | $\mu - \tau$ symmetry   | Flavour-conserving   | Flavour-universal   |
| CLFV decays  | ✓   | No   | No  |
| $\nu$ oscillation  | ✓   | ✓  | No  |
| CE $\nu$ NS  | ✓   | ✓  | ✓   |
| $\nu$ scattering   | maybe   | maybe  | maybe   |

- Existing limits on NSI constrain the parameters of the high-energy theory



# Non-standard interactions and the SWSM: preferred regions of the parameters





# Non-standard interactions and the SWSM: preferred regions of the parameters

