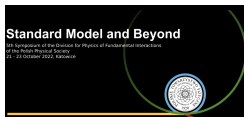


Phenomenological Aspects of Discrete Flavor Symmetries



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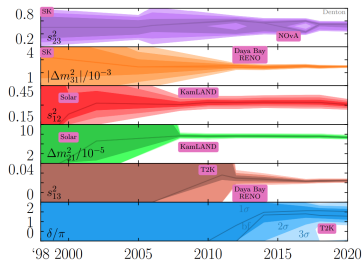
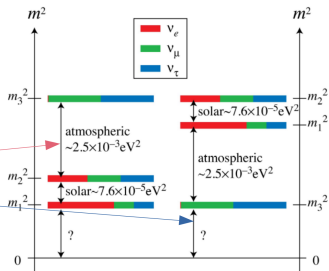
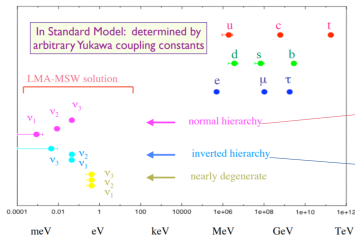
Based on 2203.08185, 2209.08610

Co-authors: G. Chauhan, P. S. Bhupal Dev, B. Dzierwit, W. Flieger, J. Ganguly, J. Gluza, K. Grzanka, J.

Vergeest, S. Zieba

Standar Model and Beyond, Katowice, Oct. 22, 2022

Parameters and the known unknowns : morning session talks, Ewa Rondio & others



	Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 2.6$)	
	bfp $\pm 1\sigma$	3 σ range	bfp $\pm 1\sigma$	3 σ range
$\sin^2 \theta_{12}$	$0.304^{+0.013}_{-0.012}$	$0.269 \rightarrow 0.343$	$0.304^{+0.012}_{-0.012}$	$0.269 \rightarrow 0.343$
$\theta_{12}/^\circ$	$33.44^{+0.77}_{-0.74}$	$31.27 \rightarrow 35.86$	$33.45^{+0.77}_{-0.74}$	$31.27 \rightarrow 35.87$
$\sin^2 \theta_{23}$	$0.573^{+0.018}_{-0.023}$	$0.405 \rightarrow 0.620$	$0.578^{+0.017}_{-0.021}$	$0.410 \rightarrow 0.623$
$\theta_{23}/^\circ$	$49.2^{+1.0}_{-1.3}$	$39.5 \rightarrow 52.0$	$49.5^{+1.0}_{-1.2}$	$39.8 \rightarrow 52.1$
$\sin^2 \theta_{13}$	$0.02220^{+0.00068}_{-0.00062}$	$0.02034 \rightarrow 0.02430$	$0.02238^{+0.00064}_{-0.00062}$	$0.02053 \rightarrow 0.02434$
$\theta_{13}/^\circ$	$8.57^{+0.13}_{-0.12}$	$8.20 \rightarrow 8.97$	$8.60^{+0.12}_{-0.12}$	$8.24 \rightarrow 8.98$
$\delta_{CP}/^\circ$	194^{+52}_{-25}	$105 \rightarrow 405$	287^{+27}_{-32}	$192 \rightarrow 361$
Δm_{21}^2	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$
Δm_{32}^2	$+2.515^{+0.028}_{-0.028}$	$+2.431 \rightarrow +2.599$	$-2.498^{+0.028}_{-0.029}$	$-2.584 \rightarrow -2.413$

Flavor symmetries, why?

$$U_{PMNS} = \begin{pmatrix} C_{12}C_{13} & S_{12}C_{13} & S_{13}e^{-i\delta} \\ -S_{12}C_{23} - C_{12}S_{13}S_{23}e^{i\delta} & C_{12}C_{23} - S_{12}S_{13}S_{23}e^{i\delta} & C_{13}S_{23} \\ S_{12}S_{23} - C_{12}S_{13}C_{23}e^{i\delta} & -C_{12}S_{23} - S_{12}S_{13}C_{23}e^{i\delta} & C_{13}C_{23} \end{pmatrix}$$

↓
(Prior to 2010)

$$s_{23} = 1/\sqrt{2} \ (\theta_{23} = 45^\circ) \text{ and } \theta_{13} = 0$$

$$U_0 = \begin{pmatrix} c_{12} & s_{12} & 0 \\ -\frac{s_{12}}{\sqrt{2}} & \frac{c_{12}}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ -\frac{s_{12}}{\sqrt{2}} & \frac{c_{12}}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

$\theta_{12} = 45^\circ$ ($s_{12} = 1/\sqrt{2}$)
Bimaximal Mixing

$\theta_{12} = 35.26^\circ$ ($s_{12} = 1/\sqrt{3}$)
Tribimaximal Mixing

$\theta_{12} = 31.7^\circ$
Golden Ratio Mixing

$\theta_{12} = 30^\circ$ ($s_{12} = 1/2$)
Hexagonal Mixing

$$U_0 = \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & 0 \\ -\frac{1}{2} & \frac{1}{2} & \frac{1}{\sqrt{2}} \\ \frac{1}{2} & -\frac{1}{2} & \frac{1}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} \sqrt{\frac{2}{3}} & \frac{1}{\sqrt{3}} & 0 \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & -\frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} \frac{\phi}{\sqrt{2+\phi}} & \frac{1}{\sqrt{2+\phi}} & 0 \\ \frac{-1}{\sqrt{4+2\phi}} & \frac{\phi}{\sqrt{4+2\phi}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{4+2\phi}} & \frac{-\phi}{\sqrt{4+2\phi}} & \frac{1}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} \sqrt{\frac{3}{4}} & \frac{1}{2} & 0 \\ -\frac{1}{2\sqrt{2}} & \frac{\sqrt{3}}{2\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ -\frac{1}{2\sqrt{2}} & \frac{\sqrt{3}}{2\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

Fukugita, Tanimoto, Yanagida PRD98; Harrison Perkins, Scott PLB02; Dutta, Ramond NPB03; Rodejohann et. al. EPJC10

(GR: $\tan \theta_{12} = 1/\phi$ where $\phi = (1 + \sqrt{5})/2$)

Flavor symmetries, why?

- Using the diagonalization relation

$$m_\nu = U_0^* \text{diag}(m_1, m_2, m_3) U_0^\dagger,$$

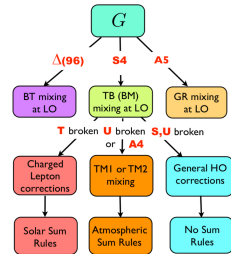
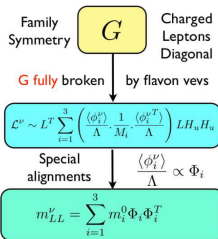
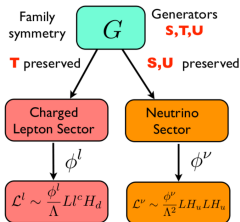
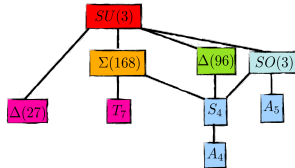
such a mixing matrices can easily diagonalize a $\mu - \tau$ symmetric (transformations $\nu_e \rightarrow \nu_e$, $\nu_\mu \rightarrow \nu_\tau$, $\nu_\tau \rightarrow \nu_\mu$ under which the neutrino mass term remains unchanged) neutrino mass matrix of the form

$$m_\nu = \begin{pmatrix} A & B & B \\ B & C & D \\ B & D & C \end{pmatrix},$$

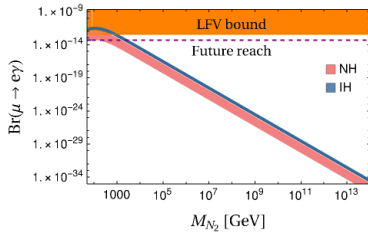
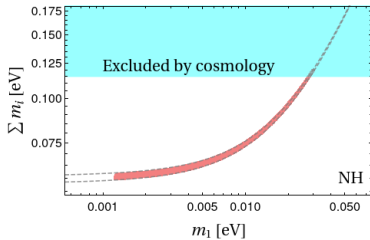
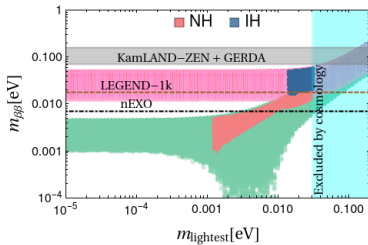
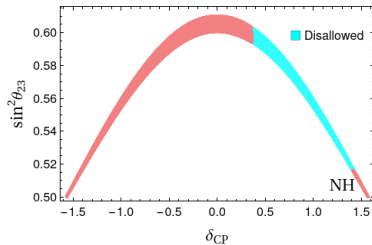
With $A + B = C + D$ this matrix yields tribimaximal mixing pattern where $s_{12} = 1/\sqrt{3}$ i.e., $\theta_{12} = 35.26^\circ$

General Framework

- Fundamental symmetry in the lepton sector can easily explain the origin of neutrino mixing which is considerably different from quark mixing.
- Incidentally, both Abelian or non-Abelian family symmetries have potential to shade light on the Yukawa couplings.
- The Abelian symmetries (such as Froggatt-Nielsen symmetry) only points towards a hierarchical structure of the Yukawa couplings.
- Non-Abelian symmetries are more equipped to explain the non-hierarchical structures of the observed lepton mixing as observed by the oscillation experiments. [S. F. King et al. 1301.1340](#)



Predictions: Ganguly, Gluza, BK 2209.08610



Flavor Symmetries in Various Frontiers:

⇒ Leptogenesis :

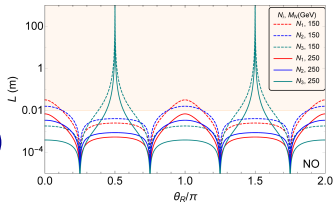
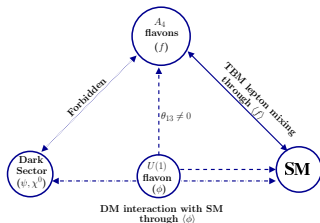
- The CP-violating out-of-equilibrium decay of RH neutrinos into lepton and Higgs doublets in the early universe produces a net lepton asymmetry [Fukugita, Yanagida, 1986; Covi, Roulet, Vissani 9605319](#)

$$\epsilon_i^\alpha = \frac{\Gamma(N_i \rightarrow \ell_\alpha H) - \Gamma(N_i \rightarrow \bar{\ell}_\alpha \bar{H})}{\Gamma(N_i \rightarrow \ell_\alpha H) + \Gamma(N_i \rightarrow \bar{\ell}_\alpha \bar{H})} = \frac{1}{8\pi} \sum_{j \neq i} \frac{\text{Im} \left[\left((\hat{Y}_\nu^\dagger \hat{Y}_\nu)_{ij} \right)^2 \right]}{(\hat{Y}_\nu^\dagger \hat{Y}_\nu)_{ii}} f \left(\frac{m_i^2}{m_j^2} \right),$$

$$f(x) = \sqrt{x} \left[\frac{2-x}{1-x} - (1-x) \ln \left(1 + \frac{1}{x} \right) \right] \text{ with } x = m_i^2/m_j^2$$

⇒ Dark Matter, Collider Physics :

- Can we extend flavor symmetry to the dark sector as well?, Can discrete symmetry play any role to ensure the stability of dark matter?
- Experiments are sensitive to the low-energy CP phases connected with flavor symmetry



Conclusion

- Is there any guiding principle behind observed pattern of lepton mixing ?
- (Discrete) flavor symmetry is one such potential candidate.
- What additional role they can play?
- How to falsify these plethora of models?
- If flavor symmetry is not the guiding principle, what else?



Thank you for your attention!!